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THE ROLE OF WORKERS IN KNOWLEDGE DIFFUSION ACROSS FIRMS

Anders Akerman and Kerstin Holzheu

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The Role of Workers in Knowledge Diffusion Across Firms*

Anders Akerman and Kerstin Holzheu[‡]

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Abstract

With about 1/5th of all jobs changing each year, labor mobility is a potentially significant source for idea exchange in the economy. In this paper, we analyze the effect of labor mobility and innovation on productivity growth in the economy. First, by leveraging administrative data for Sweden, we show suggestive evidence at the macroeconomic level that both the extent and direction of worker mobility correlates with firm productivity. With event-study analysis based on exogenous worker deaths and shift-share international trade shocks, we proceed to verify such relationship at the microeconomic level. Second, we develop a multi-worker framework with random search and on-the-job mobility to estimate the relative size of the contribution of worker mobility and R&D to growth. Estimated on a balanced growth path using the Swedish microeconomic data, we find that around 60% of output growth can be attributed to firm innovation. Intuitively, our results change significantly with the extend of worker mobility and suggest that slowdown of worker mobility can depress aggregate economic growth.

JEL codes: J24, J41, J63, J64

Keywords: Productivity, Worker Mobility

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[‡]Akerman: University of Stavanger (anders.akerman@gmail.com), Holzheu: Sciences Po (CNRS) & IZA (kerstin.holzheu@sciencespo.fr)

1 Introduction

It is widely acknowledged that approximately one-fifth of all jobs in the US economy are either created or destroyed each year (Davis and Haltiwanger, 1992; Leonard, 1986). This worker mobility redistributes not only productive working hours but also workers' knowledge and ideas across various firms and sectors of the economy. Worker mobility differs from firms' internal efforts at idea creation in two main aspects. Unlike research and development (R&D), the benefits of worker knowledge and ideas are not exclusive to the firm beyond the duration of the employment match. Moreover, in contrast to R&D — which tends to be concentrated among a few firms, with a considerable fraction of firms reporting no R&D activities at all (Klette and Kortum, 2004) — labor mobility is pervasive throughout the economy. In fact, all firms are potential beneficiaries of this source of new ideas. Due to these differences, labor mobility and R&D can mutually reinforce each other at the macroeconomic level by potentially transferring novel ideas from R&D-intensive firms to non-R&D firms. While R&D and worker mobility may act as substitutes within individual firms, they complement each other at the aggregate level of the economy. Consequently, worker mobility has the potential to amplify economic growth.

In this paper, we quantify the role of workers in driving economic growth in the economy. We make two main contributions. First, we provide empirical evidence of the effect of scope and direction of worker mobility on firm productivity, leveraging highly granular register data for Sweden on firms, products and workers. We both consider horizontal productivity changes such as increases in output per worker as well as vertical productivity changes such as adoption of new products. We conduct our analysis both at the aggregate, sectoral level as well as at the individual firm level. Our data's granularity allows us to consider arguably exogenous shifters to tease out the effect of worker mobility. Second, we develop a theoretical framework that enables us to disentangle the contributions to economic growth arising from labor mobility and firm-generated innovation. Specifically, we construct a novel multi-worker firm environment with on-the-job search. This framework is distinctive in its allowance for the interplay of heterogeneous worker and firm productivity while remaining sufficiently parsimonious to ensure the tractability of the model. We show that in our model, we can separate the effect of firm size and productivity on joint firm surplus, allowing us to define a parsimonious balanced growth path with closed-form solution. To discipline the model quantitatively, we draw on comprehensive data from the Swedish manufacturing sector, where innovation has a more pronounced influence compared to other economic sectors. Our findings emphasize the central role of worker mobility in driving economic growth. We find that worker mobility accounts for about 60% of aggregate growth in the manufacturing sector. Intuitively,

our results vary significantly with the prevalence of on-the-job search. In a split-sample analysis of the last two decades, we find that the contribution of worker mobility has slightly decreased, coinciding with a reduction in worker mobility and an increase in R&D intensity.

Our findings support the idea that worker mobility as well as R&D are both significant forces in driving aggregate productivity growth. In our empirical work, we find suggestive evidence that sectors with more worker mobility and those who tend to hire more often from more productive firms see higher aggregate productivity growth. We also analyze the relative strength of the correlation of worker mobility and R&D intensity on firm productivity, finding that high income occupation mobility is similarly related to productivity growth as R&D intensity. We then leverage quasi-experimental variation to argue for a causal interpretation to our suggestive evidence. Leveraging sudden and unexpected worker departures due to worker death, we estimate a negative effect of worker disappearance on firm productivity and the likelihood of product entry, especially for those workers with relevant previous work experience. We also analyze the effect of arguably exogenous shift-share demand shocks, based on baseline trade patterns, on firm hiring origin and destination. As negative trade shocks reallocate workers from one firm to another, we observe arguably exogenous variation in likely sending firms. We find that it matters which firm is hit by such shocks: if above median productivity firms are exposed to negative demand shocks, local competitors see increases in labor productivity on impact, whereas this is not true when a lower quality firm is hit. These analysis suggest that firm knowledge is not fully embodied in the firm, but also partially in firm-associated workers and hence partially separable from the firm upon worker displacement.

In our theoretical framework, we follow these insights by describing workers as vessels of knowledge. Firms generate new ideas through R&D and transmit these ideas to their workers, thereby assuming the dual role of innovators and knowledge transmitters. In our model, a multi-worker firm environment with constant returns ensures that workers are willing to move to lower productivity firms, as their superior knowledge benefits outside firms with lower productivity more than their previous firms. Through this mechanism, our model captures a significant and quantitatively important aspect of worker mobility, namely downward worker mobility (see, for instance, [Sorkin, 2018](#)). The worker-search setup allows for embedding in a standard balanced growth setting. We demonstrate that there exists a closed-form equation describing growth in the economy and illustrate how it relates to its various drivers. Finally, we leverage our empirical insights on the effect of worker departures and worker arrivals for estimation. In a variance decomposition, we show that our theoretical results on the importance of worker mobility for growth are quantitatively comparable to empirical estimates. Our analysis provides empirical and theoretical support for

the proposition that labor market frictions, by constraining labor mobility, impose substantial economic costs on the broader economy. In the light of decreasing average worker mobility, our analysis suggests a simultaneous decrease in aggregate productivity growth.

The paper relates mainly to three strands of the literature. The first strand has empirically analyzed the effect of workers' mobility and firm outcomes, either by considering special workers within the firm such as engineers broadly defined ([Harrigan et al., 2023](#); [Tambe and Hitt, 2014](#)), CEOs or managers ([Meinen et al., 2022](#); [Bennedsen et al., 2020](#); [Jones and Olken, 2005](#); [Becker and Hvide, 2021](#); [Mion and Opromolla, 2014](#)), inventors ([Jaravel et al., 2018](#); [Almeida and Kogut, 1999](#); [Singh and Agrawal, 2011](#); [Jaffe et al., 1993](#); [Kaiser et al., 2015](#); [Braunerhjelm et al., 2020](#)) or workers more broadly ([Hoey et al., 2023](#); [Stoyanov and Zubanov, 2012](#), [Serafinelli, 2019](#)). Some other studies have used exogenous worker disappearances through death for identification and estimation ([Andersen and Nielsen, 2011](#); [Bertheau et al., 2022](#); [Jäger and Heining, 2019](#); [Bloesch et al., 2022](#); [Sauvagnat and Schivardi, 2023](#)). While existing literature has examined different facets of innovation and worker mobility, our contribution lies in analyzing the direction of worker mobility. To our knowledge, we are the first to utilize sudden and unexpected worker deaths to discern how attributes of past employers influence the productivity of receiving firms. Additionally, we pioneer the exploration of whether a worker's prior experience in the production of a specific product influences the likelihood that the receiving firm will initiate production of the same product. Thus, our study contributes by providing well-identified evidence that underscores the significance of workers in the dissemination of knowledge across firms.

The second strand of the literature has advanced on the theoretical study of either multi-worker firms or models of idea diffusion with balanced growth paths. Our paper is closely related to [Bilal et al., 2022](#), [Engbom, 2023](#), [Audoly, 2023](#) and [Bilal et al., 2021](#), yet introduces worker heterogeneity and allows some simplifications compared to their setups. It shares with [Jarosch et al., 2021](#) the focus on learning in firms, but does not consider wage formation, similar to [Bilal et al., 2022](#). In addition, we use exogenous variations in the data to estimate key model parameters. Thematically, the paper is related to [Lentz and Mortensen, 2022](#), yet does not feature a product quality ladder and focuses on a balanced growth path. The paper also relates to [Lucas and Moll, 2014](#), [Perla and Tonetti, 2014](#), [Kortum, 1997](#), [Luttmer, 2007](#), [Benhabib et al., 2021](#), [Buera and Oberfield, 2020](#), [Koenig et al., 2016](#) and [Hopenhayn et al., 2020](#) through its analysis of a balanced growth path in an economy with knowledge diffusion. While these papers mostly abstract from the mechanism behind idea diffusion, we explicitly bring to the model both internal firm innovation as well as frictional labor mobility and associated idea transmission. In this sense, the paper is close to [Akcigit et al., 2016](#),

who also use micro-data to discipline a model of diffusion of ideas, however in the area of patents. The paper is related to a complementary paper on the role of knowledge diffusion on a balanced growth path with non-compete contracts, [Liu, 2023](#). Differently from this paper, we analyze multi-worker firms. Due to this focus, we can establish closed form expressions for the balanced growth path in all cases, whereas [Liu, 2023](#) can only do so when restricting to a perturbation of equilibrium worker mobility.

The third strand of the literature discusses the relationship between worker reallocation and productivity as mediated through employment protection legislation (EPL) and notably firing costs. In this literature, EPL are found to depress productivity and employment ([Hopenhayn and Rogerson, 1993](#); [Da-Rocha et al., 2019](#); [Bartelsman et al., 2016](#), [Aghion et al., 2023](#)) and productivity growth ([Poschke, 2009](#)) as well as shift the type of innovation in the economy ([Mukoyama and Osotimehin, 2019](#)). As EPL equally depresses labor mobility, this literature predicts a positive relationship between worker reallocation and productivity across countries. Differently from this literature, we discuss a relationship between worker mobility and innovation for a fixed EPL as mediated through worker mobility and imitation.

The paper proceeds as follows. In section [2](#) we outline our data sources and section [3](#) provides empirical results on the importance of worker mobility for firm growth. Motivated by the presented evidence, we describe a theoretical framework and derive a balanced growth path of the economy in section [4](#). In section [5](#) we show results for the decomposition of economic growth in the economy. Section [6](#) concludes.

2 Data

In the following, we outline our data sources in section [2.1](#) and discuss our sample in section [2.2](#).

2.1 Data Sources

We leverage four main data sources: a firm level data set, a worker level dataset, a product-level data set, and the death registry. The set of variables used per dataset, together with the period covered, is summarized in Appendix Table [5](#).

The firm level data derives from the database called *Företagsdatabasen* and includes for example value added, total wage sum and other production costs. The dataset is based on information from the Swedish Tax Authority on administrative registries of the firms' balance

sheets.

The worker-level data is called the *Swedish Longitudinal Integrated Database for Health Insurance and Labour Market Studies (LISA)*. It contains information on all Swedish workers in the private sector and has previously been used by for example [Balke and Lamadon \(2022\)](#) and [Saez et al. \(2019\)](#). It includes information such as income, education, and age. Occupations are reported according to the Swedish Standard Classification of Occupations (SSYK).¹ We can link employers and employees using firm identifiers and therefore track workers' experience based on the firm they work at. The reliability and quality of this data is regarded as very high, since it is based on tax reports by firms and misreporting is punishable by law.

The product-level data is drawn from the dataset *Industrins Varuproduktion (IVP)*, which is based on surveys on the production of Swedish manufacturing firms, and has previously been used by [Carlsson and Skans \(2012\)](#). The dataset includes all firms with at least five employees, and contains information on what products they produce up to the 8-digit Combined Nomenclature (CN) level.² For each year, firms report both quantity and price for each product. Using the worker-level data, this product-level data allows us to track workers' experience in specific lines of production.

We also utilise data from the dataset *Research and Development in the private sector* to obtain data on the expenditure of firms on R&D. We specifically use the overall amount in Swedish kronor that firms spend on R&D. The basic criteria for distinguishing R&D from related activities are that there should be an element of innovation and creativity in the activity. The outcome of the activity should be uncertain, and the uncertainty should also apply to the expenditure of financial and human resources. However, the activity should be planned and budgeted and the outcome should be intended to be potentially transferable and replicable in other activities.

Finally, we also leverage information on worker deaths from the registry *Dödsorsaksregistret* which includes information on date and cause of death as classified through the International Classification of Disease ICD, version 10 (cf. [Brooke et al., 2017](#), for an extensive description of the dataset). In the medical literature, a sudden unexpected death (SUD) is defined “as a natural, unexpected fatal event that occurs within 1 hour of the beginning of symptoms in

¹The base for SSYK is the international standard classification of occupations with reference year 2008 (ISCO-08).

