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Assessing the Equalizing Force of Mobility Using Short Panels: France, 1990–2000

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In this paper, we document whether and how much the equalizing force of earnings mobility has changed in France in the 1990's. For this purpose, we use a representative three-year panel, the French Labour Force Survey. We develop a model of earnings dynamics that combines a flexible specification of marginal earnings distributions (to fit the large cross-sectional dimension of the data) with a tight parametric representation of the dynamics (adapted to the short time-series dimension). Log earnings are modelled as the sum of a deterministic component, an individual fixed effect and a transitory component which is assumed first-order Markov. The transition probability of the transitory component is modelled as a one-parameter Plackett copula. We estimate this model using a sequential expectation-maximization algorithm.

We exploit the estimated model to study employment/earnings inequality in France over the 1990–2002 period. We show that, in phase with business-cycle fluctuations (a recession in 1993 and two peaks in 1990 and 2000), earnings mobility decreases when cross-section inequality and unemployment risk increase. We simulate individual earnings trajectories and compute present values of lifetime earnings for various horizons. Inequality presents a hump-shaped evolution over the period, with a 9% increase between 1990 and 1995 and a decrease afterwards. Accounting for unemployment yields an increase of 11%. Moreover, this increase is persistent, as it translates into a 12% increase in the variance of log present values. The ratio of inequality in present values to inequality in one-year earnings, a natural measure of immobility or of the persistence of inequality, remains remarkably constant over the business cycle.

1. INTRODUCTION

It is generally agreed that measuring earnings dispersion in one single year does not provide an accurate picture of earnings inequality because forward-looking consumers can smooth transitory earnings shocks to some extent. The economist interested in measuring interpersonal differences in well-being can proceed in at least three ways: by studying consumption inequality directly—but the scarcity of consumer panels renders this approach difficult to implement in practice;¹ by emulating consumer behaviour and studying individual differences in long-run earnings averages (usually, five- or ten-year means); or by decomposing individual earnings dynamics into persistent and transitory components.

1. Yet see Cutler and Katz (1992), Attanasio and Davis (1996), Blundell and Preston (1998), and Krueger and Perri (2001).

The usual distinction between longer-run earnings inequality and earnings instability, or between persistent and transitory inequality, is at the heart of the approach theoretized by Shorrocks (1978), which measures mobility by comparing the inequality in multi-year earnings averages and annual earnings inequality.² However, in a changing macroeconomic environment it is difficult to separate persistent inequality from transitory fluctuations. For this reason, several authors have recently proposed to replace actual means by simulated means calculated on artificial data generated using a parameterized model. The model is either estimated on a short period supposed to be approximately stable (Flinn, 2002; Bowlus and Robin, 2004), or on a longer period if the model specification encompasses both individual dynamics and structural change (Haider, 2001).³ In both cases, for a given year, longer-run measures of earnings are calculated holding structural parameters constant at the level of that particular year. This allows documentation of changes in the persistence of inequality—and the equalizing force of mobility—over time.

In this paper, we follow the literature and model log earnings as the sum of two factors, an individual-specific fixed effect and a stationary stochastic component, with time-varying factor loadings.⁴ However, while the literature essentially focuses on first- and second-order moments, we aim at modelling the entire multivariate distribution of earnings in the most flexible way possible. Given an estimate of the full distribution, we are then able to simulate earnings trajectories and compute longer-run measures of inequality. Our model is designed to fit the French Labour Force Survey (LFS), a sequence of 11 large three-year panels from 1990–1992 to 2000–2002. Contrary to other well-used panels like the Panel study of Income Dynamics (PSID), labour force surveys such as the Survey of Income and Program Participation (SIPP), for example, typically follow large samples of individuals over short periods of time. The model therefore combines a flexible specification of marginal earnings distributions—to fit the large cross-sections—with a tight parametric specification of the dynamics—adapted to the small time-series dimension.

The distribution of the individual effect is assumed discrete with many support points. This allows us to use a simple expectation-maximization (EM) algorithm for estimation, the EM algorithm being particularly well suited to the estimation of discrete mixtures. The marginal density of the transitory component is a normal mixture, and in order to map the marginals into the joint distribution of couples of consecutive realizations we use a parametric copula. We find that Plackett (1965) one-parameter copula captures the year-to-year dynamics quite well. We also model transitions between employment and unemployment by a Markov chain that is conditional on the fixed effect.

The model being non-identified when factor loadings are allowed to vary freely over time, we assume that they vary sufficiently slowly and smoothly for each three-year panel to face a specific set of time-invariant factor loadings. For each three-year panel, the model thus takes the form of a mixture of non-linear first-order Markov models. The non-linearity renders identification difficult to characterize in a simple way. We, nevertheless, provide a set of functional restrictions under which the distributions of the fixed effect and the transitory shocks are non-parametrically identified. Identification holds assuming the injectivity of two non-linear operators. These

2. Moffitt and Gottschalk (2002) claim that five years is the minimal number of years for averaging earnings. “A shorter lag would [give] a more distorted picture of the growth of permanent variances because short lags would be contaminated by increasing transitory variances” (p. C72). For recent applications of this technique, see, for example, Burkhauser, Holtz-Eakin and Rhody (1997), Burkhauser and Poupore, (1997), Maasoumi and Trede (2001), Aaberge, Bjørklund, Jäntti, Palme, Pedersen, Smith and Wennemo (2002), and Van Kerm (2004).

3. Other examples of models of earnings dynamics with time-varying parameters can be found in Moffitt and Gottschalk (2002), Heathcote, Storesletten and Violante (2004), Meghir and Pistaferri (2004), Baker and Solon (2003), and Guvenen (2007).

4. Thus, unlike Flinn (2002) and Bowlus and Robin (2004) our modelling allows for unobserved heterogeneity (permanent components) in earnings.

assumptions, as in most inverse problems, cannot be translated into simple properties of the data-generating process.

Our model is closely related to Geweke and Keane (2000) first-order autoregressive model with an individual-specific drift and another AR(1) transitory component. They adopt a flexible specification (normal mixtures) for the distributions of transitory shocks.⁵ By comparison, our model has a more constrained dynamic structure that is adapted to very short panels. On the other hand, Geweke and Keane estimate a stationary model using 20 years of PSID data (1968–1989), while our framework allows parameters to change with the business cycle.

We start by documenting changes in earnings inequality, and in earnings and employment mobility in France in the 1990's. We show that the first half of the period is characterized by a simultaneous increase in earnings inequality, earnings immobility, and unemployment risk, and the second half by a symmetrical decrease. As 1988–1990 and 1998–2000 correspond to periods of fast growth and 1993 to a recession, business-cycle conditions appear strongly associated with individual earnings dynamics. This structural instability justifies a model of individual earnings dynamics with time-varying parameters. We then use the estimated model to simulate individual trajectories for each year of the 1990 decade and compute measures of inequality of present values (PVs) of earnings sequences of various lengths. Finally, by computing the ratio of the inequality in PVs to earnings inequality in one cross-section, we document how the equalizing force of mobility changed in the 1990's.

We find that the permanent component (fixed effect) has a nearly Gaussian distribution. The marginal distribution of the transitory component is leptokurtic, large shocks being much more probable than for a normal distribution. Unemployment is an important source of inequality. The variance of log monthly earnings increases by 9% between 1990 and 1995 and decreases afterwards. In contrast, imputing Unemployment Insurance (UI) benefits to unemployed workers using a replacement ratio of 60%, the variance of log income in the whole sample increases by 11% between 1990 and 1995. Moreover, this increase is persistent as the variance of the log PVs of lifetime earnings also increases by 12% in the same period, before decreasing at the end of that period. Lastly, the equalizing force of mobility changed remarkably little over the period.

The remainder of the paper is organized as follows. Section 2 precisely describes the model, and Section 3 discusses its identification. Section 4 presents the data. Section 5 describes the estimation method and presents parameter estimates, and Section 6 shows how the model fits the data. Section 7 shows the main results of the paper, comparing cross-sectional and longer-run earnings inequality in France in the 1990's. Section 8 provides some model comparison exercises. The last section concludes.

2. A MODEL OF EARNINGS DYNAMICS FOR SEQUENCES OF LARGE, SHORT PANELS

We consider a series of short panel datasets \mathcal{S}_j , $j = 1, \dots, J$, with many individual observations. Each subpanel \mathcal{S}_j records individual log earnings y_{it} and individual attributes x_{it} over a fixed time length T :

$$\mathcal{S}_j = \{(y_{it}, x_{it}), i = 1, \dots, N, t = t_j, t_j + 1, \dots, t_j + T - 1\},$$

where t_j denotes the first observation date for panel \mathcal{S}_j . So t_j represents the time at which individuals in \mathcal{S}_j enter the panel. For example, the LFS is a sequence of overlapping three-year panels ($T = 3$).

5. Geweke and Keane (2007) extend their 2000 paper by permitting state probabilities to depend on covariates.

We assume a standard formulation with three components, deterministic, permanent, and transitory, as

$$y_{it} = \beta_t x_{it} + \sigma_t \eta_i + \exp(\alpha_t x_{it}) \varepsilon_{it}, \quad t = t_j, \dots, t_j + T - 1, \quad (1)$$

with parameters (row-vectors) indexed by calendar time t . There are two error components: η_i is an individual-specific effect, and ε_{it} is a strongly stationary idiosyncratic component. Both error components have mean and variance normalized to 0 and 1, respectively, and factor loadings are left unrestricted.

We complete the specification of model (1) as follows.

2.1. Observed heterogeneity

The vector x_{it} of observed individual characteristics comprises experience, squared experience, and five education dummy variables: primary education (I), some high school (II), high school (III), some college (IV), and college graduate (V).

2.2. Unobserved heterogeneity/permanent component

We model unobserved heterogeneity η_i as a strictly exogenous random effect, with zero mean and unitary variance, independent of x_{it} for all t . We assume that η_i follows a discrete distribution with K support points, $\underline{\eta}_1, \dots, \underline{\eta}_K$, with respective probabilities p_1, \dots, p_K . The c.d.f. of η_i is thus

$$F_{\eta}(x) = \sum_{k=1}^K p_k \mathbf{1}\{x \geq \underline{\eta}_k\},$$

where $\mathbf{1}\{\cdot\}$ denotes the indicator function, with $\sum_{k=1}^K p_k \underline{\eta}_k = 0$ and $\sum_{k=1}^K p_k \underline{\eta}_k^2 = 1$.

The support points are chosen *a priori* to form a grid on \mathbb{R} . In the application, we set $\underline{\eta}_k = 2\Phi^{-1}(k/(K+1))$, for $k = 1, \dots, K$. We also set K large enough, and thus the grid fine enough, to approximate a continuous distribution well. The reason why we do not discretize the distribution of η_i in the frequency domain, like a normal mixture for instance, is that modelling η_i as a discrete variable will permit to exploit a simple EM algorithm for estimation.

2.3. Transitory component

We model ε_{it} as a strongly stationary first-order Markov process with zero marginal mean and unitary variance. The only non-stationarity in the transitory component of the log earnings process that is allowed for is the dependence to experience via the variance $\exp(2\alpha_t x_{it})$. In addition, the transitory variance depends on education.

The number of observation periods ($T = 3$) does not allow for a rich structure of state dependence. However, the model can be quite flexible as far as the marginal distribution of ε_{it} is concerned because of the very large sample size (more than 30,000 individuals in each subpanel of the French LFS; see Table 2). We thus use a flexible specification for the marginal distribution of ε_{it} , namely a mixture of $M = 3$ normal distributions. The c.d.f. of ε_{it} is

$$F_{\varepsilon_t}(x) = \sum_{m=1}^M \pi_{mt} \Phi\left(\frac{x - \mu_{mt}}{\omega_{mt}}\right),$$

with $\sum_{m=1}^M \pi_{mt} \mu_{mt} = 0$, and $\sum_{m=1}^M \pi_{mt} \omega_{mt}^2 = 1$.

In order to map the couples of marginal distributions of ε_{it} and $\varepsilon_{i,t+1}$ into the joint distributions of $(\varepsilon_{it}, \varepsilon_{i,t+1})$ we use a copula. Copulas are popular in financial econometrics for modelling

dependence structures.⁶ Formally, we specify the joint c.d.f. of ε_{it} and $\varepsilon_{i,t+1}$ as

$$F_{(\varepsilon_{it}, \varepsilon_{i,t+1})}(x, y) = C(F_{\varepsilon_t}(x), F_{\varepsilon_{t+1}}(y)), \quad (2)$$

where C denotes the copula. The copula is the joint c.d.f. of the ranks of variables ε_{it} and $\varepsilon_{i,t+1}$ in their respective marginal distributions. One can think of standard matrices of transition probabilities across earnings quintiles or deciles as discrete approximations of the copula density (the second-order partial cross-derivative of the copula).

A copula representation (2) exists for any strongly stationary first-order Markov process, and the copula is unique if the marginal c.d.f.'s F_{ε_t} and $F_{\varepsilon_{t+1}}$ are continuous (Sklar's theorem). The joint density of $(\varepsilon_{it}, \varepsilon_{i,t+1})$ is the product of the two marginal densities and the copula density. Compared to the standard decomposition of a joint density into the product of marginal and conditional densities, the copula representation is thus useful to the extent that it permits independent modelling of marginal distributions and dependence structures.

Copulas are widely used in finance to model correlation patterns, as, for example, default correlation in credit risk models. Here, our use of a copula is motivated by the asymmetry between the large cross-sectional dimension of the French LFS and its small time-series dimension ($T = 3$). A parametric copula allows us to tightly parameterize earnings mobility while keeping marginal distributions flexible. This goal would be more difficult to achieve using an autoregressive moving average (ARMA) model, as the same parameters govern both the marginal distributions and the dependence structure.

Interestingly, economic models do make predictions on the form of copulas. For example, we derive in Appendix A, the particular form of the copula of consecutive earnings for a discrete-time version of Burdett and Mortensen (1998) equilibrium search model. The steady-state equilibrium earnings distribution depends on the distribution of firm productivity and search-matching parameters. Yet, the copula only depends on the search-matching parameters, because individual mobility is possible in a steady-state economy only insofar as individuals exchange positions.

After testing several popular copula specifications on the French LFS data,⁷ we selected Plackett's one-parameter copula (see Appendix B for details):

$$C(u, v; \tau) = \frac{1}{2} \tau^{-1} \{1 + \tau(u + v) - [(1 + \tau(u + v))^2 - 4\tau(\tau + 1)uv]^{1/2}\}, \quad (3)$$

where $(u, v) \in [0, 1]^2$ are generic ranks. The copula parameter τ unambiguously indexes mobility from more mobile (low τ) to less mobile (high τ). In particular, Spearman's ρ is an increasing function of τ .⁸ We specify τ as a function of calendar time and observed heterogeneity:

$$\tau_t(x_{it}) \equiv \exp(\gamma_t x_{it}) - 1.$$

As an example, Table 1 compares the observed transition probabilities between two consecutive years to the predicted probabilities using Gaussian and Plackett copulas. The Gaussian copula is implicitly assumed in linear autoregressive models with normal margins. We see that it tends to underestimate the dependence in the middle of the distribution, that is, the probabilities of remaining in the second, third, and fourth quintiles.⁹

6. Copulas were initially introduced by Sklar (1959). See Nelsen (1998) and Joe (1997) for references on copulas in statistics and finance.

7. We tried Gaussian, Plackett, Frank, Gumbel, Joe, Clayton, FGM, and Log copulas.

8. Let X and Y be two random variables with c.d.f.'s F_X and F_Y , respectively. Spearman's ρ , or rank's correlation, is given by $\rho = \text{Corr}(F_X(X), F_Y(Y))$.

9. In order to compute the transition probabilities in Table 1 we first regress log earnings on experience and experience squared. We then compute earnings ranks using the empirical c.d.f. of log earnings residuals. Finally, we estimate the copula parameters by maximum likelihood, and compute transition probabilities.

TABLE 1
Fit of 1990–1991 transition probabilities across earnings quintiles

Observed					Gaussian					Plackett				
0.68	0.21	0.08	0.03	0.00	0.66	0.25	0.08	0.01	0.00	0.73	0.20	0.04	0.02	0.01
0.20	0.50	0.22	0.06	0.02	0.25	0.37	0.26	0.11	0.01	0.20	0.52	0.21	0.05	0.02
0.07	0.21	0.47	0.20	0.05	0.08	0.26	0.32	0.26	0.08	0.04	0.21	0.50	0.21	0.04
0.03	0.06	0.19	0.53	0.19	0.01	0.11	0.26	0.37	0.25	0.02	0.05	0.21	0.52	0.20
0.02	0.02	0.04	0.18	0.74	0.00	0.01	0.08	0.25	0.66	0.01	0.02	0.04	0.20	0.73

2.4. Unemployment

We also need to model transitions from and into unemployment. This is important for any reasonable description of labour market trajectories in France where unemployment rates are chronically above or around 10%. Let e_{it} be the binary variable that is equal to 1 if the individual is employed at time t and 0 otherwise. We assume that

$$e_{i1} = \mathbf{1}\{\delta_{01}x_{i1} + \zeta_{01}\eta_i + \xi_{i1} > 0\}, \quad (4)$$

$$e_{it} = \mathbf{1}\{\rho_t e_{i,t-1} + \delta_{1t}x_{it} + \zeta_{1t}\eta_i + \xi_{it} > 0\}, \quad t=2, \dots, T, \quad (5)$$

where ξ_{i1} and ξ_{it} , $t = 2, \dots, T$, follow independent standard normal distributions.¹⁰ All parameters are indexed by calendar time t .

3. IDENTIFICATION

In this section, we first discuss the identification of the time-dependent variance and covariance/copula parameters. Then, we discuss the non-parametric identification of marginal distributions of persistent and transitory components.

3.1. Structural change

Consider the following simplified version of model (1) without covariates:

$$y_{it} = \sigma_t \eta_i + \omega_t \varepsilon_{it}, \quad t = 1, \dots, T,$$

$$\text{Var}\eta_i = \text{Var}\varepsilon_{it} = 1, \quad \text{Cov}(\varepsilon_{it}, \varepsilon_{i,t-1}) = \tau_t,$$

where, to simplify the notation, we use the same symbol for the covariances and the copula parameters, τ_t . With T observations per individual, the number of parameters to estimate is $3T - 1$ and the number of non-redundant data covariances, $\text{Cov}(y_{it}, y_{it'})$, is $T(T + 1)/2$. Clearly, the second-order parameters σ_t , ω_t and τ_t are not identifiable from second-order moments if $T = 3$ (six moments for eight parameters). It is only for $T \geq 5$ that the number of moment conditions is greater than the number of parameters. Moreover, having several overlapping subpanels does not help much. For example, with two subsequent three-year panels we have nine moments for 11 parameters.

To ensure identification, we thus have to restrict the way σ_t , ω_t , and τ_t vary with time. Our solution is to assume that structural change is smooth. We make this statement precise by assuming that σ_t , ω_t , and τ_t can be assumed constant within each three-year panel. That is, instead

10. Note that an alternative would have been to non-parametrically model the unemployment probabilities by education and experience cells. However, this approach is difficult to implement when the number of support points for η_i (K) gets large, because of the usual curse of dimensionality.

of indexing parameters on calendar time, we index them on the subpanel index j as σ_j, ω_j , and τ_j . The cost of making this assumption is that individuals may face different structural parameters in the same year t , depending on when they entered the panel (t_j). Alternatively, one could parameterize the dependence of parameters on calendar time using polynomials, for example. However, this would impose more restrictions across panels. In comparison, our preferred solution is simpler to implement and is reminiscent of the idea of using moving averages to smoothen time series.

In practice, some additional smoothing is necessary. Our first attempts at estimating the model with only panel index dependence resulted in rather imprecise estimates, yet displaying clear patterns. Eventually, we chose the following specification:

- Parameters $\beta_j, \pi_{mj}, \mu_{mj}, \omega_{mj}$ vary with j without restriction.
- Parameters $\sigma_j, \zeta_{0j}, \rho_j, \zeta_{1j}$ vary with j as cubic polynomials.
- For parameters $\alpha_j, \gamma_j, \delta_{0j}, \delta_{1j}$: the intercept and the parameters of education dummies vary with j as cubic polynomials, while the parameters of experience and experience squared do not depend on j .

3.2. Non-parametric identification of the stationary model

Let us now consider the stationary model

$$y_{it} = \eta_i + \varepsilon_{it},$$

with only three observations per individual (say $t = 1, 2, 3$). We assume that η_i is independent of (ε_{it}) . Let F_X be a generic notation for the c.d.f. of a random variable X , with density $f_X = F'_X$.

If (ε_{it}) is independently distributed, then the marginal distributions of η_i and ε_{it} are non-parametrically identified from the joint distribution of (y_{it}) (see Kotlarski, 1967). If (ε_{it}) is first-order Markov with C being the copula of $(\varepsilon_{it}, \varepsilon_{it+1})$, then the following argument shows how to reconstruct F_η, F_ε , and C from the joint distribution of (y_{i1}, y_{i2}, y_{i3}) .

Start by assuming that the distribution of the individual-specific effect η_i is known. The distribution F_ε can be uniquely obtained by deconvolution, for example, under the assumption that the characteristic function of η_i is everywhere different from 0. Then, consider the joint distribution of (y_{i1}, y_{i2}) :

$$F_{y_1, y_2}(x_1, x_2) = \int f_\eta(z) C[F_\varepsilon(x_1 - z), F_\varepsilon(x_2 - z)] dz.$$

Suppose that the operator mapping C into F_{y_1, y_2} given f_η, F_ε is injective,¹¹ then one can recover C uniquely given F_η . Lastly, consider for example the distribution of (y_{i1}, y_{i3}) :

$$F_{y_1, y_3}(x_1, x_3) = \int f_\eta(z) \left[\int_0^1 \partial_2 C(F_\varepsilon(x_1 - z), v) \partial_1 C(v, F_\varepsilon(x_3 - z)) dv \right] dz,$$

where $\partial_1 C$ and $\partial_2 C$ denote the partial derivatives of C . Making use of the previous derivations of F_ε and C as functions of f_η , this equation defines another inverse problem that has a unique solution if the operator mapping f_η into F_{y_1, y_3} is injective.

The practical implementation of this identification algorithm is not trivial. We eventually decided to use a flexible parametric model, with a discrete approximation for the distribution

11. The injectivity of this operator depends on properties of the distributions of η_i and ε_{it} . Characterizing the identifying assumptions at this deeper fundamental level is a difficult task that is outside the scope of this paper.

of η_i , a mixture of three normal distributions for the distribution of ε_{it} , and a parsimonious specification of the copula C .¹²

4. THE DATA

The study is based on data drawn from the 1990–2002 French Labour Force Survey (LFS), conducted by INSEE, the French statistical institute. This survey is a rotating panel, a third of the sampling units (dwellings) being replaced, every year, by an equivalent number of new units. The 1990–2002 data contain 11 subpanels indexed by the date of entry of individuals, from 1990–1992 to 2000–2002. Each subpanel has about 150,000 individuals aged 15 or more, in 75,000 households, which are thus interviewed three times, in March of three subsequent years, about various aspects of their employment histories. We use LFS data instead of administrative earnings data, as in Alvarez, Browning and Ejrnæs (2002), because the French register data (DADS) do not follow individuals moving to public jobs, self-employment, or non-employment. Moreover, administrative data contain limited information on individual characteristics.

4.1. *Sample construction*

Self-reported usual weekly hours worked are likely to be mismeasured. For instance, we notice that many individuals alternatively report 39 hours worked in one week (the legal working time in the 1990's), and 40 hours in another. To limit the influence of measurement error in hours on our results, we use monthly earnings rather than hourly wages. The employment status is measured at the time of the interview as well as earnings. Monthly earnings are deflated by the retail price index. We drop all earnings observations for students, retirees and self-employed workers. We only keep male employment/earnings trajectories to limit the role of labour supply as a determinant of earnings dispersion. Finally, we trim earnings below the first and above the ninety ninth percentiles.

Geographical mobility, among other reasons, generates a significant amount of attrition. Only 53% of the individuals of the sample have complete trajectories, 25% drop out after the second year, and 22% after the first year. We assume attrition exogenous to the employment-earnings process.

4.2. *Descriptive statistics*

Table 2 shows a few descriptive statistics. All reported quantities are weighted using the LFS weights. The upper part of the table displays these statistics by calendar year, from 1990 to 2000. We see that the French working population is slightly ageing between 1990 and 2002 and is also becoming more educated. The log earnings variance increases from 0.171 in 1990 to 0.186 in 1996, and returns to 0.178 in 2000. The amplitude of the increase is 8.8%. The unemployment rate (in the sample) sharply increases at the beginning of the period, from 9.5% in 1991 to 14.1% in 1994, then remains roughly constant between 1994 and 1999, and drops to 11.6% in 2000.