²The CN system is the EU classification scheme for products, and is used by custom offices as well as statistical agencies, similar to the US equivalent Harmonised System (HS).

an apparently healthy subject or in one whose disease was not so severe that such an abrupt outcome could have been predicted” (Lim et al., 2010). We identify unexpected worker deaths using information on the cause of deaths from the registry, building on Andersen and Nielsen (2011). Similar to them, we consider the list of ICD-10 causes of death in Table 1 to identify sudden deaths. Among natural causes of death, we thus consider acute myocardial infarction

ICD Code	Description
Natural Causes	
I22-I23	Acute myocardial infarction
I46	Cardiac arrest
I50	Congestive heart failure
I60-I69	Stroke
R95-R97	Sudden death by unknown cause
Unnatural Causes	
V00-V89	Traffic accidents
V90-99, X00-X59, X86-X90	Other accidents and violence

Table 1: ICD diagnosis of Death: Sudden unexpected death

(ICD-10: I22-I23), cardiac arrest (I46), congestive heart failure (I50), stroke (I60-I69) and sudden deaths by unknown causes (R95-R97). Among unnatural deaths, we consider traffic accidents (V00-V89) and deaths caused by other accidents and violence (V90-V99, X00-X59, and X86-X90) which excludes suicides or violent deaths due to relatives.

2.2 Sample

Our data covers the years 1997–2019. We restrict the population to workers 15–65 years of age with an observed occupation code, and to firms with at least five employees. Table 2 includes summary statistics for our data sample. Our data spans around 1.2 million unique workers working for around 21,500 firms. Workers are on average 43 years old. Around 31% of workers have a college degree and 1% hold a PhD. A worker is likely to leave the current employer with probability 17% each year. Our firm data shows that firms’ labor productivity grows at around 2% per year on average. Moreover, the median firm is fairly small and employs around 12 workers. This means that exits of specific workers are likely to be fairly salient for these firms’ operations. Around 7% of firms adopt a new product every year, and around 2% report positive R&D investments every year. This investment intensity is a small number, especially compared to the 17% of workers changing employment each period, as shown in Panel A. The mean age at death is 52, and is as expected higher than the sample average age. There are 2,200 sudden death events in our matched sample where a firm experiences at least one death, out of the 242,380 firm-year observations in total,

totalling about 1% of all matched observations. This means that death events are relatively rare, but more frequent than for example in the study by [Sauvagnat and Schivardi \(2023\)](#), who look at deaths of Italian CEOs (0.1%) and similar in magnitude to [Bertheau et al. \(2022\)](#) but smaller than [Jäger and Heining \(2019\)](#).³

Table 2: Summary Statistics

	Obs. (1)	Mean (2)	SD. (3)	Median (4)	Min. (5)	Max. (6)
A) Workers						
Age	8,105,124	42.91	11.62	43.00	16.00	64.00
Female	8,105,124	0.24	0.43	0.00	0.00	1.00
Income	8,105,124	3,556.81	2,054.78	3,262.00	1.00	437,802.00
Less than HS	8,105,124	0.69	0.46	1.00	0.00	1.00
More than HS	8,105,124	0.31	0.46	0.00	0.00	1.00
Phd	8,105,124	0.01	0.08	0.00	0.00	1.00
Stayer	7,643,679	0.83	0.37	1.00	0.00	1.00
# Workers	1,168,308					
# Firms	21,508					
# Occ. Groups (4-Digits)	366					
B) Firms						
Y/L Growth Rate	212,932	0.02	0.34	0.03	-8.95	7.71
Firm Size	242,380	50.67	329.63	12.00	5.00	22,610.00
New Product Adoption	72,454	0.07	0.25	0.00	0.00	1.00
R&D dummy	242,380	0.02	0.15	0.00	0.00	1.00
# Firms	25,216					
# Prod. Codes (4-Digits)	236					
B) Deaths						
Age at Death	2,027	50.81	11.68	54.00	18.00	64.00
# Events	2,027					

3 Motivation

In this section, we show in various ways that labor mobility and firm productivity are correlated. Specifically, we show that both for vertical productivity improvements (higher labor productivity) and horizontal productivity improvements (expansion of a firm’s product set), the mobility of workers is correlated with the growth rate in productivity. We perform

³Note that [Jäger and Heining \(2019\)](#) do not observe the cause of death and hence start from a larger sample of disappearing workers. To focus on unexpected deaths, they discard workers who had been on sick leave in the five years prior to the death event.

this exploration both at a sectoral level of analysis (section 3.1) as well as at the firm level (section 3.2).

3.1 Aggregate Evidence

We first explore whether there are correlations between a sector’s mobility patterns and its productivity growth in the data. Specifically, we examine whether both the extent of mobility due to worker-firm separations and the direction of worker mobility, as captured by the change in the average quality of the firm before and after mobility, correlate with aggregate productivity growth at the sector level. We use two proxies for productivity growth: vertical productivity growth computed as the average growth of labor productivity, and horizontal productivity growth as captured through new product adoptions. After considering the correlation of mobility patterns with productivity growth, we examine the size of these effects by comparing them to the correlation of productivity growth with R&D activity.⁴

Extent of mobility First, we compute the mean rate of worker separations at the four-digit sector level. We only include final separations where the worker never returns to the firm. We compute different separation rate averages by skill groups, leveraging occupation and income information for skill classification. Specifically, we rank all occupations according to the annual income of its workers and compute separation rates for the top decile and below median occupation groups separately. This classification mirrors the hypothesis that high income, high skill workers might have a higher knowledge level to impart. Consequently, we adopt a more comprehensive definition of skill than those used in previous studies, such as the focus on technology workers by [Harrigan et al. \(2023\)](#), the emphasis on IT workers by [Tambe and Hitt \(2014\)](#), the analysis of inventors’ mobility by [Jaravel et al. \(2018\)](#), or the studies of entrepreneurs and managers by [Becker and Hvide \(2021\)](#) and [Mion and Opromolla \(2014\)](#), respectively.

In the left panel of Figure 1, we first see a scatter plot across sectors showing the level of labor productivity growth and separation rates. The size of the circles indicate the total value added in each sector. Blue colored circles indicate values for workers in below median wage occupations, and red colored circles pertain to workers in the top decile of occupations. We see that there appears to be a positive correlation between separation rates and productivity growth among the workers with the highest level of embodied knowledge,

⁴Earlier studies have focused on mobility and for example R&D intensities and patent registrations. [Jaffe et al. \(1993\)](#) study geographic spillovers of patent citations, and [Almeida and Kogut \(1999\)](#) study the effects of knowledge localization in the semiconductor industry. [Tambe and Hitt \(2014\)](#) also find that movement of information technology (IT) workers lead to large productivity spillovers.

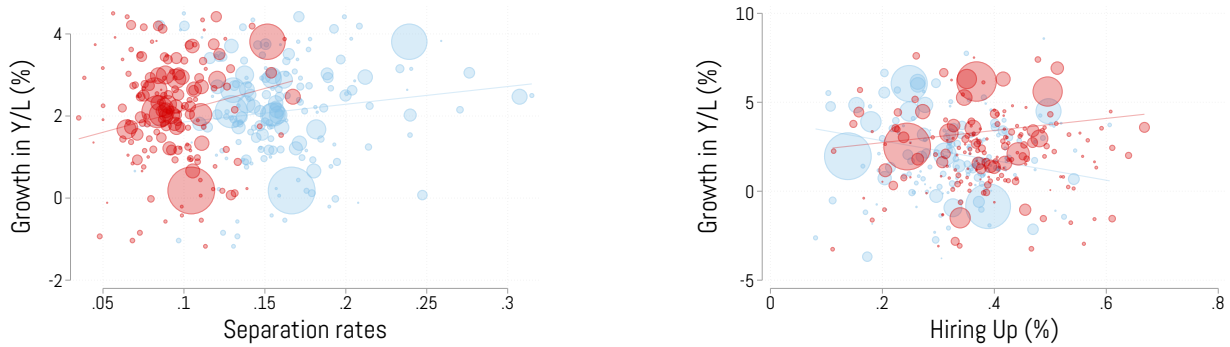
i.e. workers in the highest paid occupations (red color). Interestingly, the same pattern is weaker when one focuses on the below median occupations (blue color).

In the left panel of Figure 2, we analyze instead how separation rates are correlated with horizontal productivity growth, i.e. the likelihood that firms in a sector enter production of a new eight-digit product line. Interestingly, a similar pattern emerges, where mobility of workers in the most knowledge-intensive occupations correlate positively with productivity growth (product expansion), while mobility by workers in the less knowledge-intensive occupations do not seem to be associated with this type of productivity dynamics.

Direction of mobility We then turn our attention to the direction of worker mobility, and especially the per-sector share of firms who hire from a firm with a superior level of labor productivity. In the right panel of Figures 1 and Figures 2 we display the data in a similar scatter plot as described above, but where we use the frequency of hiring from a superior firm instead of separation rates on the x-axis. Once again, we divide workers into those that work in below-median occupations and those that work in the top decile of occupations, and display these groups in blue and red color, respectively. Since our prior is that more knowledge is embodied in workers in the highest paid occupations, we expect these worker mobility events to correlate stronger with both vertical and horizontal productivity growth. The patterns are similar to those observed for separation rates. Hiring from firms with higher levels of productivity appears to be associated with faster productivity growth, both for vertical (Figure 1) and horizontal (Figure 2) productivity growth.

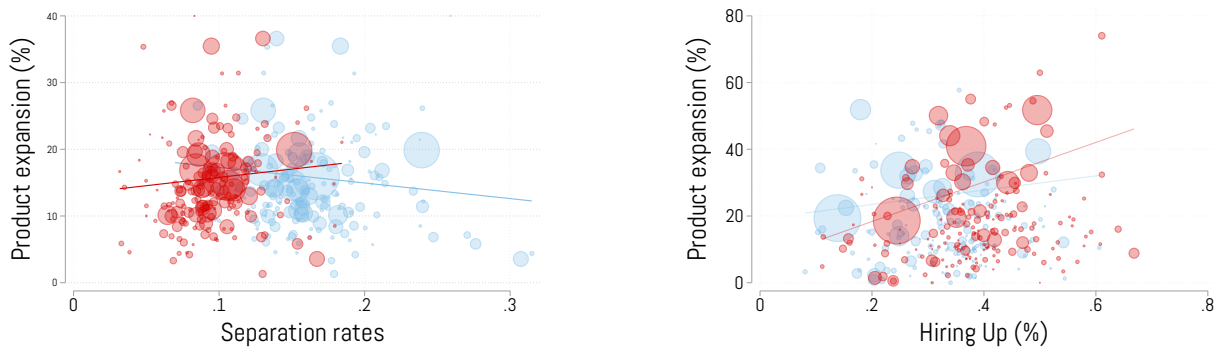
In Online Appendix Tables 6 and 7 we perform regressions for the correlations depicted in the figures above. We report results for estimating the regression line using the bottom half of the occupations according to the income ranking, and using the top decile, respectively. Appendix Table 6 reports the effects on labor productivity growth. Columns (1) and (2) show that the regression estimate is always larger for top decile occupations than for the bottom half. The differences between the estimators are statistically significant in the majority of cases. Table 7 reports the results for product expansion and the same pattern applies. In columns (3) to (6) we add additional controls. Overall, we find that the patterns remain. In column (3) to (4), we control for labor productivity in the sector, in columns (5) and (6) we further control for sectoral volatility. We also include volatility in foreign demand in this pattern, based on a shift-share instrument using the baseline export patterns of firms and the subsequent changes in aggregate global exports to those destinations (see for example [Hummels et al., 2014](#)).

Figure 1: Productivity growth and mobility.



Notes: The left column shows binned scatter plots of the separation rate and the growth in labor productivity for occupations with below median wages (blue) and top decile occupations (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the growth in labor productivity for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry. Data for Sweden, 1997-2019.

Figure 2: Product expansion and mobility.



Notes: The left panel shows binned scatter plots of the separation rate and the likelihood of product expansion for all workers (blue) and top decile occupations as categorized by average earnings (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the likelihood of product expansion for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry and products are denoted at 8-digit. Data for Sweden, 1997-2019.

Importance of mobility One way to assess the importance of these correlations is to relate them to similar estimates related to firms' effort on research and development (R&D). It is generally agreed upon that R&D efforts are quantitatively important for the evolution of firm productivity. In the following, we analyze the size of the correlation of productivity growth and R&D as compared to the correlation with worker mobility patterns. If the correlations with worker mobility are of similar magnitude and pertain despite controlling for the level of R&D, it would be a sign that worker mobility is a significant factor in driving productivity growth. We implement this analysis by employing the same regression framework as in Online Appendix Tables 6 and 7, as described in the previous paragraph, but where we also include dummies for whether firms engage in R&D, such that the sector average of this number denotes the share of firms conducting R&D. In order to be able to compare the effect of mobility with that of R&D, we first standardize our measures of mobility and R&D. We then regress our outcome variables in Figures 1 (mean labor productivity growth) and 2 (product expansion) on standardized separation rates and the standardized measure of R&D. Then we do the same exercise for the direction of mobility, using the standardized rate at which firms hire from a more productive firm.

Table 3: Growth in vertical and horizontal labor productivity with standardized mobility and R&D.

Dep. var.:	Growth in labor productivity		Product expansion	
	Bottom half	Top dec.	Bottom half	Top dec.
	(1)	(2)	(3)	(4)
Panel A				
Separation rate (standardized)	0.003** (0.001)	0.005*** (0.001)	0.000 (0.004)	0.009* (0.005)
R&D activity (standardized)	0.004*** (0.001)	0.003*** (0.001)	0.017*** (0.003)	0.017*** (0.003)
Observations	191	191	190	190
Panel B				
Hiring up (standardized)	-0.005*** (0.002)	0.006*** (0.002)	0.044*** (0.008)	0.083*** (0.010)
R&D activity (standardized)	0.000 (0.002)	0.008*** (0.002)	0.043*** (0.009)	0.070*** (0.009)
Mean hiring up	0.33	0.38	0.34	0.39
Observations	183	180	181	178

Notes: The table shows regression estimates of changes in productivity on worker mobility patterns and R&D activity. Regression estimates are standardized.

We demonstrate our results for how R&D compares with mobility in statistically explaining productivity growth in Table 3. Our conclusion is that in most specifications the links with separation rates and hiring rates are as important as the link to R&D. This is especially the case for the top decile of occupations, while for the bottom half of occupations the coefficient on R&D is usually of a higher magnitude than the one for mobility. The results are slightly noisy and don't always go in the desired direction, but we attribute this noise largely to the fact that R&D data is collected in a survey. Nevertheless, in the majority of cases our conclusion applies: mobility of workers in top decile occupations correlates with productivity growth at a comparable rate as R&D.

If the correlation between mobility and productivity growth is due to knowledge embodied in workers, it is likely that worker mobility from employment (EE move) correlates more strongly with productivity growth as compared to mobility with intermittent unemployment spell (EUE move). During unemployment, workers may simply forget some of the technology they previously mastered, or this technology may become outdated. In the Online Appendix, we therefore examine whether the correlations described in this section are more pronounced for job-to-job (EE) mobility than when workers experience a period of unemployment between work spells (EUE mobility). In Appendix Figures 11 and 13 we note that the relationships described above apply to EE mobility. Similarly, in Appendix Figures 12 and 14, we note that the correlations are substantially weaker for EUE mobility events.⁵

3.2 Microeconomic Evidence

Given the individual-level data at our disposal, we can go a step further and consider causality of the correlation between worker mobility and productivity. To do so, we ideally wish to be able to exogenously vary the set of workers that are employed in a firm. Specifically, the ideal, yet practically and ethically impossible, variation would be generated through random assignment of workers. To proxy for such an ideal scenario, we consider two alternative quasi-experimental variations. First, we build on a literature that exploits sudden and unexpected deaths of individuals as a way to identify the impact that individuals have in various settings. [Becker and Hvide \(2021\)](#) study the impact on young Norwegian firms when entrepreneurs die unexpectedly, while [Sauvagnat and Schivardi \(2023\)](#) do the same for the effect of CEO deaths on more mature firms in Italy. [Jones and Olken \(2005\)](#) study the impact of deaths of national leaders on the growth levels of countries, and [Jaravel et al. \(2018\)](#) explore the impact on inventor team members when one member of the team dies. Related, [Hoey et](#)

⁵For separations, we include cases where the worker transitions into unemployment. For hiring, we consider transitions from one firm to another where the worker experiences a period of unemployment between the two jobs.

al. (2023) study the impact of hospitalizations on the productivity of team members who continue working. Our work is most closely related to [Bertheau et al. \(2022\)](#) and [Jäger and Heining \(2019\)](#), who use large administrative datasets in Denmark and Germany, respectively, to study the impact on firms and workers when incumbent workers die. [Bertheau et al. \(2022\)](#) study the costs to a firm of losing a worker in terms of lost revenues, and [Jäger and Heining \(2019\)](#) identify which workers are complements and substitutes, respectively, to the deceased worker, by studying the effect of workers’ wages when one of their colleagues pass away.⁶ As described in Section [A.2](#) we only use deaths that are unexpected, and therefore less likely to be anticipated by firms or to be correlated with secular trends in a firm’s performance. Second, we use negative exogenous demand shocks to local firms in the same industry, if such shocks lead to a flow of workers away from the negatively hit firms to other firms in the same location. Specifically, we exploit trade-based shift-share instruments based on firms’ baseline export patterns to create these negative shocks (see for example [Hummels et al., 2014](#)). While the first analysis therefore focuses on separations, the second analysis examines new hires⁷.

Separations by sudden and unexpected death A natural methodology to estimate the causal impact of an exogenous separation is to perform an event study of the effect of an exogenous death on productivity. We first examine vertical productivity, and specifically analyse how the mean level of labor productivity evolves during four years before and four years after a death event. Equation [1](#) describes our specification:

$$\log P_{it} = \sum_{\tau=t-3}^{t+3} \alpha_{\tau} \times I_{\text{period}_{\tau}} + \gamma_i + \eta_t + \varepsilon_{it} \quad (1)$$

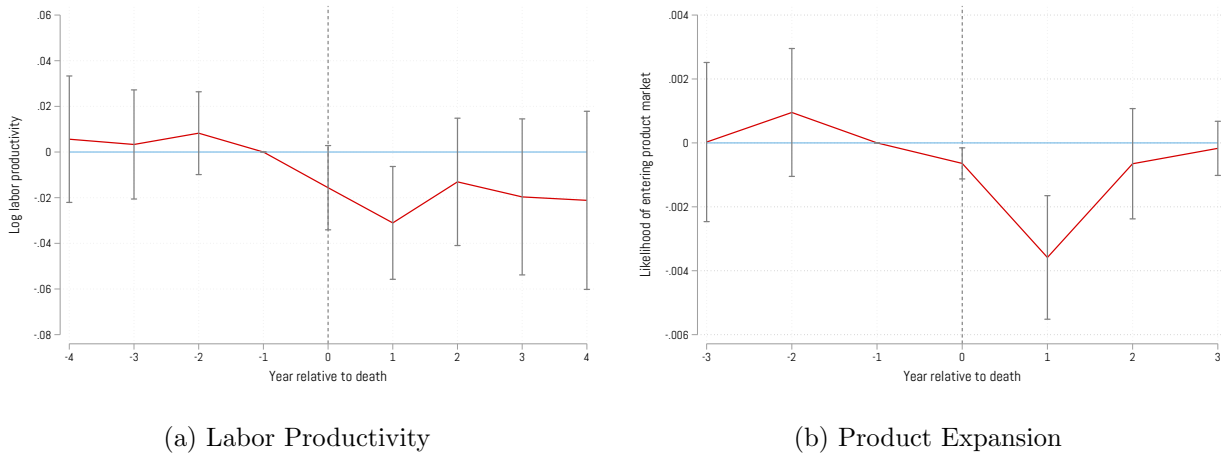
⁶[Bloesch et al. \(2022\)](#) use the impact of worker deaths on firm performance as a way to measure workers’ holdup power. For a different outcome variable, [Andersen and Nielsen \(2011\)](#) study the effect of deaths that result in large windfall financial gains for close relatives of the deceased, and the subsequent investment patterns of these individuals.

⁷Other studies that do not leverage these types of separations include for example [Mion and Oromolla \(2014\)](#), who focus on whether past export experience carries over to new employers when managers move. [Singh and Agrawal \(2011\)](#) find that workers keep using the inventions they registered at previous employers also when they move to a new employer, and [Kaiser et al. \(2015\)](#) and [Braunerhjelm et al. \(2020\)](#) focus on patenting activity overall when knowledge workers move across firms. [Meinen et al. \(2022\)](#) use a control function approach to isolate the causal effect of manager mobility on internationalisation patterns of firms. [Harrigan et al. \(2023\)](#) find that ”techies” (STEM-skill intensive workers associated with innovation) raise productivity of firms. Closest to our study, but without exploiting sudden and unexpected deaths, is likely [Stoyanov and Zubanov \(2012\)](#) who find that the productivity gap between the new and old employer matters for how a worker impacts the new firm it moves to. Positive gaps affect the new firm, and more so if the worker is more educated or a manager. Similarly, [Serafinelli \(2019\)](#) analyses mobility among workers in the Italian region of Veneto, regardless of the reason of the mobility, and finds that hiring workers with experience at the most productive firms significantly increases the productivity of other firms.

where γ_i and η_t indicate firm and year fixed effects and I_{period_t} is an indicator variable for the time before and after a separation. The sample thus includes observations three years before and three years after the event. We keep firms who either suffer one or two exogenous death events during the sample. If the firm suffers two events, we keep both in the sample, but the two death occasions enter as separate events. The year before the event is the reference category.

We report our results of the event study in the left panel of Figure 3. The results indicate that, first, there is a statistically significant and immediate effect of a death on labor productivity. This occurs especially during the year of the event, but the firm experiences a further decrease in the year after. There is a small improvement in the second year but not enough to revert the overall effect, and we therefore see scarring effects. These amount to about two percent of the labor productivity that the firm had prior to the event.

Figure 3: Event study of death on productivity.



Notes: The left figure shows the impact of a worker death on firm labor productivity around the time of a worker death. The corresponding regression specification is $\log P_{jt} = \sum_{\tau=t-3}^{t+3} \alpha_{\tau} \times I_{\text{period}_{\tau}} + \gamma_i + \eta_t + \varepsilon_{it}$. The right figure shows the impact of a worker death on whether a firm starts producing a certain product when the worker that died had experience in producing exactly that product. The corresponding regression specification is $X_{ijt} - X_{ij,t-1} = \sum_{\tau=t-3}^{t+3} \alpha_{\tau} \times I_{\text{period}_{\tau}} \times \text{years}_{ij} + \gamma_i + \eta_t + \varepsilon_{it}$ where X_{ijt} takes the value 1 if firm i produces product j in year t and years_{ij} indicates the number of years of experience the dying worker had of producing product j . We also control for contemporaneous firm sales.

Next, we perform the same analysis with horizontal productivity as outcome variable. We follow equation (1), but we can now use the data in even greater detail. Specifically, we can leverage our dataset to trace the employment history of each worker, allowing us to determine

their experience with each potential product line based on their past employers. For example, a worker that has been employed by a firm producing circular glass bottles of certain shape at any point in their career, is recorded as having experience in producing such glass bottles. One way to specifically test for worker effects on productivity is therefore to estimate whether losing a worker with a certain product experience negatively affects the likelihood that a firm will enter production of that specific product line.

We estimate this regression at the firm-product-year level, with the outcome variable represented by a dummy for whether a firm starts producing a certain product in a given year and the event indicator represented by events where the deceased worker had experience in producing exactly the product concerned. To account for the intensity of the treatment, we compute the number of years that a worker has experience in a specific product line, and multiply the treatment dummy with the number of years of experience. The corresponding regression specification is:

$$X_{ijt} - X_{ij,t-1} = \sum_{\tau=t-3}^{t+3} \alpha_{\tau} \times I_{\text{period}_{\tau}} \times \text{years}_{ij} + \gamma_i + \eta_t + \varepsilon_{it} \quad (2)$$

where X_{ijt} takes the value 1 if firm i produces product j in year t . The variable years_{ij} indicates the number of years of experience the dying worker had of producing product j . We also control for contemporaneous firm sales.

In the right panel of Figure 3 we report the results from the event study on horizontal productivity. We note that the periods before the event are characterised by parallel trends. When the death occurs, there is an immediate small but statistically significant negative effect. In the first year after the death, however, the effect is much larger. In the second year there is no longer a negative effect, but since the second- and third-year changes do not revert the initial hit, the effects seem to last. We conclude that an exogenous separation negatively and permanently reduces the likelihood of a firm entering production of a product in which the departing worker had specific expertise. This finding suggests that at least some product knowledge resides with the worker and is not fully embedded within firms.

Firm growth through exogenous shocks of competitors While the above event studies have focused on the role of separations, we now aim at examining the effect of hiring. While exogenous variation in hiring is difficult, if not impossible, to find, one way to examine the effect of hiring is to exploit negative shocks to other firms in the same location. Large negative shocks that hit firms in the same municipality and in the same sector can increase

hiring, since they reduce the labor demand of workers in a firm’s industry. We exploit trade-based shift-share instruments to create arguably exogenous demand shocks. We hereby consider variation in the direction of mobility, caused by the exogenous shock. Based on the firm-level export patterns in the first year of the sample, we compute firm-level shocks to the demand for their exports based on changes in the global import demand for their products in their specific export markets. We assume for example that if China reduces their imports of a specific type of steel bolt, this will create more of a negative shock for firms that were exporting this product to China in the first year of the sample relative to firms that did not export such steel bolts, or were exporting them to markets other than China. We then calculate for each firm the shock to their local peers, i.e. firms in the same sector, and assume that the demand shocks to a firm’s local peers are negatively correlated with that firm’s number of workers.