The lower part of the table completes the description by showing statistics by date of entry in the panel: from 1990(–1992) to 2000(–2002).¹³ We document average earnings growth and relative earnings immobility, as measured by Spearman's ρ (rank's correlation), over one or two

12. Our estimation results will show that when we increase the number of support points for the distribution of η_i , the estimated discrete distribution apparently converges to a continuous limit (see Figure 1).

13. All individuals in the 1990 cross-section are treated as individuals entering the panel in 1990 because, in the estimation, we are not estimating separate parameters for the 1988 and 1989 cohorts, earnings data being measured by interval before 1990. A proper treatment of the cohorts of individuals entering the LFS panel before 1990 would have thus required a more complicated model.

TABLE 2
Data description, by calendar year and by year of entry in the panel

<i>t</i>	1990	1991	1992	1993	1994	1995	1996	1997	1998	1999	2000
By calendar year											
Number of individuals	32,749	32,402	32,855	34,629	35,689	35,674	35,780	34,927	34,945	35,309	35,376
Age	37.9	38.0	38.1	38.2	38.4	38.6	38.8	39.0	39.1	39.2	39.3
Age at the end of school	17.5	17.5	17.6	17.8	17.9	18.0	18.1	18.2	18.3	18.5	18.6
<i>Earnings</i>											
Mean log earnings	8.90	8.92	8.93	8.94	8.93	8.92	8.91	8.92	8.92	8.93	8.93
Log earnings variance	0.171	0.173	0.172	0.179	0.183	0.185	0.186	0.186	0.179	0.178	0.178
Unemployment probability	0.098	0.095	0.107	0.123	0.141	0.130	0.135	0.141	0.134	0.137	0.116
By year of entry in the panel											
Nb of individuals entering at <i>t</i>	32,749	16,156	16,022	16,955	17,151	16,643	17,030	16,599	16,947	17,157	17,869
Nb present at <i>t+1</i>	16,246	10,294	10,652	11,229	11,236	10,899	10,973	10,543	10,897	10,492	10,995
Nb present at <i>t+2</i>	6539	7022	7409	7795	7851	7355	7455	7255	7015	6938	7204
Age	38.7	38.1	38.2	38.4	38.6	38.8	38.9	39.2	39.2	39.4	39.2
Age at the end of school	17.4	17.6	17.7	17.9	18.0	18.1	18.2	18.3	18.4	18.6	18.6
<i>Earnings</i>											
Mean log earnings	8.92	8.93	8.92	8.94	8.92	8.92	8.92	8.92	8.92	8.94	8.94
Log earnings variance	0.166	0.173	0.177	0.181	0.185	0.188	0.184	0.182	0.179	0.179	0.173
Earnings growth over 1 year	0.027	0.013	0.008	0.009	0.012	0.010	0.021	0.027	0.025	0.026	0.026
Earnings growth over 2 years	0.042	0.023	0.016	0.018	0.015	0.017	0.040	0.047	0.044	0.046	0.044
Spearman ρ over 1 year	0.866	0.869	0.887	0.902	0.901	0.900	0.905	0.902	0.896	0.891	0.892
Spearman ρ over 2 years	0.851	0.859	0.872	0.883	0.885	0.892	0.890	0.882	0.886	0.871	0.861
<i>Unemployment probability</i>											
Marginal	0.091	0.099	0.119	0.126	0.140	0.131	0.134	0.142	0.131	0.128	0.112
Transition from employment	0.034	0.041	0.050	0.045	0.042	0.041	0.040	0.037	0.038	0.030	0.033
Transition from unemployment	0.63	0.65	0.66	0.65	0.64	0.67	0.68	0.66	0.64	0.61	0.64

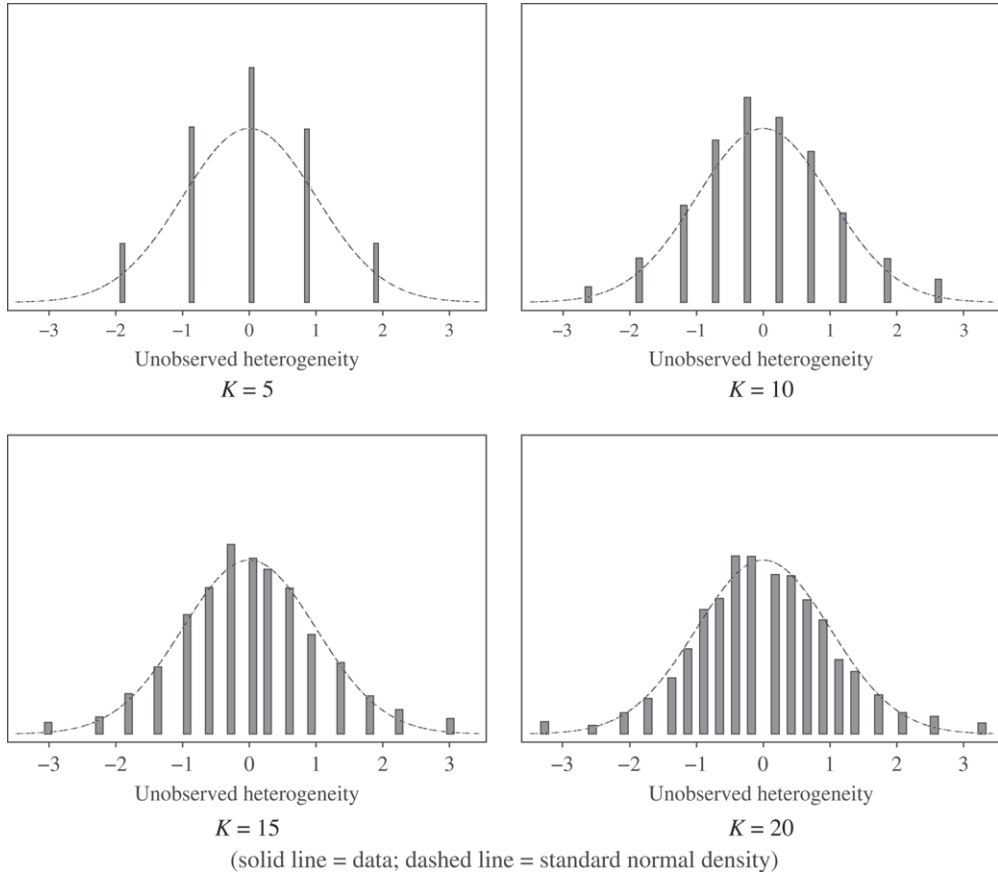


FIGURE 1

Distribution of unobserved heterogeneity, η_i , for different values of K , the number of support points

years. Earnings mobility clearly decreases in the first half of the decade and increases in the second half.

Overall, the first half of the 1990's is thus characterized by a simultaneous increase in earnings inequality, earnings immobility and unemployment risk, and the second half by a symmetrical decrease.

5. ESTIMATION RESULTS

The true value of the unobserved heterogeneity component η_i being equal to η_k with probability p_k , the likelihood for one individual observation is a discrete mixture. We take advantage of this property in the estimation to develop a sequential variant of the EM algorithm that is detailed in Appendix C. Using arguments similar to Arcidiacono and Jones (2003), this estimation procedure can be shown to deliver a consistent estimator of the model's parameters, asymptotically equivalent to a GMM estimator. This algorithm is very simple to implement but is slow to converge, as usually are EM-type algorithms. It delivers, as a by-product of the estimation, the posterior probabilities of unknown types η_k , which can be used to simulate individual trajectories.

In the remainder of this section, we present the parameter estimates that the EM algorithm delivers for all subpanels 1990–1992 to 2000–2002.

TABLE 3
Parameter estimates for subpanel 1990–1992

	Log earnings			Unemployment	
	Mean (β, σ)	Volatility (α)	Mobility (γ)	Initial (δ_0, ζ_0)	Transition (δ, ρ, ζ_1)
Expe	0.03776 (0.00112)	-0.01172 (0.0191)	0.06154 (0.00713)	-0.1104 (0.00351)	-0.05234 (0.00538)
(100×) Expe ²	-0.06113 (0.00237)	0.07065 (0.0380)	-0.04738 (0.0144)	0.2154 (0.00751)	0.1049 (0.0110)
Educ II	0.1850 (0.00808)	0.1206 (0.187)	0.1026 (0.0462)	-0.5928 (0.0259)	-0.2576 (0.0347)
Educ III	0.4269 (0.0104)	0.7416 (0.194)	0.7007 (0.0586)	-0.8137 (0.0374)	-0.4092 (0.0518)
Educ IV	0.5869 (0.0137)	0.5230 (0.264)	0.6368 (0.0766)	-1.282 (0.0636)	-0.4968 (0.0770)
Educ V	0.8952 (0.0134)	1.086 (0.206)	0.9898 (0.0747)	-1.315 (0.0633)	-0.6853 (0.0863)
η_i	0.2304 (0.00321)	-	-	-0.7775 (0.0137)	-0.3334 (0.0167)
$e_{i,t-1}$	-	-	-	-	1.744 (0.0384)
Constant	8.173 (0.0130)	-3.486 (0.266)	1.107 (0.0869)	-0.1165 (0.0354)	-1.115 (0.0612)

Notes: educ, education; expe, experience.

5.1. Distribution of unobserved heterogeneity

Figure 1 shows the distribution of the individual effect η_i for different choices of support. We draw the density of the standard normal distribution for comparison. There is clear evidence of a “convergence” of the distribution of η_i to a continuous density when K increases. Moreover, this density resembles a standard normal density. This finding is consistent with what Horowitz and Markatou (1996) found for the U.S., using a model with an individual-specific effect and i.i.d. transitory shocks. It is also consistent with the idea that the unobserved heterogeneity component aggregates many missing individual characteristics.

5.2. Effects of covariates

Table 3 displays parameter estimates for subpanel 1990–1992, all other subpanels yielding similar estimates. Asymptotic S.E.’s are given in parentheses.¹⁴

The mean log earnings is concave in experience, with a maximum at 31 years. The copula parameter is monotonically increasing in experience, and so relative mobility decreases with experience. The relation between unemployment risk and experience is U-shaped, with a minimum at 25 years of experience. This is true for the initial probability of being unemployed as well as for the transition probabilities into unemployment. Lastly, the log earnings volatility (*i.e.* the variance of the transitory component) is U-shaped in experience: it initially decreases with experience, and starts to increase after eight years.

Education has an increasing effect on the mean log earnings and the log earnings volatility, and a decreasing effect on mobility and unemployment risk. The unobserved heterogeneity component η_i has the same effects as education. Lastly, the strong positive effect of e_{it-1} on e_{it} shows that the employment status is highly persistent, even after accounting for unobserved heterogeneity.

14. We report the asymptotic S.E.’s of the last EM step before numerical convergence, that is, taking the prior probability of each heterogeneity type as given. These are thus likely to be understated.

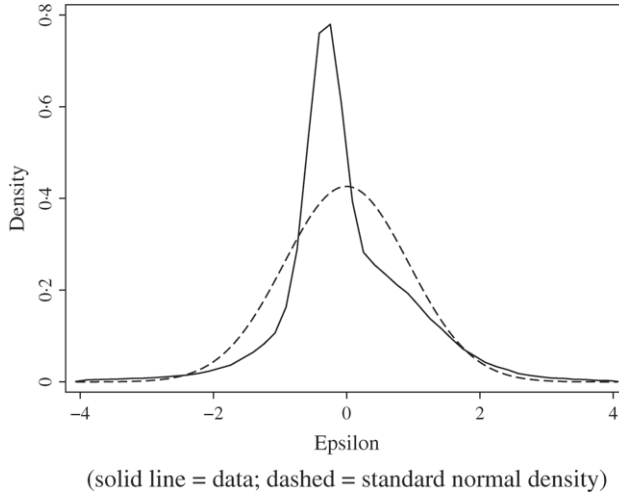


FIGURE 2

Density of ε_{it} for subpanel 1990–1992

On Figure 2 we draw the density of ε_{it} . We observe that the distribution is highly non-normal, displaying a very peaked mode and some skewness to the left. This visual impression is confirmed by the skewness and kurtosis values equal to 0.26 and 7.5, respectively. The non-normality of transitory shocks ε_{it} contrasts with the near-normality of the permanent component η_i . Using a much longer panel, Geweke and Keane (2000) also find strong evidence of leptokurtic transitory shocks (but they constrain individual-specific effects to be Gaussian).

5.3. Changes across subpanels

The left panel in Figure 3 shows the evolution of the variance of the deterministic component of log earnings, that is, $\text{Var}(\beta_j x_{it})$. It increases from 0.070 in 1990–1992 to 0.081 in 1995–1997 (a 16% increase), and returns to its initial level in 2000–2002.