We mimic an event study by calculating for each firm in which year its peers (i.e. firms in the same location and industry) experienced their most negative shock to world import demand for their products. We call this year the event year, which is different for each firm. We then restrict the sample to two years before and two years after that year for each firm. We only keep firms whom we observe during the entire event window in order to keep a balanced sample. We residualize each variable of relevance, i.e. firm-level trade shocks to peers, output, employment, and productivity growth, on municipality fixed effects, time-varying sector fixed effects, as well as the firm’s own world import demand shock (to exploit differences in how the firm is affected by global shocks compared to how the peers are affected). The mean residuals across firms for each year relative to the event form the basis for the event.

To focus more specifically on the mechanism in our model—namely, that hired workers bring knowledge from their previous employer—we differentiate between shocks to peers with above-median labor productivity and those with below-median labor productivity. This allows us to measure whether hiring effects differ based on the productivity level of a new worker’s previous employer.

We report the results for the trade-shock-based events in Figures 4 and 5. First, we note that the events appear to mimic real event studies fairly well. The changes in year 0 in the residualized foreign demand levels are sharply negative. First, in Figure 4 we note that a drop in the demand for the exports of local peers induces firms to increase the number of workers that they hire. To see how workers transmit the technology of their previous employers to the new firm, we divide shocks to peers into two categories: shocks that affect above-median productivity peers and shocks that affect below-median productivity peers. Our hypothesis

is that shocks to above-median peers lead to higher productivity among unaffected firms, because the workers bring knowledge about how production processes are designed in firms with high productivity. The opposite is expected to take place when workers move from less productive firms. In Figure 5 we report the impact on labor productivity. Panel a shows that when the event is based on negative shocks to highly (above median) productive firms, then labor productivity growth of the firm in question improves, likely based on the firm's ability to hire workers from more productive firms. The effect appears to be largely contemporaneous, and the increase in levels appears to remain after the event. In panel b it is clear that the effect is the opposite when the shock instead hits less productive firms, i.e. when the new hires come from less productive firms the effect on a firm's labor productivity growth is instead negative.

Summary We can now summarize the findings of this empirical section. We have seen that there is suggestive evidence of worker mobility patterns correlating with aggregate productivity both for vertical and horizontal productivity. We have provided suggestive evidence that worker mobility is a separate and equally important factor driving productivity patterns as compared to R&D activity. We have been able to substantiate these correlations at the microeconomic level through event study analysis of quasi-exogenous mobility events.

These empirical findings motivate us to develop a framework to quantify the aggregate importance of worker mobility in the following sections.

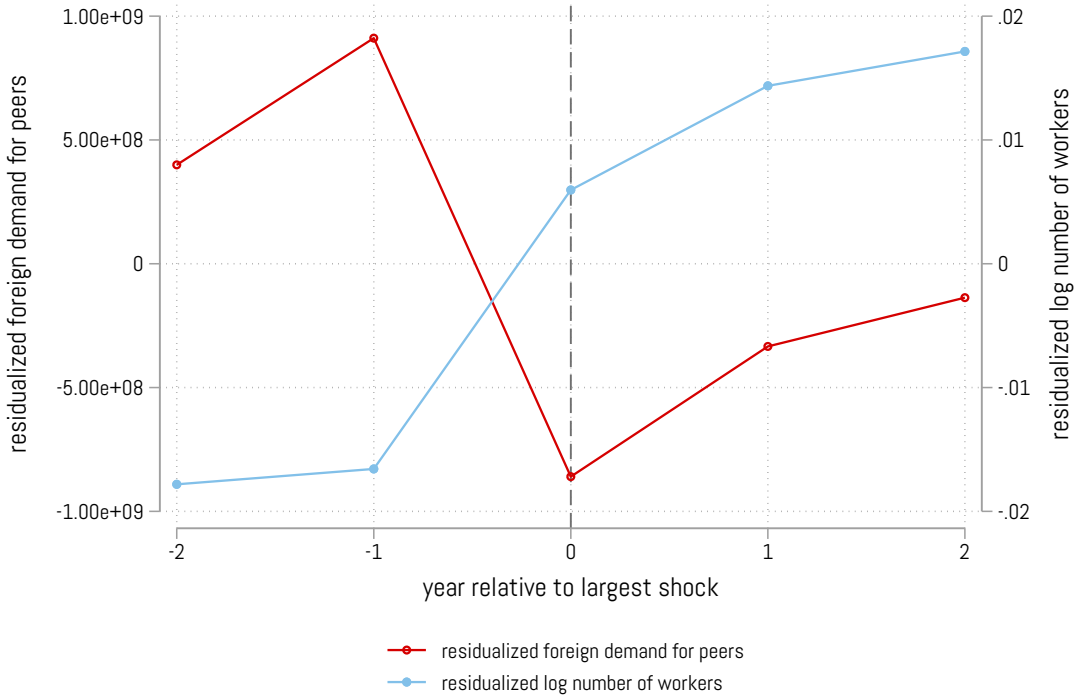
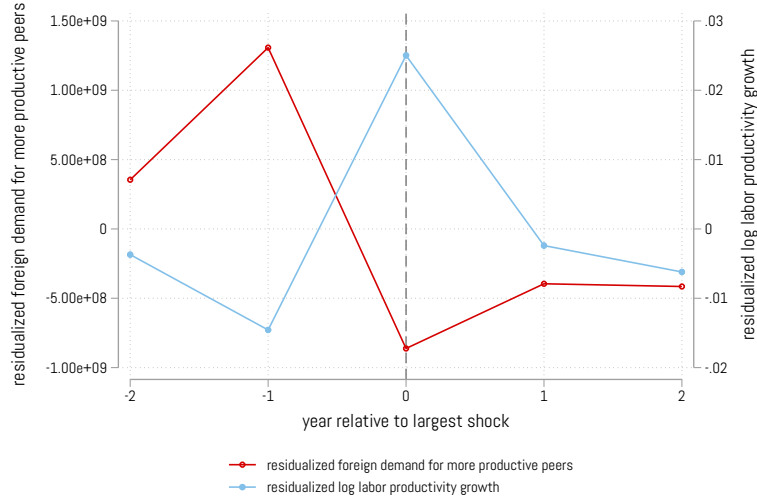
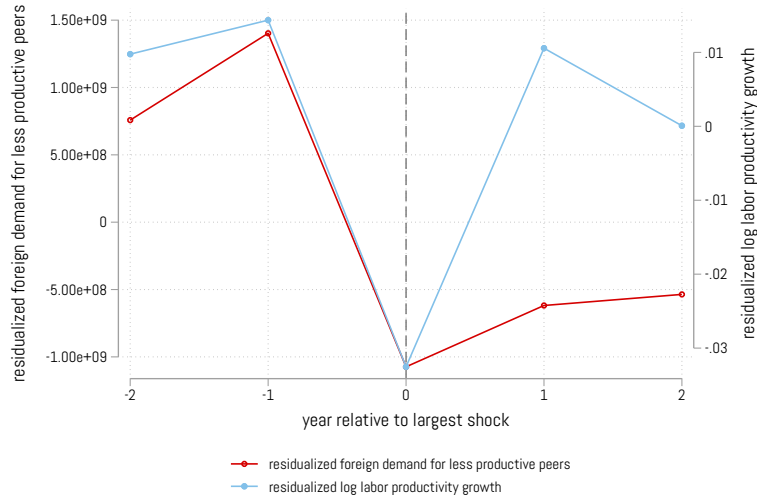


Figure 4: Effect of shocks to local peers on a firm’s employment.

Notes: We mimic an event study by calculating for each firm in which year its peers (i.e. firms in the same location and industry) experienced their most negative shock to world import demand for their products. We call the year the event year, which is different for each firm. We then restrict the sample to two years before and two years after that year for each firm. We only keep firms whom we observe during the entire event window in order to keep a balanced sample. We then residualize each variable of relevance, i.e. firm-level trade shocks to peers, output, employment, and productivity growth, on municipality fixed effects, time-varying sector fixed effects, as well as the firm’s own world import demand shock (to exploit differences in how the firm is affected by global shocks compared to how the peers are affected). The mean residuals across firms for each year relative to the event are plotted in the figure.



(a) Effect on productivity of shocks to peers with above-median productivity.



(b) Effect on productivity of shocks to peers with below-median productivity.

Figure 5: Causal effect of hiring on firm performance.

Notes: We mimic an event study by calculating for each firm in which year its peers (i.e. firms in the same location and industry) experienced their most negative shock to world import demand for their products. We call the year the event year, which is different for each firm. We then restrict the sample to two years before and two years after that year for each firm. We only keep firms whom we observe during the entire event window in order to keep a balanced sample. We then residualize each variable of relevance, i.e. firm-level trade shocks to peers, output, employment, and productivity growth, on municipality fixed effects, time-varying sector fixed effects, as well as the firm's own world import demand shock (to exploit differences in how the firm is affected by global shocks compared to how the peers are affected). The mean residuals across firms for each year relative to the event are plotted in the figure. We separate peers into firms above and below median labor productivity. Panel a shows events based on shocks to peers with above-median labor productivity, and panel b to firms with below-median labor productivity.

4 Theory

In the following, we describe a framework used to estimate the effect of worker disappearances on a balanced growth path. The theory describes a multi-worker firm as a learning and innovation environment where productivity change and diffusion originates. In this economy, firm output per worker changes due to worker mobility, but also in the absence of worker mobility due to in-house innovation.

In the following, we first lay out the details of the economy (cf. section 4.1) and describe the value functions (cf. section 4.2). In this section, we will show that the worker-firm surplus admits an affine representation, which allows us to understand the interplay of firm productivity, size and time. We then derive the laws of motion for the productivity distributions (cf. section 4.3) and the balanced growth path of the economy (cf. section 4.4), using the previous insights. In the following, we first outline a model without on-the-job search in order to facilitate exposition. In section 4.5, we relax this assumption and show how the main model equations change with on-the-job search. All derivations are relegated to Appendix section A.1.

4.1 Environment

Physical Environment The economy is set in continuous time and there is no aggregate uncertainty. The labor market consists of a measure of workers $i \in 1, \dots, N_t^I$ and a measure of firms $j \in 1, \dots, N_t^J$. Workers are endowed with one unit of time each period, that they supply inelastically to the labor market. Both firms and workers are risk neutral, infinitely lived, and discount the future at the risk free rate r . They have heterogeneous and time-varying productivity, denoted $p_{it} \geq \underline{P}$ for workers and $P_{jt} \geq \underline{P}$ for firms, where \underline{P} denotes the minimum productivity threshold. Firm productivity follows an endogeneous distribution function, denoted as $G(P, t)$.

Workers can be employed or unemployed. There is a share u_t of unemployed workers, whose productivity follows the endogeneous productivity distribution $F(p, t)$. When employed, workers can be exogeneously displaced. If unemployed, they receive unemployment benefit $b(t)$, and have a chance to meet a new firm every period.⁸ We assume that firms and workers meet each other in a frictional labor market governed by random search. There is no

⁸Note that the assumption of the independence of unemployment benefits from worker productivity is not crucial, and can be relaxed. If relaxed, we additionally need to assume that surplus renegotiation at the firm satisfies mutual consent, an assumption equally used for instance in [Lise and Robin \(2017\)](#). This is necessary to avoid that the worker's value falls below the unemployment value when the worker learns.

on-the-job search (as in [Bertheau et al. \(2022\)](#)).

Each period, through the entry of new labor market participants, the work force grows by a factor μ_I such that $N_t^I = N_{t-1}^I \mu_I$. Skills of the new labor market entrants are drawn from the productivity distribution $w(p, t)$. Thereafter, worker skills evolve with learning on the job and job mobility. Finally, each period new firms enter the market, with initial size 0, at rate μ_J such that $N_t^J = N_{t-1}^J \mu^J$. New firms imitate existing technology such that they draw a productivity from the endogeneous incumbent firm productivity distribution $G(P, t)$.

Firm and worker productivity evolution An individual firm’s productivity varies over time through firm innovation and worker mobility. In both cases, when firms meet a new worker, or encounter a new technology with productivity ρ , they adopt the new technology whenever it exceeds the current state of the art at the firm, hence $P'_j = \max\{\rho_{it}, P_{jt}\}$. Similarly, workers with productivity p_{it} adopt the current technology of the firm such that $p'_{it} = \max\{p_{it}, P_{jt}\}$.⁹ While worker arrival has the potential to increase firm productivity by bringing new knowledge to the firm, worker displacement can disrupt firm productivity.¹⁰ Figure 6 schematically represents these adaptation processes.

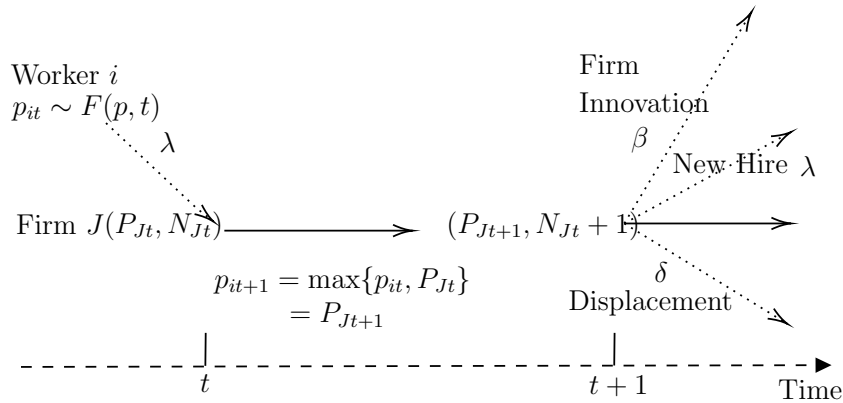


Figure 6: Mobility and Adaptation

Notes: The figure shows the evolution of productivity within the firm together with the events possibly affecting the firm on a time-line.

Specifically, firms search for workers, and meet a new worker ι at rate λ each period. The productivity of the encountered worker, $p_{\iota t}$, is drawn from the endogeneous skill distribution

⁹The notion that firms and worker become closer in terms of technology has been used previously for instance in [Lise and Postel-Vinay \(2020\)](#). Here we assume an instantaneous adaptation of technologies.

¹⁰Without modelling these alternations in detail, we consider them reflective of organizational disruptions, adaptation difficulties or loss in knowledge after a previous worker configuration changes.

of unemployed workers $F(p, t)$. When a worker with productivity p_{it} joins the firm, firm productivity increases if $p_{it} > P_{jt}$. Hence, a firm of productivity P meets a more knowledgeable worker at rate $\bar{F}(P, t)$. Otherwise, the hired worker's productivity is updated to the firm's current productivity level, no change of firm level productivity occurs, and the firm gains a new worker. As a result, a firm increases its productivity through worker arrival with probability

$$\lambda \bar{F}(P, t).$$

When a worker leaves the firm, we assume that the firm experiences productivity adjustments to

$$\tilde{P} = \alpha P + \underline{P}(1-\alpha)$$

with $0 < \alpha < 1$. At the same time, we assume that the worker carries with himself his initial level of productivity, P . These assumptions reflect the idea that a worker's disappearance can create disruptions at the firm, while the re-entry of a worker with the same level of productivity resolves the initial disruption.

The productivity of the firm also evolves through firm-level innovation by drawing from the exogenous idea distribution $V(P, t)$. We denote this idea generation as within firm innovation. At rate β , the firm draws from the idea distribution $V(P, t)$, and adjusts its productivity whenever it is worthwhile doing so. This occurs at rate $\bar{V}(P, t)$.

The search and separation process changes the size of the firm over time. We denote the total number of workers at the firm with N_t . Note that innovation and worker hiring can only increase productivity or leave it unchanged, whereas worker departures can decrease productivity.

Firms produce a single homogeneous good according to the constant returns to scale technology¹¹

$$Y(P, N, t) = P_t N_t$$

Contracts and Negotiations We follow [Bilal et al. \(2022\)](#) and [Bilal et al. \(2021\)](#) regarding the negotiation protocol within the firm. In our baseline set-up without on-the-job search, we make a single assumption on contracting, that is that negotiations involve take-it-or-leave-it

¹¹Constant returns are a crucial assumption that allows us to obtain a balanced growth path in this economy. Note that in [Bilal et al. \(2022\)](#) individual firm technology is also constant returns to scale, but at the aggregate level, decreasing returns result from demand with constant elasticity of substitution across goods.

offers. Notably, this implies that workers receive their unemployment value when being hired from unemployment, and that therefore all workers accept to work for all firms. We describe changes to this contracting framework in section 4.5.

4.2 Value function and productivity distributions

Value Functions We can now write the value of the firm and of unemployed workers. First consider the value of unemployment $U(t)$. It is composed of the flow value of receiving unemployment benefits $b(t)$ and the option value of matching with a firm. Given the negotiation protocol with take-it-or-leave-it offers, the worker is offered his second best outcome when hired from unemployment, leaving his value before and after job finding unchanged. Hence the value of unemployment is simply

$$rU(t) = b(t) + U_t$$

Denote with $\Omega(P, N, t)$ the joint value of the firm and its firm-associated workers. With some abuse of notation, we will denote the marginal values of a change in firm size, Ω_N , with $\Omega_N := \Omega(P, N, t) - \Omega(P, N - 1, t)$, and the marginal value of a change in productivity to value P' as $\Omega_{P',P} := \Omega(P', N, t) - \Omega(P, N, t)$.

The joint value $\Omega(P, N, t)$ is composed of the flow output $Y(P, N, t)$ and the option value of the firm's team. The option value is composed of three terms:

- EU mobility: the change in the value due to an exogenous separation or a labor market exit of one firm-associated worker, occurring with probability δ ,
- UE mobility: the increase in the value due to the matching with an unemployed worker at rate λ
- Innovation: the increase in the value due to innovation within the firm at rate β

We will explain and evaluate these terms in turn. In case of an EU mobility event, the firm loses a worker such that the firm's team experiences a change in value due to a) the new unemployment status of the displaced worker, b) the change in the team size and c) the change in firm productivity due to productivity disruption, leading to change of productivity to \tilde{P} . These three changes total the value of

$$(U(t) - \Omega_N - \Omega_{\tilde{P},P})$$

In the case of a UE hiring event, the firm expands its workforce and updates its productivity if the new worker has a productivity exceeding the current firm productivity P . This involves a change in the firm's team value due to a) the increase in the value due to the expansion of the team, b) the loss of the unemployment value of the new hire, and c) the increase in the value due to a potential productivity upgrading. These three forces total a change in value of

$$\left(\Omega_N - U(t) + \int_P^\infty \Omega_{P',P} dF(P', t) \right)$$

Finally, innovation at rate β leads to an increase in the team's value due to innovation of $\int_P^\infty \Omega_{P',P} dV(P', t)$. We bring together these different forces and write the value of the firm coalition as

$$\begin{aligned} r\Omega(P, N, t) &= Y(P, N, t) + \Omega_t \\ & \text{(EU Mobility)} + \delta (U(t) - \Omega_N - \Omega_{\bar{P},P}) \\ & \text{(UE Mobility)} + \lambda \left(\Omega_N - U(t) + \int_P^\infty \Omega_{P',P} dF(P', t) \right) \\ & \text{(Innovation)} + \beta \left(\int_P^\infty \Omega_{P',P} dV(P', t) \right) \end{aligned}$$

The incentive compatibility constraints ensure that the firm makes non-negative profits and that the workers' value in employment, denoted $W(P, t)$, is not smaller than the unemployment value, such that i) $\Omega(P, N, t) \geq NU(t)$ and ii) $W(P, t) \geq U(t)$ hold at all points in time. The definition of the lowest support \underline{P} ensures that these two criteria are satisfied on all points of the productivity distribution. We derive the continuous time Bellman equation from the discrete time analogue in Appendix section [A.1](#).

Surplus Representation It is useful to represent the value function in form of the worker-firm surplus $S(P, N, t)$ such that $\Omega(P, N, t) = S(P, N, t) + NU(t)$. We can write the surplus value equation as

$$rS(P, N, t) = (P - b(t))N + S_t + (\lambda - \delta) S_N + \omega(P, N, t) \quad (3)$$

where the last term denotes productivity changes due to mobility and innovation, $\omega(P, N, t)$

$$\omega(P, N, t) = \left(\lambda \int_P^\infty S_{P',P} dF(P', t) + \beta \int_P^\infty S_{P',P} dV(P', t) - \delta S_{\bar{P},P} \right)$$

Using this equation, we show that the surplus equation satisfies an affine representation such that $S(P, N, t) = N\hat{S}(P, t) + S^0(P, t)$. Firm size affects the worker-firm surplus hence only linearly in the slope of the worker-firm surplus while leaving the intercept independent of firm size (cf. Appendix section [A.1](#) for the derivation).

Result 1 (Affine Surplus Representation) *The surplus equation is affine in firm size*
 $S(P, N, t) = N\hat{S}(P, t) + S^0(P, t)$

This is an important finding allowing us to define a balanced growth path in section [4.4](#).

4.3 Productivity Distributions

We can now derive the law of motion of the endogenous distributions of firm productivity $g(P, t)$ and of unemployed workers $f(P, t)$, by combining the in-flows and out-flows of workers and tracing instances of innovation activity. We first turn to the distribution of firm productivity. Inflows into the firm productivity distribution $g(P, t)$ derive from four different sources. First, a measure $G(P, t)$ of firms finds a P -skilled unemployed worker at rate $\lambda f(P, t)$. Second, a measure $G(P, t)$ of firms finds productivity P through innovation at rate $\beta v(P, t)$. Third, a measure δ of firms experiences a disappearance and sees their productivity adjust to $\tilde{P} = \alpha P + \underline{P}(1-\alpha)$. The inflow of new firms with productivity P' is hence $g(\tilde{P}/\alpha - \frac{(1-\alpha)\underline{P}}{\alpha}, t)\delta$. Finally, there is new entry of firms at rate $\mu_f g(P, t)$. The outflow is composed of the flip side of these events. First, a measure $g(P, t)$ of firms finds a higher-skilled worker at rate $\lambda \bar{F}(P, t)$. Second, a measure $g(P, t)$ of firms finds a higher-skilled worker at rate $\lambda \bar{F}(P, t)$, and finally, a measure $g(P, t)$ experiences adaptation and productivity change at likelihood $g(P, t)\delta$. Hence, we can write the law of motions as

$$\begin{aligned}
\frac{\partial g(P, t)}{\partial t} = & \underbrace{\underbrace{f(P, t)G(P, t)\lambda}_{\text{Mobility Upgrade}} + \underbrace{\beta v(P, t)G(P, t)}_{\text{Innovation}} + \underbrace{\delta g\left(\frac{P - (1-\alpha)\underline{P}_t}{\alpha}, t\right)}_{\text{Displacement}} + \underbrace{\mu_f g(P, t)}_{\text{New Firms}}}_{\text{Inflow}} \\
& - \underbrace{\underbrace{\lambda g(P, t)\bar{F}(P, t)}_{\text{Mobility Upgrade}} + \underbrace{\beta g(P, t)\bar{V}(P, t)}_{\text{Innovation}} + \underbrace{g(P, t)\delta}_{\text{Displacement}}}_{\text{Outflow}}
\end{aligned} \tag{4}$$

We also keep track of the productivity distribution of unemployed workers $f(P, t)$. To do this, we consider the change in the share of unemployed workers with skill level P due to inflows and outflows from the pool of the unemployed. On the one hand, a measure $\lambda f(P, t) \frac{N_t^J}{u_t N_t^I}$

finds a new job. On the other hand, the inflow into unemployment derives from a measure $g(P, t)\delta \frac{N_t^J}{u_t N_t^I}$ who enter unemployment after displacement from firms with productivity P and a measure $\mu_w w(P, t)\frac{N_t^I}{u_t N_t^I}$ who newly enter the job market. By bringing these effects together, we obtain

$$\begin{aligned} \frac{\partial f(P, t)}{\partial t} = & \\ & \underbrace{\underbrace{\delta g(P, t)\frac{N_t^J}{u_t N_t^I}}_{\text{Displacement}} + \underbrace{\mu w(P, t)\frac{N_t^I}{u_t N_t^I}}_{\text{New Entrants}}}_{\text{Inflow}} - \underbrace{\lambda f(P, t)\frac{N_t^J}{u_t N_t^I}}_{\text{Outflow: New Hires}} \end{aligned} \quad (5)$$

4.4 Balanced growth path of the economy

We can now define an equilibrium and a balanced growth path in this economy.

Definition 1 (Equilibrium) *Given the initial productivity distributions $f(z, 0)$ and $g(z, 0)$ and the exogenous idea distributions $v(z, 0)$ and $w(z, 0)$ as well as initial worker and firm sizes N_0^J, N_0^I , an equilibrium is a set of three functions (f, g, S) such that i) given (f, v) , S satisfies the surplus equation for all (z, N, t) as in equation 3, iii) (f, g) satisfy the laws of motion in equations 5 and 4.*

Our interest in a study of the growth rate of the economy motivates the following definition of the balanced growth path of this economy.

Definition 2 (Balanced Growth Path) *A balanced growth path is a number γ such that*

$$\begin{aligned} F(P, t) &= \Phi(Pe^{-\gamma t}) \\ G(P, t) &= \Theta(Pe^{-\gamma t}) \\ S(P, N, t) &= e^{\gamma t}\sigma(Pe^{-\gamma t}, N) \\ W(P, t) &= \Pi(Pe^{-\gamma t}) \\ V(P, t) &= \Upsilon(Pe^{-\gamma t}) \end{aligned}$$

for all (P, N, t) with the initial conditions $\Phi(P), \Theta(P), \Pi(P), \Upsilon(P)$ and (Φ, Θ, σ) are an equilibrium.