In Table 4 we report the results of an Oaxaca decomposition, taking 1990–1992 as reference. The contribution of age and education to the log earnings variance (row labelled “composition effects” in the Table) increases in France in the 1990’s because the average age and education of the labour force increase in this period (see Table 2). Composition effects account for six percentage points (out of 16) of the rise of the log earnings variance between 1990–1992 and 1995–1997. Allowing returns to education to change (in the second row), the variance decreases. This is because returns to education decrease in France in the 1990’s (see Figure 4). At the same time, returns to experience increase very steeply during the first half of the 1990’s (30%) and compensate for some of the variance reduction due to lower returns to education.¹⁵

The central and right panels in Figure 3 display the evolution of two key parameters, that we shall refer to as the *permanent* and *transitory* components of the log earnings variance. The first parameter is σ_j^2 , and is approximately equal to the variance of the effect of unobserved heterogeneity η_i on log earnings.¹⁶ The second parameter is the average volatility, namely the

15. The effect of experience on the mean log earnings is quadratic in the model, so the return to experience is linear in experience. The mean return in the sample is reported on the right panel of Figure 4.

16. The variance of η_i in the sample of employed workers is not exactly equal to 1 because unemployment risk also depends on x_{it} and η_i , and, therefore, the sample of employed workers, for whom we observe earnings, is endogenously selected.

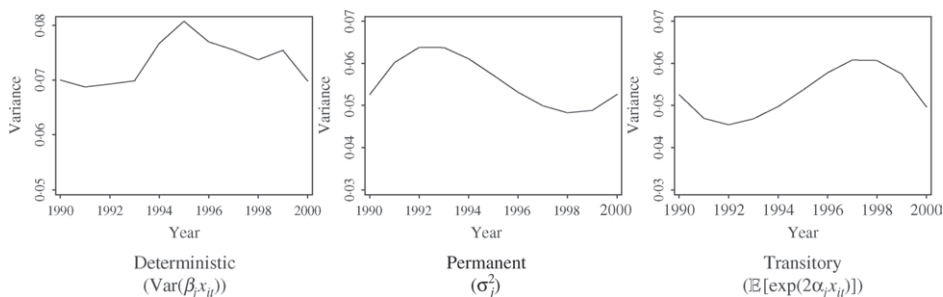


FIGURE 3

Decomposition of the cross-sectional variance of log earnings, subpanels 1990–1992 to 2000–2002

TABLE 4

Oaxaca decomposition of the deterministic component of the variance of log earnings (reference = 1990–1992)

	1990	1993	1995	1997	2000
Composition effects	0.0700	0.0704	0.0741	0.0734	0.0742
+ Returns to education	0.0700	0.0700	0.0733	0.0696	0.0666
+ Returns to experience	0.0700	0.0699	0.0807	0.0755	0.0698

mean of $\exp(2\alpha_j x_{it})$ (the square of $\exp(\alpha_j x_{it})$). Figure 3 shows that the deterministic, permanent and transitory components respectively account for about 40%, 30% and 30% of the log earnings variance. Moreover, permanent and transitory variances follow opposite business-cycle dynamics. While the permanent component increased by 20% at the beginning of the observation period, to reach a peak in 1992–1994, meanwhile, the transitory component decreased by 15%. In the 1993 recession, the effect of the permanent component is reinforced while the transitory variance is reduced.¹⁷

6. MODEL FIT

In this section, we evaluate the capacity of the model to reproduce the main features of the data.

6.1. Marginal earnings distribution and earnings dynamics in 1990–1992

Figures 5 and 6 compare actual and predicted distributions of log earnings levels y_{it} and log earnings residuals $u_{it} = y_{it} - \beta_j x_{it}$ for 1990–1992.¹⁸ In Figure 5, we separately consider the distribution of levels, y_{it} , the distributions of first and second differences, $y_{it} - y_{it-1}$ and $y_{it} - y_{it-2}$, and the distribution of three-year averages, $(y_{it} + y_{it+1} + y_{it+2})/3$. Figure 6 repeats this comparison study for residuals. Overall, the fit is good although the model does not fully succeed

17. Baker and Solon (2003) find, using Canadian tax records, that both persistent and transitory variances increased during the recessions of 1982–1983 and 1991–1992. Haider (2001), using U.S. data from the PSID for the period 1967–1991, finds that the transitory variance increased more during recessions. In comparison, our results could point at a special nature of the 1993 recession in France. However, given the lack of studies covering the period post-1990, it is hard to say how specific to the French context our results are.

18. We predicted these distributions by simulation, using parameters estimated on the subpanel 1990–1992. This requires to simulate transitory shocks from the copula model. We briefly explain how this can be done at the end of Appendix B.

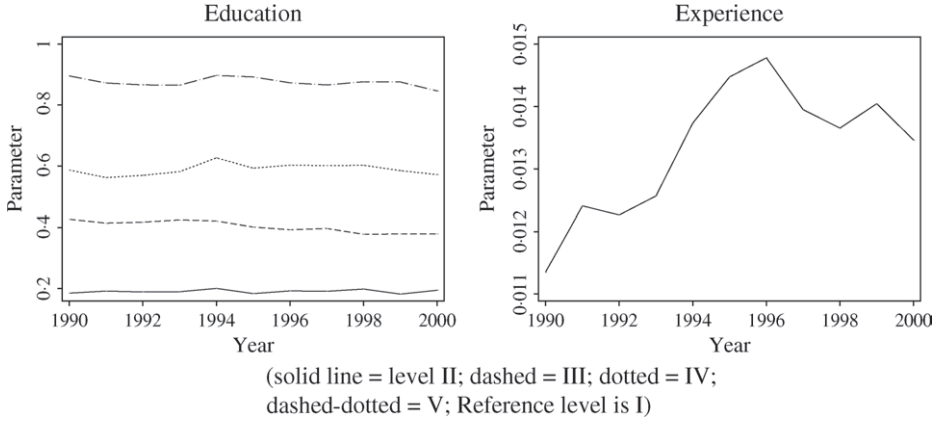


FIGURE 4
Average returns to education and experience

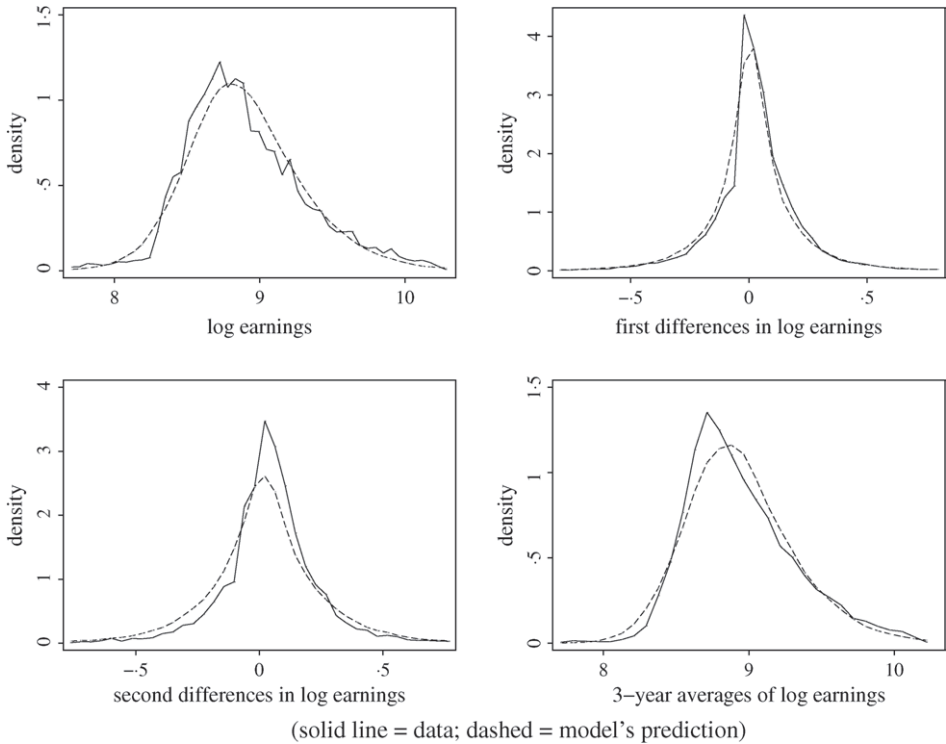


FIGURE 5
Fit of the marginal distributions of log earnings levels (subpanel 1990–1992)

in capturing the peak of the distribution of second differences. Moreover, comparing the upper left and lower right panels on the two figures shows that the additive structure of the model fails to fit the skewness of log earnings precisely, though the full distribution of log earnings residuals is very well fitted.

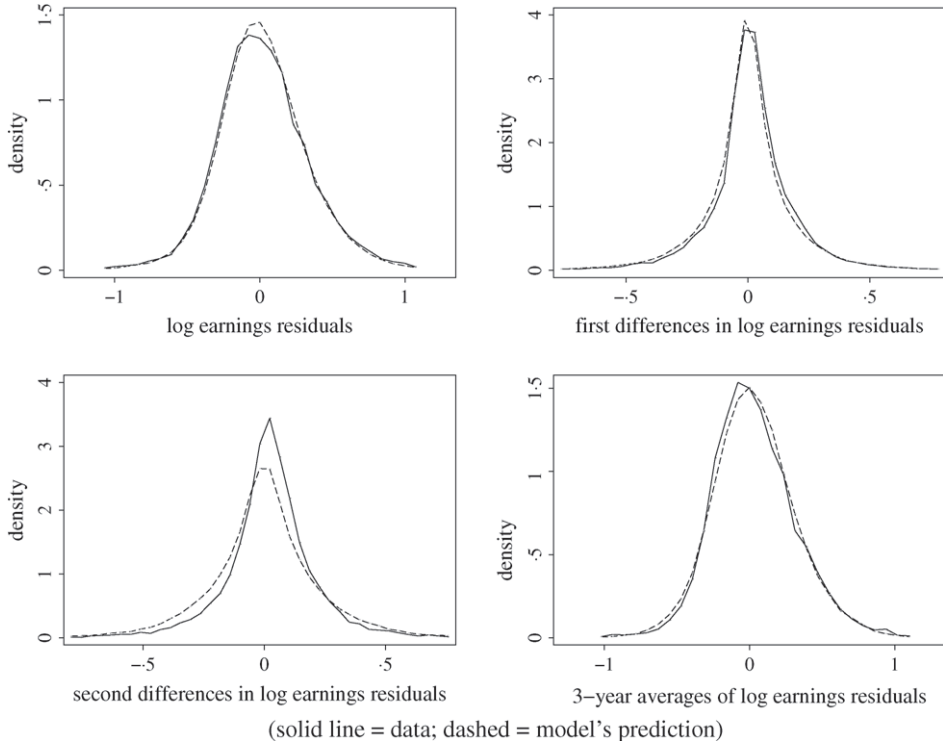


FIGURE 6
Fit of the marginal distribution of log earnings residuals (subpanel 1990–1992)

TABLE 5
Fit of 1990–1992 transition probabilities across earnings quintiles

	Actual					Predicted				
1990/1991	0.70	0.20	0.07	0.02	0.01	0.76	0.18	0.04	0.01	0.00
	0.21	0.54	0.19	0.04	0.01	0.19	0.56	0.19	0.05	0.01
	0.06	0.22	0.53	0.17	0.02	0.04	0.20	0.53	0.19	0.03
	0.02	0.03	0.18	0.63	0.14	0.01	0.05	0.20	0.57	0.16
	0.01	0.01	0.02	0.14	0.82	0.00	0.01	0.03	0.16	0.79
1990/1992	0.67	0.23	0.08	0.02	0.01	0.68	0.22	0.07	0.03	0.01
	0.23	0.49	0.22	0.04	0.01	0.22	0.46	0.22	0.08	0.02
	0.07	0.23	0.50	0.18	0.03	0.07	0.22	0.43	0.22	0.06
	0.02	0.04	0.19	0.59	0.16	0.02	0.08	0.23	0.47	0.20
	0.01	0.01	0.02	0.16	0.80	0.01	0.02	0.05	0.20	0.72

6.2. Transition probabilities in 1990–1992

Next, we consider the transition probabilities across earnings quintiles between t and $t + 1$, and between t and $t + 2$. Actual and predicted probability matrices are displayed in Table 5. The fit is there also quite good, despite a certain tendency to overestimate mobility in the upper part of the distribution.