It is immediate that we can find a balanced growth representation of the surplus function given its affine representation such that $S(P, N, t) = N\hat{S}(P, t) + S^0(P, t) = \hat{\sigma}(Pe^{-\gamma t})N + \sigma_0(Pe^{-\gamma t}) = \sigma(Pe^{-\gamma t}, N)$, cf. Appendix section A.1.4. We study the balanced growth path of the productivity distributions next. Following the definition of the balanced growth path,

we can define the densities of the productivity distributions as $f(P, t) = e^{-\gamma t} \Phi'(Pe^{-\gamma t})$, $g(P, t) = e^{-\gamma t} \Theta'(Pe^{-\gamma t})$. As a result, $\frac{\partial f(P, t)}{\partial t} = -\gamma e^{-\gamma t} \Phi'(Pe^{-\gamma t}) - P\gamma(e^{-\gamma t})^2 \Phi''(Pe^{-\gamma t})$, and $\frac{\partial g(P, t)}{\partial t} = -\gamma e^{-\gamma t} \Theta'(Pe^{-\gamma t}) - P\gamma(e^{-\gamma t})^2 \Theta''(Pe^{-\gamma t})$. To proceed, we will make the following two assumptions.

Assumption 1 *All initial distributions $D \in \{\Phi, \Theta, \Pi, \Upsilon\}$ have a Pareto tail with parameters θ and k_D , such that*

$$\lim_{x \rightarrow \infty} \frac{1 - D(x, 0)}{x^{-1/\theta}} = k_D$$

Assumption 2 *The two distributions $D \in \{\Pi, \Upsilon\}$ of new ideas through innovation Υ and the distribution of new workers Π evolve with the distribution of firm productivity Φ such that*

$$1 - D(x, t) = \alpha_D k_\Phi x_t^{-1/\theta}$$

While the first assumption expresses that the stock of ideas is inexhaustible (and follows [Lucas and Moll, 2014](#)), the second assumption flexibly links the current distribution of innovation and worker ability to the distribution of firms. We believe that such a relationship makes intuitive sense: in the long run, the education of labor market entrants evolves with the current state of knowledge in the economy and so does the stock of innovative ideas.

Using equations [4](#) and [5](#), together with assumptions [1](#) and [2](#), we obtain two equations

$$\begin{aligned} \frac{(\lambda + \frac{\gamma}{\eta_p \theta})}{\delta} &= \frac{k_\Theta}{k_\Phi} - \frac{\mu_w}{\delta} \frac{N_0^I}{N_0^J} \alpha_\Pi \\ \gamma/\theta &= \lambda \frac{k_\Phi}{k_\Theta} + \beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta} + \mu_f + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) \end{aligned}$$

where $\frac{N_t^J}{u_t N_t^I} = \eta_p$ (cf. Appendix section [A.1.5](#)).

4.5 Extension with on-the-job search

So far, we have entertained the assumption that workers cannot search on the job. In the following, we relax this assumption by allowing workers to move across jobs without intervening unemployment spells. Given our set-up, we will show that we can characterize mobility decisions of workers and that the previous insights pertain with only minor modifications. We will then show that the equilibrium equations on the balanced growth path feature an additional margin due to job mobility. In the following, we will first describe additional assumptions necessary for the case of job-to-job mobility before extending the

model equations.

Additional Assumptions We assume that with chance $s\lambda(1 - u_t)$, a firm receives a job offer from an employed worker and with chance λu_t from an unemployed worker. Similarly, a firm loses a worker to another firm at rate $\tilde{\lambda}s(1 - u_t)$. We assume that job-to-job mobility is a less disruptive process than displacement such that no productivity disturbance occurs at the firm due to job-to-job mobility.¹²

Contracting and Mobility Contracts follow the sequential auction framework in [Bilal et al. \(2021\)](#) that is i) firms can vary contract offers according to characteristics of workers, ii) firms can counter offers received by employees, and iii) contracts are only renegotiated with mutual consent after a credible threat. These assumptions clarify that a worker in negotiations between two firms will always receive the second best offer. Moreover, the worker will move to the firm with the highest marginal value. As an incumbent worker only contributes to the worker-firm coalition through production, but potentially contributes to learning at a receiving firm, we can analyze the mobility decisions of the worker. Specifically, the marginal value at an incumbent firm is

$$\Omega(P, N, t) - \Omega(P, N - 1, t) := \Omega_N(P, N, t),$$

and at the outside firm

$$\begin{aligned} & \Omega(\max\{P', P\}, N' + 1, t) - \Omega(P', N', t) \\ &= \Omega_N(P', N' + 1, t) + (\Omega(P, N' + 1, t) - \Omega(P', N' + 1, t)) I_{P-P' \geq 0}. \end{aligned}$$

We hence know that the contract C is such that

$$C = \min \{ \Omega_N(P, N, t), \Omega_N(P', N' + 1, t) + (\Omega(P, N' + 1, t) - \Omega(P', N' + 1, t)) I_{P-P' \geq 0} \}.$$

We know that the worker $p_{it} = P$ meeting a firm $P_{jt} = P'$ is moving to the outsider firm if

$$\Omega_N(P, N, t) \leq \Omega_N(P', N' + 1, t) + (\Omega(P, N' + 1, t) - \Omega(P', N' + 1, t)) I_{P-P' \geq 0}.$$

To further study the direction of worker mobility, we follow a guess-and-verify approach. Specifically, we guess that surplus continues to take the form of an affine representation in firm size even with on-the-job search. We will verify this assumption later on.

¹²This is a necessary assumption to preserve tractability. Under this assumption, mobility leaves the joint surplus of the worker firm coalition unchanged (as in [Postel-Vinay and Robin, 2002](#)), which facilitates the analysis considerably.

Assumption 3 (Affine Representation) *The surplus equation satisfies*

1. *Surplus is affine in N : $S(P, N, t) = \hat{S}(P, t)N + S^0(P, t)$.*
2. *$\hat{S}(P, t), S^0(P, t)$ are weakly increasing in P .*

Given this guess, the mobility equation hence simplifies to

$$\begin{aligned} \Omega_N(P, N, t) &\leq \Omega_N(P', N' + 1, t) + (\Omega(P, N' + 1, t) - \Omega(P', N' + 1, t)) I_{P-P' \geq 0} \\ \hat{S}(P, t) &\leq \hat{S}(P', t) + \left((\hat{S}(P, t) - \hat{S}(P', t)) (N' + 1) + (S^0(P) - S^0(P')) \right) I_{P-P' \geq 0} \end{aligned}$$

Using our assumptions, we know that this always holds true, irrespective of whether the worker meets a more or less productive firm. Concretely, if the outside firm is more productive than the incumbent, no learning takes place but the marginal return is higher at the outside firm. If the outside firm is less productive than the current firm, then the difference in marginal value is at least as high as the benefit from learning, such that the worker moves as well. Note that this setting is different from the standard mobility choices in [Postel-Vinay and Robin \(2002\)](#) where workers move to an outside firm only if its productivity exceeds the productivity of the incumbent firm¹³.

Value Functions and Distribution Functions Using these insights, we can write the surplus equation as

$$\begin{aligned} rS(P, N, t) &= N(P - b(t)) + S_t \\ \text{(EU Mobility)} &+ \delta(-S_N + S_{\bar{P}, P}) \\ \text{(Mobility)} &+ \lambda \left(u_t \int_P^\infty S_{P', P} dF(P', t) + s(1 - u_t) \int_P^\infty S_{P', P} dG(P', t) \right) \\ &+ \lambda \left(S_N - s(1 - u_t) \int_P^\infty S_{N'}(P', t) dF(P', t) \right) \\ \text{(Innovation)} &+ \beta \int_P^\infty S_{P', P} dV(P', t) \end{aligned}$$

Compared to the setting without on-the-job search, we find that the option value features two additional terms. The first term is the expected gain due to learning from workers hired from other firms and the second term is the loss in value at the origin firm associated with a job-to-job mobility.¹⁴ We verify that this surplus equation permits an affine representation

¹³As a result, in this model, there is no surplus renegotiation at the job through job search - while there is a potential renegotiation due to the incentive compatibility constraints.

¹⁴Note that due to the affine representation, $S_{N'}(P', t)$ is independent of firm size at the origin firm N' .

(cf. Appendix section [A.1.7](#)). The productivity distribution of firms similarly changes to

$$\begin{aligned}
\frac{\partial g(P, t)}{\partial t} = & \underbrace{\beta v(P, t)G(P, t)}_{\text{Innovation}} + \underbrace{\mu_f g(P, t)}_{\text{New Firms}} + \underbrace{g(P, t)G(P, t)\lambda s(1 - u)}_{\text{Mobility Upgrade EE}} + \underbrace{f(P, t)G(P, t)\lambda u}_{\text{Mobility Upgrade UE}} \\
& \underbrace{\hspace{10em}}_{\text{Inflow 1}} \\
& + \underbrace{\delta g\left(\frac{P - (1 - \alpha)P_t}{\alpha}, t\right)}_{\text{Inflow 2: Displacement}} \\
& - \underbrace{\lambda u g(P, t)\bar{F}(P, t)}_{\text{Mobility Upgrade UE}} - \underbrace{\lambda s(1 - u)g(P, t)\bar{G}(P, t)}_{\text{Mobility Upgrade EE}} + \underbrace{\beta g(P, t)\bar{V}(P, t)}_{\text{Innovation}} + \underbrace{g(P, t)\delta}_{\text{Displacement}} \\
& \underbrace{\hspace{10em}}_{\text{Outflow}}
\end{aligned}$$

Compared to the flow equation without job-to-job mobility, we find two new terms that are associated, respectively, with the arrival or departure of workers to other firms. Note that the distribution function for unemployed worker productivity remains unaffected. Taking these insights together, we find that the limiting equation on the balanced growth path is therefore altered to

$$\gamma/\theta = \lambda \left(\frac{k_\Phi}{k_\Theta} u + s(1 - u) \right) + \beta \alpha \gamma \frac{k_\Phi}{k_\Theta} + \mu_f + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right)$$

In the following section, we will demonstrate how we can apply this equilibrium equation to the data. We will then empirically illustrate its implications for quantifying the importance of worker mobility for aggregate growth.

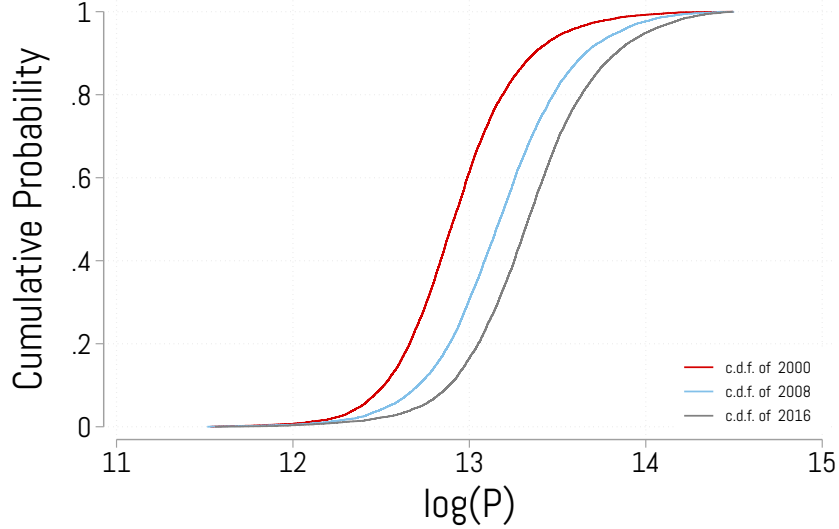
5 Results

In the following, we show quantitative results using micro-economic firm data on output and worker mobility events. We first present the calibration argument in section [5.1](#), before proceeding to show the empirical results in section [5.2](#). After presenting parameter estimates and the growth decomposition into parts deriving from mobility and innovation, we present an application in section [5.3](#). Through a sub-sample analysis, we demonstrate the change in the growth decomposition due to a recent decline in labor mobility .