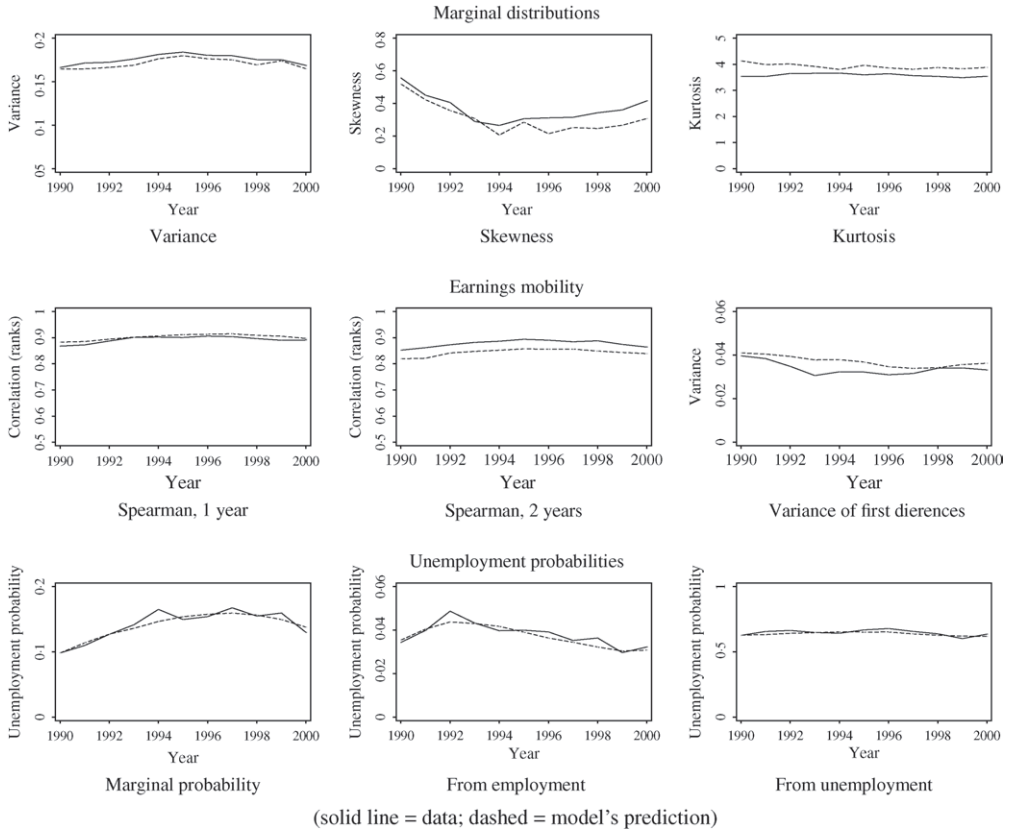


FIGURE 7

Model fit, subpanels 1990–1992 to 2000–2002

6.3. Evolution, 1990–2000

Finally, we look at the capacity of the model to reproduce the observed changes in the log earnings distribution, earnings dynamics, and unemployment risk across subpanels, from 1990–1992 to 2000–2002. The top panels of Figure 7 show how the model fits the variance, the skewness, and the kurtosis of log earnings. The middle panels compare Spearman's ρ for actual and simulated log earnings dynamics over one and two years, and the variance of first-differences of log earnings levels. The lower panels plot unemployment probabilities in the first year, and transition probabilities from employment and from unemployment. Again, the overall fit is quite satisfactory, although the central graph shows that the model underpredicts Spearman's ρ two years apart. It is likely that the model predicts too much mobility because of the first-order Markov assumption. It will be important to keep in mind this caveat, due to the very short time length of the French LFS, when interpreting longer-run inequality results in the next section.

7. LONGER-RUN INEQUALITY

With a fully parametric model in hand, we can now simulate individual earnings trajectories. Specifically, we assign to every individual in the survey the parameters of the subpanel he belongs to. We then draw a value for the unobserved heterogeneity component η_i conditional on

observations, using the posterior distribution of latent variables that the EM algorithm delivers. Next, given η_i and given the first three employment/earnings observations at $t, t + 1, t + 2$ we simulate employment/earnings trajectories after $t + 2$ until retirement at age 65. We simulate transitory earnings dynamics using the parametric copula as explained at the end of Appendix B. Lastly, we impute a replacement income to unemployed individuals equal to 60% of the last earnings.¹⁹ For each individual who is unemployed in the first year, we draw his “last earnings” from the equilibrium (marginal) earnings distribution.

For a given H , we then compute annuitized present values of finite sequences of H future income as

$$Y_{itH}^P = \frac{Y_{it} + \beta Y_{i,t+1} + \dots + \beta^{H_{it}-1} Y_{i,t+H_{it}-1}}{1 + \beta + \dots + \beta^{H_{it}-1}},$$

where Y_{it} denotes year- t income (earnings or unemployment replacement income), $H_{it} = \min\{H, 65 - \text{Age}_{it}\}$ is the minimum of H and the remaining time before retirement, and $\beta = 0.95$. Computing annuities is important in order to compare the present values of income sequences of different lengths.²⁰ When the horizon H is less than the subpanel length, Y_{itH}^P is a sample average.

Our approach extends the classical way of measuring permanent income to short panels by simulating income trajectories beyond the observation period. Contrary to most microsimulation exercises we predict unobserved heterogeneity *conditional* on observed earnings/employment sequences, and this requires a fully parametric model. However, as the short length of the French LFS forces us to restrict transitory dynamics to be first-order Markov, we expect simulations to be less accurate for higher horizons because of possible specification errors. To allow for richer individual dynamics, longer panels are required, together with a methodology that allows for structural change within the panel time frame.

Table 6 displays the variances of log PVs, $y_{itH}^P = \ln Y_{itH}^P$, together with other inequality indices (Gini index and 90/10 percentile ratio), for horizons $H = 1, 5, 10, \infty$ years. In the remainder of this section, we comment on these statistics, displaying them in graphical form to make interpretation easier.

7.1. The contribution of unemployment to income inequality

We start by studying the impact of unemployment risk on income inequality. In Figure 8, we compare the variance of y_{itH}^P computed in two samples: the sample of workers employed in period t “employees”) and the whole sample of both employed and unemployed workers in period t (“whole sample”).

We expect workers employed in year t to face unemployment risk at future dates as all other workers. But, as unemployment has long-lasting consequences, unemployed workers should have lower income present values. In addition, unobserved heterogeneity determines unemployment risk. Hence, the sample of employees in a given year is a selected sample as far as unobservable (permanent) characteristics are concerned. These two effects together explain why there is more current and longer-run income inequality in the whole sample than in the sample of employees.

In cross-section ($H = 1$), we find that the variance of employees’ log earnings is one third less than the log income variance in the whole sample. When the horizon increases, the inequality differential between both samples is reduced but never completely disappears (about 15% for

19. The average replacement ratio in France over the period is 60%, see Martin (1996). Note that we neglect several important features, such as heterogeneity in the replacement ratio, non-stationary UI schemes and specific disutility of unemployment.

20. In the rest of the paper, present values are always annuitized and we keep using the same shorthand PV.

TABLE 6

Longer-run inequality for various horizons, 1990–2000 (replacement ratio = 60%, discount rate = 5%)

Year	Whole sample				Employees only			
	1-year	5-year	10-year	Lifetime	1-year	5-year	10-year	Lifetime
<i>Variance of log</i>								
1990	0.2449	0.2012	0.1858	0.1753	0.1708	0.1594	0.1539	0.1512
1991	0.2435	0.2036	0.1869	0.1765	0.1728	0.1626	0.1569	0.1544
1992	0.2494	0.2064	0.1902	0.1791	0.1718	0.1622	0.1576	0.1552
1993	0.2621	0.2170	0.1991	0.1864	0.1792	0.1717	0.1670	0.1647
1994	0.2758	0.2259	0.2072	0.1943	0.1830	0.1745	0.1705	0.1694
1995	0.2720	0.2276	0.2085	0.1958	0.1849	0.1778	0.1717	0.1694
1996	0.2729	0.2258	0.2054	0.1913	0.1856	0.1758	0.1703	0.1677
1997	0.2748	0.2249	0.2048	0.1907	0.1858	0.1750	0.1690	0.1661
1998	0.2647	0.2180	0.1995	0.1877	0.1785	0.1702	0.1642	0.1622
1999	0.2659	0.2151	0.1954	0.1830	0.1778	0.1663	0.1600	0.1579
2000	0.2511	0.2060	0.1886	0.1784	0.1778	0.1655	0.1596	0.1575
<i>Gini</i>								
1990	0.2689	0.2490	0.2416	0.2367	0.2409	0.2317	0.2275	0.2255
1991	0.2675	0.2499	0.2421	0.2374	0.2410	0.2332	0.2290	0.2273
1992	0.2686	0.2501	0.2429	0.2380	0.2390	0.2317	0.2285	0.2270
1993	0.2740	0.2558	0.2485	0.2433	0.2419	0.2369	0.2345	0.2333
1994	0.2792	0.2598	0.2526	0.2476	0.2435	0.2387	0.2368	0.2365
1995	0.2774	0.2603	0.2522	0.2470	0.2440	0.2400	0.2365	0.2352
1996	0.2796	0.2599	0.2514	0.2452	0.2453	0.2389	0.2358	0.2341
1997	0.2803	0.2594	0.2506	0.2444	0.2453	0.2388	0.2350	0.2332
1998	0.2755	0.2557	0.2472	0.2421	0.2415	0.2356	0.2317	0.2306
1999	0.2757	0.2538	0.2448	0.2389	0.2410	0.2335	0.2292	0.2274
2000	0.2708	0.2506	0.2425	0.2373	0.2424	0.2339	0.2298	0.2277
<i>Percentile ratio, P90/P10</i>								
1990	3.323	2.954	2.836	2.782	2.826	2.714	2.638	2.633
1991	3.253	2.963	2.857	2.789	2.802	2.714	2.664	2.652
1992	3.459	2.994	2.893	2.843	2.799	2.708	2.684	2.687
1993	3.694	3.104	2.950	2.879	2.831	2.784	2.738	2.728
1994	3.905	3.173	3.012	2.950	2.916	2.797	2.782	2.779
1995	3.820	3.183	3.041	2.966	2.884	2.828	2.784	2.792
1996	3.833	3.203	3.022	2.940	2.834	2.787	2.749	2.770
1997	3.894	3.180	3.019	2.955	2.788	2.804	2.767	2.773
1998	3.845	3.116	2.954	2.902	2.729	2.766	2.722	2.736
1999	3.839	3.084	2.920	2.872	2.729	2.766	2.722	2.736
2000	3.482	3.022	2.880	2.858	2.855	2.745	2.689	2.710

lifetime earnings). The memory of the initial inequality does not vanish as the horizon increases, despite the stationarity assumed in simulating trajectories.

The figure also displays the evolution of the log PV variance differential of employees vs. all workers (employed and unemployed). It decreases at the beginning of the period, from 0.70 in 1990 to 0.66 in 1994. Thus, income inequality increases more than earnings inequality following the 1993 recession, mirroring the increase in the unemployment rate. This business-cycle effect vanishes in the long run.

7.2. The structure of longer-run income inequality

In this section we decompose the log PV variance into four components. The first one is the *deterministic* contribution of differences in education and experience across individuals. It is calculated as the *between-group* variance of y_{itH}^P across education and experience cells. The second one, called *permanent*, captures unobserved heterogeneity differences (η_i). We compute it as the within-group variance—by education and experience—of y_{itH}^P simulated with transitory shocks

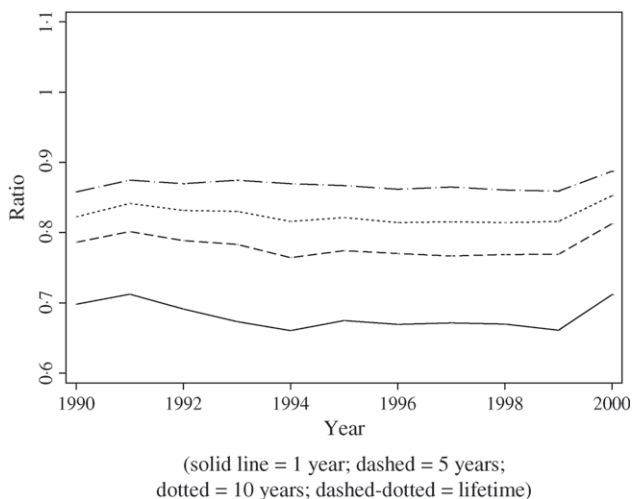


FIGURE 8

Variance of log PVs of employees' earnings as a proportion of the variance of log PVs of workers' income in the whole sample (replacement ratio = 60% and discount rate = 5%)

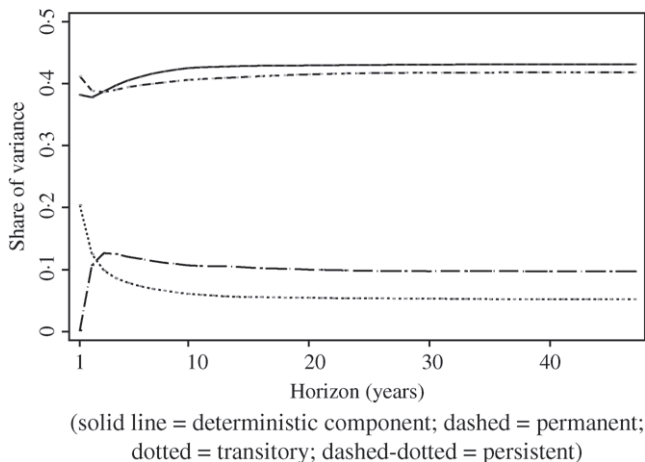


FIGURE 9

Decomposition of log PV variance as a function of the horizon in 1990 (replacement ratio of 60% and discount rate of 5%)

set to 0 in order to cancel any source of persistence other than η_i . The third and fourth components measure the contribution of transitory shocks. Because transitory shocks are persistent, we decompose their contribution as follows. A first transitory component (simply called *transitory*) is calculated as the within-group variance—by education, experience, and unobserved heterogeneity—of y_{itH}^P simulated with i.i.d. transitory shocks, that is, setting the copula parameter to 0. A *persistent* component is lastly computed as the residual variance.