5.1 Calibration argument

A look at the productivity data for Sweden in figure 7 reveals that the distribution of productivity seems indeed to have shifted over time, in line with the premises of our model. In this section, we would like to leverage the model equations to understand the importance

Figure 7: Shifting Productivity distribution



Notes: The figure shows the empirical density of firm productivity for three years, focusing on the core of the productivity distribution.

of labor mobility for this shift in the productivity distribution. To do so, we leverage the two equilibrium equations 6 and 7 which describe the equilibrium unemployment u and economic growth γ given labor market and idea distribution parameters

$$\frac{(\lambda + \frac{\gamma}{\eta_p \theta})}{\delta} = \frac{k_\Theta}{k_\Phi} - \frac{\mu_w}{\delta} \frac{N_0^I}{N_0^J} \alpha_\Pi \quad (6)$$

$$\gamma/\theta = \lambda \left(\frac{k_\Phi}{k_\Theta} u + s(1-u) \right) + \beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta} + \mu_f + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) \quad (7)$$

We specialize the productivity distributions as Pareto distributions with countercumulative distribution function $\text{Prob}(X > x) = \kappa^{1/\theta} x^{-1/\theta}$.¹⁵ We would now like to pin down the labor and idea distribution parameters by leveraging firm productivity and worker mobility data. First, the calibration of labor market parameters mostly follows standard practices. In the

¹⁵Given this parameterization, $k_D = \kappa^{1/\theta}$ in the model.

data, we can estimate the likelihood of firms to hire a worker from unemployment, $UE = u\lambda$, and the likelihood of firms to hire a worker from employment, $EE = \lambda(1 - u)s$, as well as the average firm size $f = \frac{(1-u)N^I}{N^J}$ and the likelihood of losing a worker to unemployment, δ . We obtain estimates of these rates with simple sample averages over the firm distribution. Specifically, we estimate δ from EU mobility events as the likelihood of firms to experience a worker exit.

$$\text{Prob}\{\text{EU}\} = \delta$$

such that $E_{\Theta}[EU] = \hat{\delta}$, where the subscript Θ denotes averages over the firm distribution. Similarly, we estimate $\hat{f} = E_{\Theta}\left[\frac{N^I(1-u)}{N^J}\right]$, and we estimate UE and EE from UE and EE mobility events as firms' likelihood of experiencing such a worker entry

$$\text{Prob}\{\text{Hire—UE Transition}\} = UE$$

$$\text{Prob}\{\text{Hire—EE Transition}\} = EE$$

such that $E_{\Theta}[\text{Hire}|\text{UE Transition}] = \hat{UE}$ and $E_{\Theta}[\text{Hire}|\text{EE Transition}] = \hat{EE}$. From these estimates, the model predicts a mapping to pin down μ_w and μ_f .¹⁶

To pin down the remaining parameters, we will use microeconomic data on worker events and firm productivity trajectories. Specifically, we use firm-level data on a) average worker productivity $P = Y/N$, obtained as (revenue-based) value-added per worker, b) mobility events, obtained as indicators whether firms experience a new arrival of a worker - including whether the new hire is a labor market entrant, moves from unemployment or has previously worked at other firms - or a worker departure - including whether the departure was exogenous or not - , c) expenditure data on R&D as well as d) demand shocks as obtained through shift-share instruments, building on [Hummels et al. \(2014\)](#). We leverage shift-share instruments to control for revenue-based changes in value added per worker due to demand shocks. We will show in the following how we use this data for recovering the parameters of the model.

First, we can pin down productivity losses due to worker mobility, α , using firms' mobility

¹⁶The equilibrium relationship for the pool of unemployed, requiring inflows into unemployment to balance outflows from unemployment, yields

$$\mu_I = (\lambda u - \delta) \frac{N^J}{N^I} = \frac{(UE - \delta)(1 - u)}{f}.$$

Constancy of the average firm size f implies $\mu_I = \mu_f$. Finally, the fact that new workers always enter the economy through unemployment implies $\mu_I = \mu_w u$. More details can be found in Appendix section [A.1.8](#).

events. We set $\underline{P} = 0$, such that in the event of an exit of a worker to unemployment, productivity changes to αP . We can estimate α on the sample of firms, indexed with letter i , experiencing a worker exit to non-employment due to worker death at time t , using the regression specification

$$P_{i,t} - P_{i,t-1} = \sum_{\tau=t-2}^{t+2} (\alpha_{\tau} - 1) \times I_{\text{period}_{\tau}} + \gamma_i + \eta_t + \varepsilon_{it}$$

where ε denotes simple measurement error. We set α equal to the first coefficient after the death event, so $\alpha = \alpha_1$. We leverage our data on unexpected worker deaths to avoid reverse causality. We include firm and year effects.

Second, we can calibrate the likelihood of innovation, β , using R&D data. To do this, we factor the likelihood of productivity increases in the absence of mobility into two terms: a) the likelihood of innovation and b) the likelihood of productivity increases given innovation

$$\text{Prob}\{\Delta P > 0 | \text{No Mobility}\} = \text{Prob}\{\text{Innov.} | \text{No Mob}\} \text{Prob}\{\Delta P > 0 | \text{Innov.} \& \text{No Mob}\}$$

For the estimation of the first part, we estimate $\text{Prob}\{\text{Innov} | \text{No Mob}\} = G(z_{j,t}\beta)$ using a logit regression based on innovation data, and a vector of predictive variables z , including labor productivity, firm size, sector and year effects as well as shift-share demand shocks. Using the predictive value $\hat{\text{Innov}}$, we can obtain an estimate of β

$$\text{Prob}\{\hat{\text{Innov}} | \text{No Mob.}\} = \beta$$

such that $E_{\Theta}[\hat{\text{Innov}}] = \hat{\beta}$.

Third, we can use the model's predictions on the likelihood of productivity increases in specific cases to calibrate the tail parameter of ideas, θ . In the absence of worker mobility, the model predicts productivity increases through innovation at rate $\bar{\Upsilon}(P, t)$, such that

$$\text{Prob}\{\Delta P > 0 | \text{Innov.} \& \text{No Mob}\} = (\alpha_{\Upsilon} \kappa_{\Phi})^{1/\theta} (P e^{-\gamma t})^{-1/\theta}$$

In the case of mobility from labor market entrants, the likelihood of productivity increases is $\bar{\Pi}(P, t)$, such that

$$\text{Prob}\{\Delta P > 0 | \text{Enter}\} = (\alpha_{\Pi} \kappa_{\Phi})^{1/\theta} (P e^{-\gamma t})^{-1/\theta}$$

In the event of UE or EE mobility, the likelihood is

$$\text{Prob}\{\Delta P > 0|\text{UE}\} = k_{\Phi}^{1/\theta} (Pe^{-\gamma t})^{-1/\theta} \text{ and } \text{Prob}\{\Delta P > 0|\text{EE}\} = k_{\Theta}^{1/\theta} (Pe^{-\gamma t})^{-1/\theta}$$

respectively. These three equations jointly suggest a regression specification to estimate θ using the likelihood of productivity changes, averaged over productivity levels P and time t , forming $n = 1, \dots, N$ observations, such that

$$\begin{aligned} \log E [\text{Prob}\{\Delta P > 0\}]_{n,t} &= c_{\text{No Mobility, Innov}} + c_{\text{Enter}} + c_{\text{UE}} + c_{\text{EE}} - 1/\theta \log P_{n,t} + \gamma/\theta t + u_{n,t} \\ &= c_0 - 1/\theta (\log P_{n,t} - \gamma t) + u_{n,t} \end{aligned}$$

Notably, we bin labor productivity P across firms within a year in equal sized bins. Across productivity-year bins, we can then estimate the parameter θ .¹⁷

Using this calibration strategy, we can recast the two equilibrium equations 6 and 7 as (cf. Appendix section A.1.9 for derivation)

$$\begin{aligned} \frac{\gamma}{\theta} &= UE \frac{k_{\Phi}}{k_{\Theta}} + EE + \beta \alpha_{\Upsilon} \frac{k_{\Phi}}{k_{\Theta}} + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) + (UE - \delta) \frac{(1-u)}{f} \\ \frac{\gamma}{\theta} &= \frac{(1-u)}{uf} \left(\delta \frac{k_{\Theta}}{k_{\Phi}} - \frac{((UE - \delta)\alpha_{\Pi} + UE)}{u} \right). \end{aligned}$$

We can see that this equation relates parameter estimates to the growth rate γ , the unemployment rate u and the relative efficiencies of innovation sources α_{Π} and α_{Υ} . Next, we will discuss calibration estimates and conclusions we can draw about the relative importance of innovative sources for productivity.

5.2 Model estimates and Growth Decomposition

Parameter estimates We summarize the set of estimated parameters in Table 10 in the Appendix, with the two panels in Figure 8 showing a graphical representation of the estimation results for the skill depreciation parameter α , on the left side, and the productivity distribution parameter θ , on the right side. While the estimated labor market parameters are rather standard, the innovation parameters α , θ and β are a novel feature of our theory. In our estimates, we find that firms' productivity declines on average by 2% of their labor productivity when losing a worker such that $\alpha = 0.98$. None of the previous literature

¹⁷Note that this equation could suggest an estimation of α_{Υ} , α_{Π} and $\frac{k_{\Phi}}{k_{\Theta}}$. However, such an estimation would require excluding the coexistence of ideas arriving from different sources. which would likely yield biased results.

has estimated precisely comparable estimates of the effect of worker disappearances on firm output per worker. However, [Sauvagnat and Schivardi \(2023\)](#) report a drop in ROA of 2.1% after the death of an executive in thin labor markets and of 0.8% in thick labor markets which is quantitatively comparable to our results. We also find a scale parameter of the Pareto distribution θ of 0.61. We can compare our estimate for the tail Parameter θ to values used in [Lucas and Moll \(2014\)](#) who consider values between 0.5 and 0.8 for the US economy. We find $\beta = 0.02$, such that (after controlling for observables), we expect a small share of firms to perform innovation. While this number is low, the literature has long noted that there is a significant share of firms without R&D expenditures ([Klette and Kortum, 2004](#)).

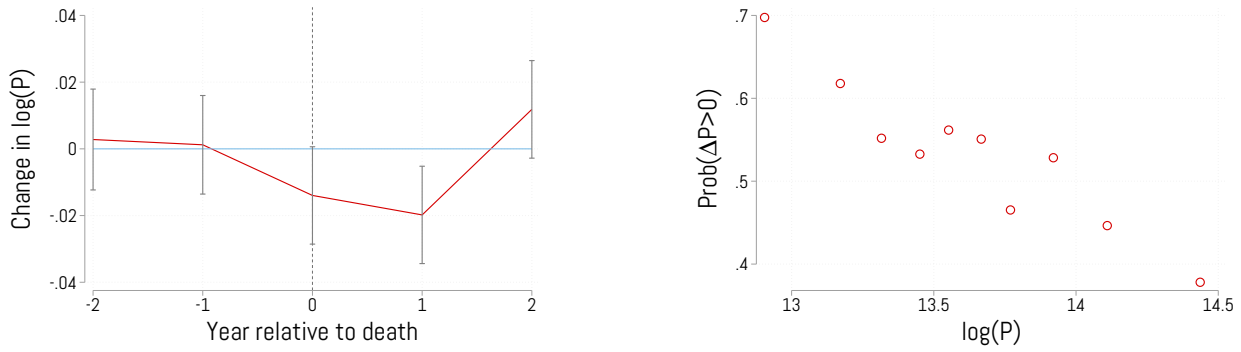


Figure 8: Parameter estimates

Notes: The left panel shows the impact of a worker death on firm labor productivity around the time of a worker death. The corresponding regression specification is $P_{i,t} - P_{i,t-1} = \sum_{\tau=t-2}^{t+2} (\alpha_{\tau} - 1) \times I_{\text{period}_{\tau}} + \gamma_i + \eta_t + \varepsilon_{it}$. The right panel shows the likelihood of firm productivity increases for a new hire event. Estimation is performed across year-specific bins of firm productivity. The corresponding estimation equation is $\log E[\text{Prob}\{\Delta P > 0\}]_{n,t} = c_0 - 1/\theta (\log P_{n,t} - \gamma t) + u_{n,t}$

Given these parameter estimates, we can analyze the implied relationship between the relative productivity distribution parameters $\frac{k_{\Phi}}{k_{\Theta}}$, and the relative innovation intensities of innovation α_{Υ} and labor market entry α_{Π} . We illustrate this relationship in Figure 15 in the Appendix.¹⁸ The figure illustrates the economically relevant range of the parameter $\frac{k_{\Phi}}{k_{\Theta}}$ such that $\alpha_{\Upsilon} > 0$ and $\alpha_{\Pi} > 0$. Over this range, it is mostly the case that $\alpha_{\Upsilon} > \alpha_{\Pi}$, such that the distribution

¹⁸We here make use of the mapping

$$\alpha_{\Upsilon} = \frac{\left(\frac{\gamma}{\theta} - UE \frac{k_{\Phi}}{k_{\Theta}} - EE - \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) - (UE - \delta) \frac{(1-u)}{f} \right)}{\beta \frac{k_{\Phi}}{k_{\Theta}}}$$

$$\alpha_{\Pi} = \frac{\delta \frac{k_{\Theta} u}{k_{\Phi}} - \frac{\gamma u^2 f}{\theta(1-u)} - UE}{(UE - \delta)}$$

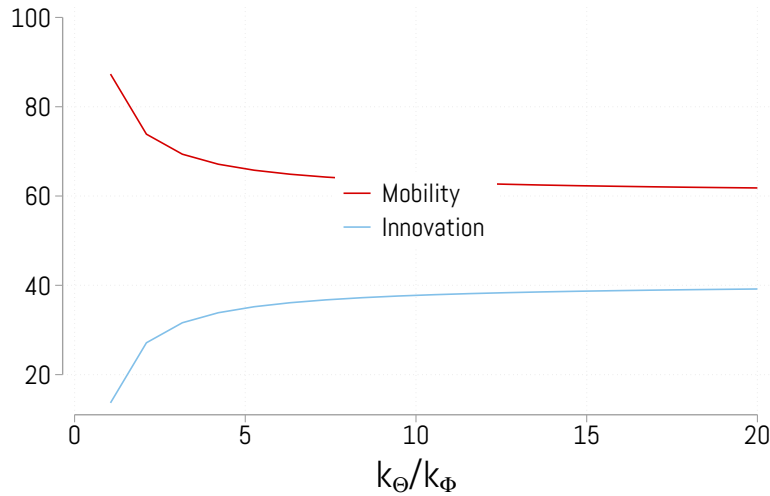
of new ideas has a higher mean than the distribution of skills of new labor market entrants, as expected.