Figure 9 shows the results for the year 1990. The deterministic and permanent components both explain approximately 40% of the total variance of y_{itH}^P for all H . Transitory shocks contribute as follows. Initially, in cross-section, the transitory component accounts for 20% of the variance. When the horizon increases its share rapidly decreases to 8% after five years and 5%

after 20 years. In contrast, the share of the persistent component rises to 13% after 3 years, and then moderately decreases to 10%. The total contribution of transitory shocks to lifetime income inequality slightly decreases with the horizon and accounts for 15–20% of the total variance of lifetime income PVs.²¹

Hence, the structure of longer-run earnings inequality remains very much constant after five years. This is an interesting result, which shows that the use of five-year sequences goes a long way towards capturing the distribution of lifetime PVs. Note, however, that the level of inequality decreases steadily with the time horizon. Table 6 shows that the variance of log PVs computed over five years is 82% of its cross-section value (0.2012 vs. 0.2449), while it decreases to 76% over 10 years (0.1858) and 72% for lifetime PVs (0.1753).

7.3. Evolution, 1990–2000

In this section we document the evolution of longer-run income inequality over the 1990's. Panel (a) of Figure 10 shows the evolution of the variance of y_{itH}^P in the sample of employees and the whole sample, separately.

Longer-run inequality follows a similar hump-shaped pattern as cross-sectional earnings inequality. However, the amplitude is significantly larger. For example, the variance of log PV of lifetime income ($H = \infty$) in the whole population of both employed and unemployed workers grows from 175 in 1990 to 0.196 in 1995—a 12% increase—and then returns to 0.178 in 2000. For one-year income, the increase between 1990 and 1995 is 11%.

Panel (b) of Figure 10 displays the evolution of the variance of y_{itH}^P in proportion to the variance of y_{it1}^P . As more mobility makes individuals exchange position more frequently, this ratio is an index of immobility, and its evolution measures the changes in the equalizing force of mobility over the decade (see Shorrocks, 1978; Fields, 2005). Two remarks are in order. First, according to this index, there is much less mobility in the sample of employees than in the whole sample. In the whole sample, the ratio of five-year and lifetime income inequality to the cross-sectional variance ranges around 82% and 72%, respectively. In the sample of employees, the immobility index is always close to 90%. The differences in the levels reflect the greater homogeneity of the employees' sample. The fact that the horizon matters less for the subsample of employees is due to unemployment being a transitory state.

Second, and importantly, the equalizing force of mobility remains remarkably constant over the decade. Indeed, in the whole sample the ratio of lifetime to cross-sectional income inequality varies between 72% (in 1991) and 69% (in 1999). This near constancy is all the more noticeable as all inequality indices follow a marked hump-shaped pattern.²² These results imply that cross-sectional income inequality is already quite informative of the evolution of longer-run income inequality, provided that unemployed workers are included in the base sample with lower imputed replacement income.

8. MODEL COMPARISON EXERCISES

In this section, we perform two model checks: we test the sensitivity of the previous results to unemployment risk, and we measure the consequences of non-Gaussianity and non-linearity in the process of transitory shocks.²³

21. Geweke and Keane (2000, table 11), using the PSID, regress the PVs of lifetime earnings on observables and unobserved individual effects. They find that observable account for 20–35% of the variance of PVs, unobserved individual effects account for 35–45%, and between 25% and 35% of the variance is left unexplained.

22. The Gini index gives a similar picture. However, being less sensitive to the lower tail of the earnings distribution, the effect of unemployment is less pronounced.

23. We also evaluated the effect of neglecting unobserved heterogeneity on longer-run inequality. We found that both the level and the persistence of inequality are then strongly understated.

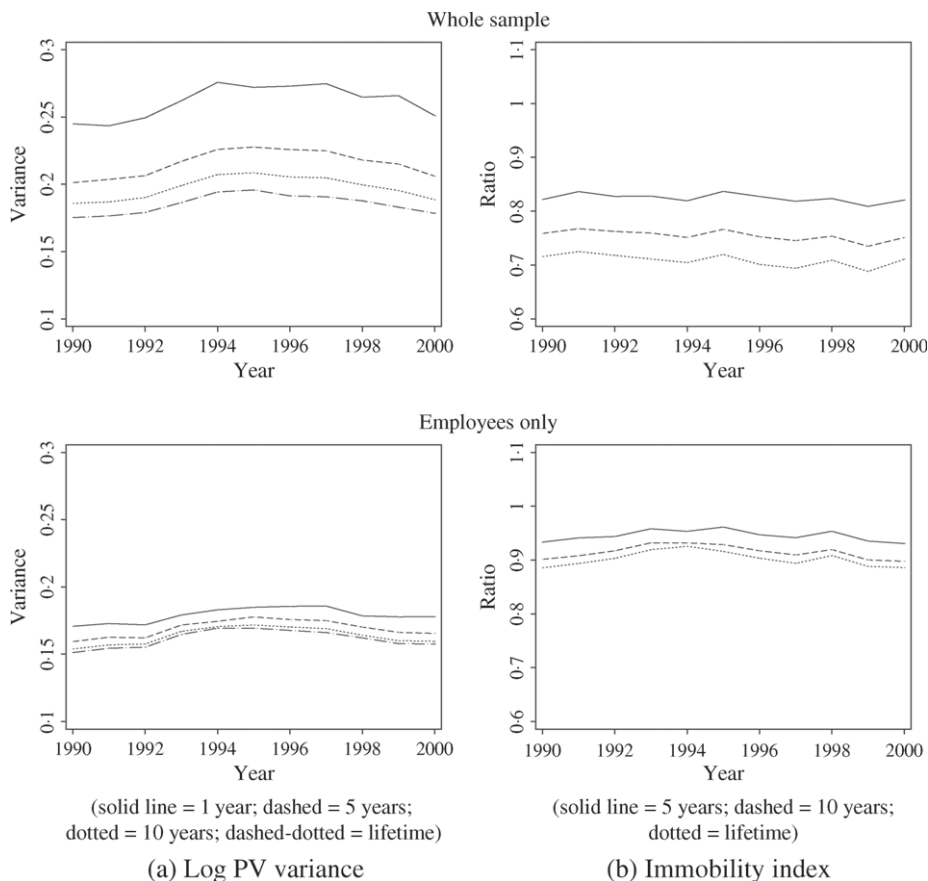


FIGURE 10
Longer-run income inequality (replacement ratio = 60% and discount rate = 5%)

8.1. *Varying unemployment risk*

We first study the sensitivity to unemployment insurance by varying the replacement ratio of UI benefits between 40% and 80%. Given the UI legislation in France, these percentages can be seen as conservative lower and upper bounds for unemployment compensation. Figure 11 shows that lowering the replacement ratio from 80% to 40% has important effects on longer-run income inequality. Inequality rises by about 25% (lifetime) or 60% (one year). The depressing effect of the 1993–1995 recession is also more pronounced when the replacement ratio is lower, as unemployment risk increases in 1993. Finally, the equalizing force of mobility is stronger, the immobility index decreasing from 75% to 60% when the replacement ratio decreases from 80% to 40%. This is because employment spells last on average much longer than unemployment spells, making unemployment shocks to income intense but transitory.²⁴

Second, we study the consequence of suppressing unemployment risk altogether. The results of this exercise are displayed in Figure 12. Lifetime earnings inequality increases by 11% from 1990 to 1995, a close match to the 12% increase generated by the actual parameters. So, cancelling unemployment risk has small effects on the evolution of the equalizing force of

24. Note that in the case where the replacement ratio is 40% the immobility index varies slightly more over the business cycle, with a low in 1994 when the unemployment rate is highest.

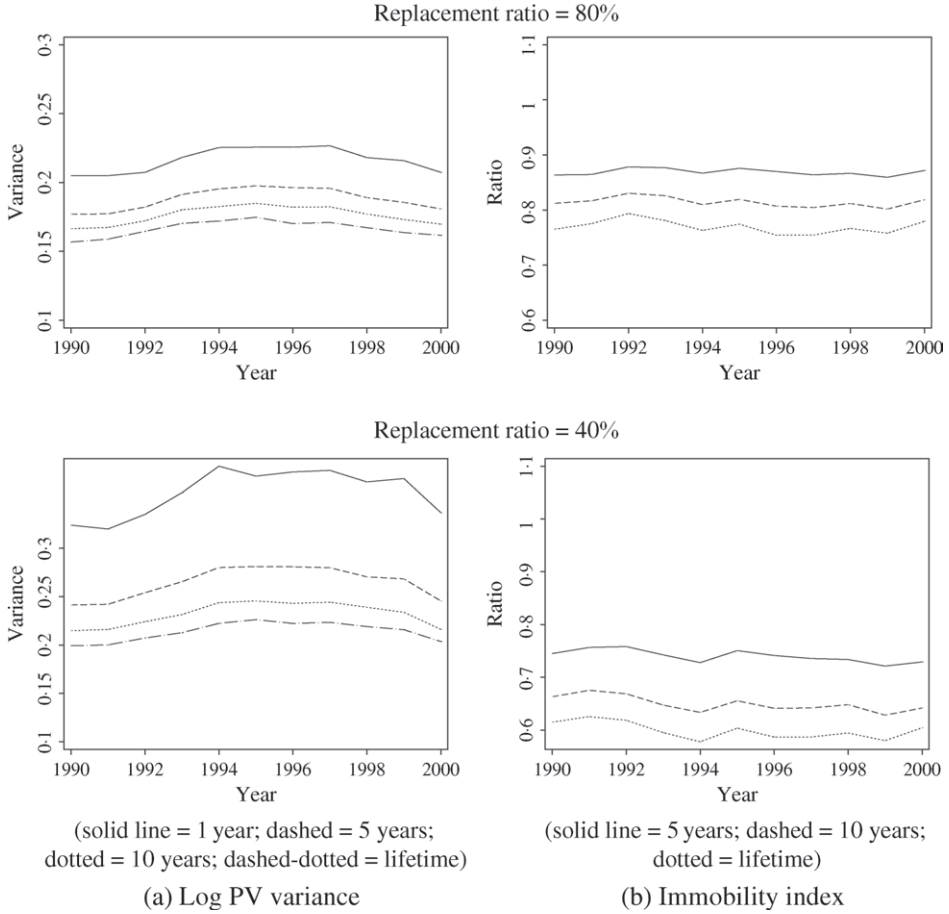


FIGURE 11
Longer-run income inequality for replacement ratios of 40% and 80% (whole sample)

mobility. However, we see that the level of inequality is now noticeably smaller (*e.g.* 0.155 vs. 0.175 in 1990), and that lifetime earnings inequality is more persistent (index of immobility of about 80% instead of 72%).

8.2. *Gaussian transitory shocks and copula*

Most earnings models assume linear dynamics and Gaussian innovations. In our model, the transitory process (ϵ_{it}) is AR(1) if margins and copula are all Gaussian. We already established that the distribution of the permanent component η_i is approximately normal, but that neither the margins of (ϵ_{it}), nor the copula, are Gaussian. We now study the effect on longer-run inequality of estimating and simulating a fully Gaussian model.²⁵

Table 7 shows the parameter estimates. Compared with Table 3, we see that the Gaussian model yields a very different decomposition of log earnings into deterministic, permanent, and

25. With Gaussian margins, the parameter of the Gaussian copula is also the autoregressive parameter of the AR(1) model. We model it as $\tau_j(x_{it}) = \exp(\gamma_j x_{it}) - 1$.

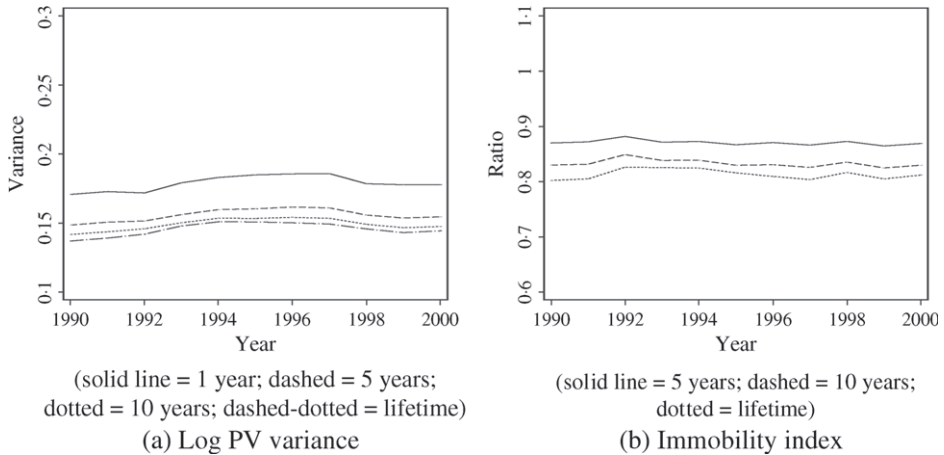


FIGURE 12

Longer-run income inequality with no unemployment risk (whole sample, replacement ratio = 60% and discount rate = 5%)

TABLE 7

Parameter estimates for subpanel 1990–1992, model with Gaussian margins and Gaussian copula

	Log earnings			Unemployment	
	Mean (β, σ)	Variance (α)	Mobility (γ)	Initial (δ_0, ζ_0)	Transition (δ, ρ, ζ_1)
Expe	0.03369 (0.00112)	0.003746 (0.0336)	0.02598 (0.00186)	-0.07973 (0.00302)	-0.03773 (0.00518)
(100×) expe^2	-0.05071 (0.00237)	0.04423 (0.0671)	-0.03307 (0.00351)	0.1566 (0.00649)	0.07755 (0.0106)
Educ II	0.1607 (0.00807)	0.2389 (0.391)	0.1633 (0.0165)	-0.4507 (0.0226)	-0.1889 (0.0336)
Educ III	0.4378 (0.0158)	1.182 (0.375)	0.4283 (0.0163)	-0.5630 (0.0320)	-0.3057 (0.0497)
Educ IV	0.5624 (0.0137)	0.5444 (0.559)	0.2997 (0.0221)	-0.9377 (0.0534)	-0.4021 (0.0748)
Educ V	0.8976 (0.0134)	1.447 (0.394)	0.4545 (0.0172)	-0.9491 (0.0521)	-0.5345 (0.0816)
η_i	0.2965 (0.00342)	-	-	-0.1025 (0.0106)	-0.07642 (0.0157)
$e_{i,t-1}$	-	-	-	-	20.033 (0.0357)
Constant	8.215 (0.0130)	-4.453 (0.507)	-0.4010 (0.0258)	-0.1961 (0.0315)	-1.283 (0.0594)

transitory components. Indeed, the variance of the permanent component is $\sigma_j^2 = 0.2965^2 = 0.088$, compared to $0.2304^2 = 0.053$, that is two thirds more. In the Gaussian model, the unobserved heterogeneity component thus accounts for 50% of the variance of log earnings, compared to 30% in the non-Gaussian model. As a consequence, transitory shocks have a smaller variance and are much less persistent. Moreover, the Gaussian model predicts *more* state dependence in employment (2.03 vs. 1.74 for the autoregressive coefficient in unemployment), but *less* dependence on unobserved heterogeneity (compare the seventh row in the two tables). We checked that the Gaussian copula, rather than the Gaussian margins, is mostly responsible for the observed differences. Hence, the choice of the parametric copula used to describe dynamic tail dependence does have important consequences on the estimation of the factor loadings.

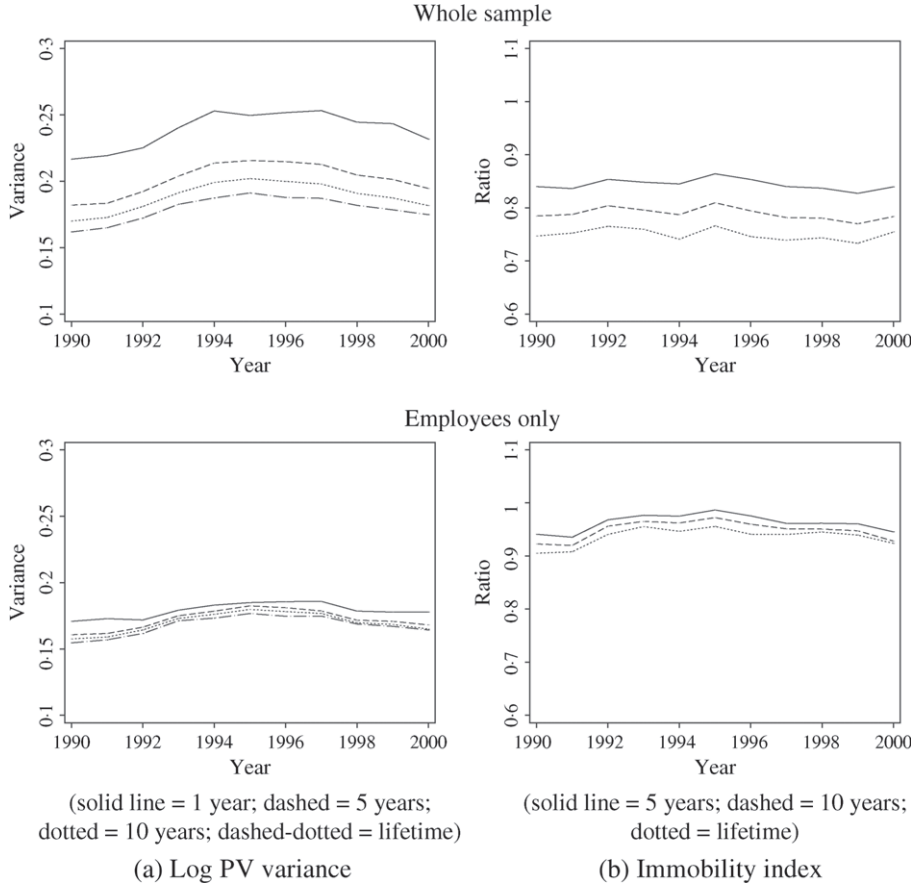


FIGURE 13

Counterfactual longer-run income inequality under full Gaussianity (replacement ratio = 60%, and discount rate = 5%)

Figure 13 shows the effect on longer-run inequality. On panel (a), we see that the Gaussian AR(1) model predicts about 12% less inequality in cross-section. This is due to the fact that unobserved heterogeneity determines unemployment less than in the non-Gaussian model. The difference in terms of lifetime inequality is smaller, as the Gaussian model predicts about 7% less lifetime inequality in the whole sample, and 2% more in the sample of employees. The Gaussian model predicts an immobility index that is about five percentage points higher in the whole sample. For employees, the ratio is close to 90% in both simulations. The evolutions of inequality and immobility indices are also nearly identical. It is quite remarkable that two models with such different decompositions of the log earnings variances yield so similar lifetime inequality patterns.

9. CONCLUSION

In this paper, we study the evolution of cross-sectional and longer-run measures of inequality in France in the 1990's, a period characterized by significant business-cycle fluctuations. For this purpose, we use the French LFS. In order to fit this type of data, we construct a model that combines a flexible specification of the marginal earnings distributions (adapted to the large

cross-sectional dimension) with a tight parameterization of the dependence structure (that the small number of recording periods requires).

The model's structure is standard, with an individual effect and stationary transitory shocks, and we allow parameters to change with the date of entry of individuals into the panel. We simulate individual trajectories beyond the observation period by drawing from the conditional distribution given observations. The ratio of the inequality of long-run averages of earnings to the inequality in a cross-section is an aggregate measure of the persistence of inequality. Thus, our approach adapts an empirical methodology that previously required long panels to short panels like labour force surveys.

The representation of log earnings as the convolution of several factors is standard in the literature. The necessity of allowing for structural change (i.e. time-varying factor loadings) is now recognized of utter importance. A few recent papers also point at non-linearities in the process of transitory shocks. Our model has all these characteristics while still being simple and interpretable.

We find that the distribution of the unobserved heterogeneity component is approximately Gaussian and the distribution of transitory shocks is leptokurtic. Relative mobility, as measured by the joint distribution of the ranks of two consecutive transitory shocks (*i.e.* the copula), is also non-Gaussian, and best approximated by Plackett's copula. Unemployment risk and unemployment insurance are found to be an important source of permanent inequality. Despite significant business-cycle fluctuations in earnings inequality, earnings mobility, and unemployment risk in the 1990's, the measure of the persistence of inequality (the immobility index) is remarkably stable.

Moreover, a model comparison exercise shows that the parametric specification chosen for the copula has important consequences on the estimation of factor loadings. A Gaussian copula attributes to unobserved heterogeneity a greater share of the total log earnings variance. As, at the same time, the unemployment process depends less on unobserved heterogeneity, the Gaussian-copula model yields a very similar picture in terms of longer-run inequality. If, as our discussion of identification suggests, the copula is non-parametrically identified, in the future it will be interesting to push the analysis further and estimate a model with a flexible specification of the marginal distributions of fixed effects and transitory shocks and the copula.

It will be also interesting to test the model on longer panels. The basic structure of the model could be extended for that purpose. With four or five observation periods per individual, it should be possible to identify and estimate a model with second-order Markov transitory dynamics, or with an additional measurement error. Another interesting extension is to allow for an additional individual factor governing the unemployment process specifically. The estimation algorithm performs well and could easily be modified to incorporate these extensions.

APPENDIX A

A.1. Copulas: an economic model

The main structure of our model is a single factor model with first-order Markov errors. We model individual transitory dynamics using copulas. In Section 2, we justified this choice by the ability of the copula representation to tightly parameterize the dependence structure while being flexible as far as marginal distributions are concerned. In this section of the appendix, we argue that modelling the law of individual earnings processes using copulas also arises naturally in steady-state equilibrium models.

The prototypical steady-state search model describes an economy where a population of heterogeneous firms post different wages, and where a population of homogeneous workers sequentially search for a job both when they are unemployed and when they are employed. The wage offer distribution is some function $F(w)$ that depends on the distribution of productivity across different occupations and the search friction parameters. One can allow for heterogeneity in worker ability by assuming that the labour market is segmented (see, for example, Van den Berg and Ridder, 1998).

Search frictions are modelled as follows. Time is discrete. At the end of each period, an employee can be laid off with probability δ or may draw an alternative earnings offer with probability λ . This alternative offer is a draw w' from the equilibrium distribution F . Employees accept alternative offers w' strictly greater than the current wage w . In steady state, the cross-sectional earnings distribution is related to the wage offer distribution by the one-to-one relationship:

$$G(w) = \frac{F(w)}{1 + \kappa[1 - F(w)]} \Leftrightarrow F(w) = \frac{(1 + \kappa)G(w)}{1 + \kappa G(w)}, \quad (\text{A.1})$$

where $\kappa = \lambda/\delta$.²⁶

Conditional on being employed at time t and $t + 1$ (alternative offers thus accrue with conditional probability $\frac{\lambda}{1-\delta}$), individual wage dynamics follows a first-order Markov process such that

$$\begin{aligned} \Pr\{w_{t+1} \leq w' \mid w_t = w\} &= \left(1 - \frac{\lambda}{1-\delta} + \frac{\lambda}{1-\delta}F(w')\right) \mathbf{1}\{w' \geq w\} \\ &= \frac{1}{1-\delta} \left[1 - \frac{\delta + \lambda}{1 + \kappa G(w')}\right] \mathbf{1}\{w' \geq w\}, \end{aligned}$$

where $\mathbf{1}\{w' \geq w\} = 1$ if $w' \geq w$ and 0 otherwise. Hence

$$\begin{aligned} \Pr\{w_{t+1} \leq w', w_t \leq w\} &= \frac{1}{1-\delta} \left[1 - \frac{\delta + \lambda}{1 + \kappa G(w')}\right] (G(w)\mathbf{1}\{w' \geq w\} + G(w')\mathbf{1}\{w' < w\}) \\ &= \frac{1}{1-\delta} \left[1 - \frac{\delta + \lambda}{1 + \kappa G(w')}\right] \min(G(w), G(w')). \end{aligned}$$

The copula thus follows as

$$C(u, v) = \frac{1}{1-\delta} \left[1 - \frac{\delta + \lambda}{1 + \kappa v}\right] \min(u, v). \quad (\text{A.2})$$

Hence, the steady-state search-wage-posting model naturally delivers a simple formula for the copula, which only depends on the friction parameters δ and λ and not on the equilibrium wage distribution F . We do not use this specification because it would not fit earnings mobility data well (as wage cuts are impossible). Yet, we want to put forward the interpretation that a steady-state labour market can be characterized, first, by the equilibrium wage distribution G (*i.e.* the marginal distribution of employees' earnings), and, second, by a description of the way workers exchange positions (via mobility rate parameters embodied in the copula C).

Now, the economy is clearly not in steady state. Structural parameters like G , δ , and λ do fluctuate over time. However, there is some evidence that steady-state flow conditions like (A.1) or the classical equality between the unemployment rate and $\delta/(\delta + \lambda_0)$, where λ_0 is the exit rate from unemployment, are empirically well verified (see Postel-Vinay and Robin, 2006; Jolivet, Postel-Vinay and Robin, 2006). This happens because net annual flows are small in relation to gross flows. Over a limited period of time, macro trends can thus be neglected, and it seems that workers only exchange positions. This is how we justify our assumption that each subpanel S_j approximately reflects a steady-state economy with a specific set of parameters.

APPENDIX B

B.1. The Plackett copula

Plackett (1965) generalizes the independence condition for contingency tables. He shows that, if U and V are uniform random variables on $[0, 1]$, then the following equation:

$$\frac{P(U \leq u, V \leq v)P(U > u, V > v)}{P(U \leq u, V > v)P(U > u, V \leq v)} = \tau + 1 \quad \forall (u, v), \quad (\text{B.1})$$

where $\tau > -1$ is a given constant, has one single solution. This solution is a copula, and writes:

$$C(u, v; \tau) = \frac{1}{2} \tau^{-1} \{1 + \tau(u + v) - [(1 + \tau(u + v))^2 - 4\tau(\tau + 1)uv]^{1/2}\}.$$

26. See Burdett and Mortensen (1998). $\delta + \lambda[1 - F(w)]$ is the exit rate from the stock of employees paid less than w , which is itself proportional to $G(w)$. The inflow is itself proportional to $F(w)$.

Equation (B.1) shows that τ is a natural mobility index. More precisely, let us define the following ordering \succsim_c on copulas, called the concordance ordering (e.g. Joe, 1997):

$$C_1 \succsim_c C_2 \text{ iff } C_1(u, v) \leq C_2(u, v), \quad \forall (u, v).$$

\succsim_c is the first-order stochastic dominance ordering. It measures relative mobility: the ranks process governed by copula C_1 will be said more mobile than the ranks process governed by C_2 if $C_1 \succsim_c C_2$. Moreover, the concordance ordering possesses a lower and an upper bound (Fréchet, 1935). The lower bound C_L satisfies: $C_L(u, v) = \max(u + v - 1, 0)$. The upper bound C_U satisfies $C_U(u, v) = \min(u, v)$.

The Plackett copula satisfies the following properties (Joe, 1997):

1. $C(\cdot, \cdot; \tau_1) \succsim_c C(\cdot, \cdot; \tau_2)$ for all $\tau_2 > \tau_1$.
2. $C(\cdot, \cdot; \tau) \rightarrow C_L$ when $\tau \rightarrow -1$.
3. $C(\cdot, \cdot; \tau) \rightarrow C_U$ when $\tau \rightarrow \infty$.
4. $C(\cdot, \cdot; \tau) \rightarrow C^\perp$ when $\tau \rightarrow 0$, where $C^\perp(u, v) = uv$ is the independent copula.

Therefore, the Plackett copula is mobility decreasing with respect to its parameter, and the Plackett family covers the whole range of bivariate dependence, from immobility (C_U) to independence (C^\perp) and perfect mobility (C_L).

Simulation. Let u be earnings ranks at time t . For given u , we here show how to simulate earnings ranks at $t + 1$ (v) from the Plackett copula. Note that for $u \in [0, 1]$ given, $\frac{\partial C}{\partial u}(u, v)$ is uniform(0,1). So in order to simulate a v draw a uniform(0,1) variable w and solve for v in $\frac{\partial C}{\partial u}(u, v) = w$. In the case of the Plackett copula, this implicit equation writes as a quadratic polynomial equation with two roots in $[0, 1]$. Choose the highest or the lowest root with probability $\frac{1}{2}$.

APPENDIX C

C.1. Estimation algorithm

Fix K , and a grid η_1, \dots, η_K for the distribution of the permanent component η_i , and fix M the number of Gaussian components for the marginal distribution of transitory shocks ε_{it} .

Let $\mathbf{x}_i = (x_{i1}, \dots, x_{iT})$, $\mathbf{y}_i = (y_{i1}, \dots, y_{iT})$, and $\mathbf{e}_i = (e_{i1}, \dots, e_{iT})$ be the observations for individual i . Let $j(i) \in \{1, \dots, J\}$ be the index of the panel sample these observations belongs to (i.e. $j(i) = j$ such that $i \in S_j$).

The likelihood for one individual observation is the discrete mixture:

$$\ell_j(\mathbf{y}_i, \mathbf{e}_i | \mathbf{x}_i) = \sum_{k=1}^K p_k \ell_j(\mathbf{y}_i, \mathbf{e}_i | \mathbf{x}_i, k), \quad i \in S_j,$$

where

$$\begin{aligned} \ell_j(\mathbf{y}_i, \mathbf{e}_i | \mathbf{x}_i, k) &= P_j^0(e_{i1} | x_{i1}, k) \times \prod_{t=1}^{T-1} P_j(e_{i,t+1} | e_{it}, x_{i,t+1}, k) \times \prod_{t=1}^T \left[\frac{1}{\exp(\alpha_j x_{it})} f_j(\epsilon(y_{it} | x_{it}, k) | x_{it}) \right]^{e_{it}} \\ &\times \prod_{t=1}^{T-1} c[F_j(\epsilon(y_{it} | x_{it}, k) | x_{it}), F_j(\epsilon(y_{i,t+1} | x_{i,t+1}, k)); \exp(\gamma_j x_{it}) - 1]^{e_{it} e_{i,t+1}}, \end{aligned}$$

where c is Plackett's copula density, with parameter $\exp(\gamma_j x_{it}) - 1$, and where

$$\epsilon(y_{it} | x_{it}, k) = \frac{y_{it} - \beta_j x_{it} - \sigma_j \eta_k}{\exp(\alpha_j x_{it})},$$

$$P_j^0(e_{i1} | x_{i1}, k) = \Phi(\delta_{0j} x_{i1} + \zeta_{0j} \eta_k)^{e_{i1}} \Phi(-\delta_{0j} x_{i1} - \zeta_{0j} \eta_k)^{1-e_{i1}},$$

$$P_j(e_{i,t+1} | e_{it}, x_{i,t+1}, k) = \Phi(\rho_j e_{it} + \delta_{1j} x_{i,t+1} + \zeta_{1j} \eta_k)^{e_{i,t+1}} \Phi(-\rho_j e_{it} - \delta_{1j} x_{i,t+1} - \zeta_{1j} \eta_k)^{1-e_{i,t+1}},$$

$$f_j(\varepsilon_{it} | x_{it}) = \sum_{m=1}^M \pi_{mj} f_j(\varepsilon_{it} | x_{it}, m) = F'_j(\varepsilon_{it} | x_{it}),$$

$$f_j(\varepsilon_{it} | x_{it}, m) = \frac{1}{\omega_{mj}} \varphi\left(\frac{\varepsilon_{it} - \mu_{mj}}{\omega_{mj}}\right) = F'_j(\varepsilon_{it} | x_{it}, m).$$

Note that we allow for a specific marginal distribution of transitory shocks ε_{it} to each subpanel j .

E-step. For initial values of the parameters p_k , $(\mu_{mj}, \pi_{mj}, \omega_{mj})$, (δ_{0j}, μ_{0j}) , $(\rho_j, \delta_{1j}, \mu_{1j})$, $(\beta_j, \sigma_j, \alpha_j)$, and γ_j , for each individual in the samples \mathcal{S}_j , $j = 1, \dots, J$, compute the posterior probabilities of the latent types of η_i and ε_{it} :

$$p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) = \frac{p_k \ell_j(\mathbf{y}_i, \mathbf{e}_i | \mathbf{x}_i, k)}{\ell_j(\mathbf{y}_i, \mathbf{e}_i | \mathbf{x}_i)}, \quad k = 1, \dots, K,$$

$$\pi_j(m | y_{it}, x_{it}, k) = \frac{\pi_{mj} f_j(\varepsilon(y_{it} | x_{it}, k) | x_{it}, m)}{f_j(\varepsilon(y_{it} | x_{it}, k) | x_{it})}, \quad m = 1, \dots, M.$$

M-step. With $p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i)$ and $\pi_j(m | \varepsilon_{it}, x_{it}, k)$ set to these values,

- Update p_k by maximizing

$$\sum_{j=1}^J \sum_{i \in \mathcal{S}_j} \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \ln p_k,$$

with respect to p_k and subject to

$$\sum_{k=1}^K p_k = 1, \quad \sum_{k=1}^K p_k \eta_k = 0, \quad \sum_{k=1}^K p_k \eta_k^2 = 1.$$

Then for each subpanel j perform the following steps:

- Maximize

$$\sum_{i \in \mathcal{S}_j} \sum_{m=1}^M \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \sum_{t/e_{it}=1} \pi_j(m | y_{it}, x_{it}, k) \ln \pi_{mj},$$

with respect to π_{mj} and s.t.

$$\sum_{m=1}^M \pi_{mj} = 1, \quad \sum_{m=1}^M \pi_{mj} \mu_{mj} = 0, \quad \sum_{m=1}^M \pi_{mj} \omega_{mj}^2 = 1.$$

- Maximize

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \ln P_j^0(e_{i1} | x_{i1}, k; \delta_{0j}, \mu_{0j}),$$

with respect to (δ_{0j}, μ_{0j}) , and

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K \sum_{t=1}^{T-1} p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \ln P_j(e_{i,t+1} | e_{it}, x_{i,t+1}, k; \rho_j, \delta_{1j}, \mu_{1j}),$$

with respect to $(\rho_j, \delta_{1j}, \mu_{1j})$.

- Minimize

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) (y_{it} - \beta_j x_{it} - \sigma_j \eta_k)^2,$$

with respect to β_j and σ_j . Then, compute residuals $u(y_{it} | x_{it}, k) = y_{it} - \beta_j x_{it} - \sigma_j \eta_k$ and minimize

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) [u(y_{it} | x_{it}, k)^2 - \exp(2\alpha_j x_{it})]^2,$$

with respect to α_j .

- Compute standardized residuals $\varepsilon(y_{it} | x_{it}, k)$ and maximize

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \sum_{m=1}^M \sum_{t/e_{it}=1} \pi_j(m | y_{it}, x_{it}, k) \ln \left[\frac{1}{\omega_{mj}} \varphi \left(\frac{\varepsilon(y_{it} | x_{it}, k) - \mu_{mj}}{\omega_{mj}} \right) \right],$$

with respect to μ_{mj} and ω_{mj} . The solution can be written as weighted means and variances of the standardized residuals.

- Compute ranks

$$r(y_{it} | x_{it}, k) = F_j(\epsilon(y_{it} | x_{it}, k) | x_{it}),$$

and maximize

$$\sum_{i \in \mathcal{S}_j} \sum_{k=1}^K \sum_{m=1}^M p_j(k | \mathbf{y}_i, \mathbf{e}_i, \mathbf{x}_i) \sum_{t/e_{it}=e_{i,t+1}=1} \ln c[r(y_{it} | x_{it}, k), r(y_{i,t+1} | x_{i,t+1}, k); \exp(\gamma_j x_{it}) - 1]$$

with respect to γ_j .

- Lastly, pooling all subpanels together regress the estimates of j -specific parameters on a constant, j , j^2 , and j^3 . Compute the restricted parameter estimates, and start a new E-step. Iterate until convergence.

A STATA program is available from the authors.

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