Growth Decomposition Using these estimates, we can decompose economic growth into four parts: worker mobility, innovation, new firm arrival and worker displacement, as shown in equation 8.

$$\gamma = \overbrace{\theta UE \frac{k_\Phi}{k_\Theta}}^{\text{Mobility}} + \overbrace{\theta EE}^{\text{Innovation}} + \overbrace{\theta \beta \alpha \Upsilon \frac{k_\Phi}{k_\Theta}}^{\text{Displacement}} + \overbrace{\theta \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) + \theta (UE - \delta) \frac{(1-u)}{f}}^{\text{New Firms}} \quad (8)$$

All else equal, our parameter estimates show that a drop in the EE firm mobility rate by 10% (by 0.003) affects output growth by 0.00183 percentage points (or 6% of the estimated aggregate average growth rate). These growth shares depend on the relative productivity distribution parameters $\frac{k_\Phi}{k_\Theta}$. However, quantitatively, we find that the growth decomposition does not vary much with these estimates over the economically relevant range, as we show in Figure 9. Overall, we find that worker mobility accounts for over 60% for the majority of economic growth, and that mobility and innovation account for the large majority of the contribution to growth. The first result finds resonance in Liu (2023). While featuring a different setting, Liu (2023) reports that worker mobility accounts for 61.3% of TPF growth.

Figure 9: Growth Decomposition



Notes: The figure shows a graphical representation of the the growth share due to worker mobility or innovation given $\frac{k_\Phi}{k_\Theta}$ together with the rest of the parameters space.

We can compare these findings to our empirical analysis through a variance decomposition of labor productivity growth across sectors. This analysis is shown in Table 4. At the cross-section of sectors, we find that the majority of productivity growth is accounted for by worker mobility and this especially so when considering worker mobility among the top ten percent of the income distribution. These results further lend support to our findings.

	Category of occupations	
	Bottom half	Top ten percent
Dep. var: productivity growth	(1)	(2)
Factor		
EE mobility	0.021** (48%)	0.132*** (69%)
R&D	0.008 (18%)	0.057*** (30%)
Covariance	0.015* (34%)	0.002 (1%)
Sum	0.044*	0.191***

Note: The table contains estimates of a variance composition of residual productivity growth on EE mobility, R&D and the covariance between these two factors. Residualization has been performed with respect to productivity, trade-shocks and firm size. Estimates in parentheses denote shares in percent. * denotes a p-value of less than 10 percent, ** less than 5 percent, and *** less than 1 percent.

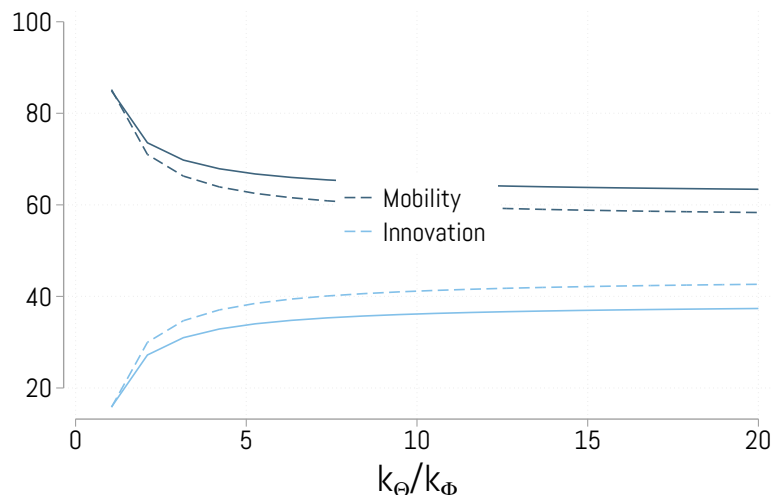
Table 4: Share of variation in productivity growth explained by mobility versus innovation.

5.3 Sub-sample Analysis

We now consider an application of our framework to the discussion of recent changes in economic growth determinants. A significant literature has documented a decline in rates of job creation and job destruction (Davis and Haltiwanger, 2014; Decker et al., 2016) and E2E mobility (Baksy et al., 2024; Hyatt and Spletzer, 2016; Fujita et al., Forthcoming) for the U.S. economy. Simultaneously, the literature has discussed a relative decline in R&D spending devoted to innovation - despite increases in research expenditures overall (Arora et al., 2020). While these facts have been observed above all for the U.S. economy, we find evidence for a small decline in our estimates of EE hiring rate at the firm level over our sample period in Sweden, cf. Figure 16 in the Appendix. Note that this estimate is constructed at the firm level, whereas the literature usually documents the job mobility level at the worker level.

We take this as motivation to undertake a sub-sample analysis with split year 2009, yielding a half sample split. Parameter estimates for the two samples are collected in Table 11 in the Appendix. We find that labor market mobility has slightly decreased whereas innovation intensity increased in our Swedish data. At the same time, estimates for the tail parameter θ and overall growth γ are found to be higher in the post as compared to the pre-period. Figure 10 shows that these estimates imply that labor mobility had less impact on aggregate growth in Sweden after 2009. Nevertheless, labor mobility accounts for the majority of economic growth over both sample periods.

Figure 10: Growth Decomposition - Sub-sample Analysis



Notes: The figure shows a graphical representation of the growth share due to worker mobility or innovation given $\frac{k_{\Theta}}{k_{\Phi}}$ together with the rest of the parameters space. The dashed line represents the decomposition for the period after 2009 whereas the solid line represents estimates before 2009.

6 Conclusion

In this paper, we have shown empirically and theoretically grounded evidence that worker mobility affects firm growth. We have proceeded two-fold with our analysis. First, using highly granular data for workers and firms in Sweden, we provide aggregate and microeconomic evidence for the correlation of worker mobility and growth in labor productivity, both for horizontal and vertical productivity growth. At the aggregate level, we find suggestive evidence that both worker mobility as well as R&D shape firm productivity growth. Second, we develop a random search model on a balanced growth path to estimate the relative impact of worker mobility and R&D for aggregate productivity growth. As in our empirical evidence, we find that both channels matter for growth. Crucially - and intuitively - the rate of worker mobility conditions the efficiency of worker mobility for aggregate growth.

Our results have important implications for understanding productivity growth, especially in light of decreasing mobility of workers across space and firms in recent decades and differences in worker mobility across countries. All else equal, our model predicts falling aggregate productivity growth in the presence of reduced worker mobility. This has important implications for policy makers. In fact, employment protection legislation that reduces labor mobility can therefore have an aggregate effect on labor productivity, even beyond their effect

on firm incentives for R&D as studied in [Aghion et al. \(2023\)](#).

Appendix A Online Appendix

The following online appendix assembles details for the derivations in the theoretical section (cf. section A.1) as well as additional details on the data set (cf. section A.2) and empirical evidence (cf. section A.3).

A.1 Derivations

A.1.1 Derivation Continuous Time Bellman Equation Joint Value

Time is indexed by $t, t + \Delta, \dots$. The discount factor between two periods is denoted as $(1 - \Delta r)$. The discrete time Bellman equation is

$$\begin{aligned}
 \Omega(P, N, t) = & \Delta Y(P, N, t) + (1 - \Delta r)[\\
 & \text{(EU Mobility)} + \Delta \delta \left(U(t + \Delta) + \Omega(\tilde{P}, N - 1, t + \Delta) \right) \\
 & \text{(UE Mobility)} + (1 - \Delta \delta) \Delta \lambda \left(\int_P^\infty \Omega(P', N + 1, t + \Delta) dF(P', t) + \int_{\underline{P}}^P \Omega(P, N + 1, t + \Delta) dF(P', t) \right) \\
 & - (1 - \Delta \delta) \Delta \lambda U(t + \Delta) \\
 & \text{(Innovation)} + (1 - \Delta \delta) (1 - \Delta \lambda) \Delta \beta \left(\int_P^\infty \Omega(P', N, t + \Delta) dV(P, t) + \int_{\underline{P}}^P \Omega(P, N, t + \Delta) dV(P, t) \right) \\
 & \text{(No change)} + (1 - \Delta \delta) (1 - \Delta \lambda) (1 - \Delta \beta) \Omega(P, N, t + \Delta)] \tag{9}
 \end{aligned}$$

where $\tilde{P} = \alpha P + \underline{P}(1 - \alpha)$. Note that

$$\begin{aligned}
 \Omega(P', N + 1, t + \Delta) &= \Omega(P', N + 1, t + \Delta) - \Omega(P, N + 1, t + \Delta) \\
 &+ \Omega(P, N + 1, t + \Delta) - \Omega(P, N, t + \Delta) \\
 &+ \Omega(P, N, t + \Delta) \\
 \Omega(P, N + 1, t + \Delta) &= \Omega(P, N + 1, t + \Delta) - \Omega(P, N, t + \Delta) + \Omega(P, N, t + \Delta) \\
 \Omega(\tilde{P}, N - 1, t + \Delta) &= \Omega(\tilde{P}, N - 1, t + \Delta) - \Omega(P, N - 1, t + \Delta) \\
 &+ \Omega(P, N - 1, t + \Delta) - \Omega(P, N, t + \Delta) + \Omega(P, N, t + \Delta)
 \end{aligned}$$

Using the substitutions $\Omega_{N+1} := \Omega(P, N + 1, t + \Delta) - \Omega(P, N, t + \Delta)$, $\Omega_{t+\Delta} := \Omega(P, N, t + \Delta) - \Omega(P, N, t)$ and $\Omega_{P',P,N} := \Omega(P', N, t + \Delta) - \Omega(P, N, t + \Delta)$, we can rewrite

$$\begin{aligned}\Omega(P', N + 1, t + \Delta) - \Omega(P, N, t) &= \Omega_{P',P,N+1} + \Omega_{N+1} + \Omega_{t+\Delta} \\ \Omega(P, N + 1, t + \Delta) - \Omega(P, N, t) &= \Omega_{N+1} + \Omega_{t+\Delta} \\ \Omega(\tilde{P}, N - 1, t + \Delta) &= \Omega_{\tilde{P},P,N-1} + \Omega_{N-1} + \Omega_{t+\Delta}\end{aligned}$$

We subtract $(1 - \Delta r)\Omega(P, N, t)$ from both sides of equation 9 and use the substitutions, yielding

$$\begin{aligned}\Delta r\Omega(P, N, t) &= \Delta Y(P, N, t) + (1 - \Delta r)[\\ (EU \text{ Mobility}) &+ \Delta\delta (U(t + \Delta) + \Omega_{\tilde{P},P,N-1} + \Omega_{N-1} + \Omega_{t+\Delta}) \\ (UE \text{ Mobility}) &+ (1 - \Delta\delta)\Delta\lambda (\Omega_{N+1} - U(t + \Delta) + \Omega_{t+\Delta}) \\ &+ (1 - \Delta\delta)\Delta\lambda \left(\int_P^\infty \Omega_{P',P,N+1} dF(P', t) \right) \\ (\text{Innovation}) &+ (1 - \Delta\delta)(1 - \Delta\lambda)\Delta\beta \left(\int_P^\infty \Omega_{P',P,N} dV(P', t) + \Omega_{t+\Delta} \right) \\ (\text{No change}) &+ (1 - \Delta\delta)(1 - \Delta\lambda)(1 - \Delta\beta)\Omega_{t+\Delta}\end{aligned}$$

We divide by Δ and take the limit when Δ goes to zero

$$\begin{aligned}r\Omega(P, N, t) &= Y(P, N, t) + \Omega_t \\ (EU \text{ Mobility}) &+ \delta (U(t) + \Omega_{\tilde{P},P,N-1} + \Omega_{N-1}) \\ (UE \text{ Mobility}) &+ \lambda \left(\Omega_{N+1} - U(t) + \int_P^\infty \Omega_{P',P,N+1} dF(P', t) \right) \\ (\text{Innovation}) &+ \beta \int_P^\infty \Omega_{P',P,N} dV(P', t)\end{aligned}$$

with $\Omega_t := \lim_{\Delta \rightarrow 0} \frac{\Omega(P, N, t + \Delta) - \Omega(P, N, t)}{\Delta}$. Note that we can similarly derive the value for an unemployed worker from the discrete-time value function

$$\begin{aligned}U(t) &= b(t)\Delta + (1 - \Delta r) (\Delta\lambda U(t + \Delta) + (1 - \Delta\lambda)U(t + \Delta)) \\ &= b(t)\Delta + (1 - \Delta r)U(t + \Delta)\end{aligned}$$

we subtract $(1 - \Delta r)U(t)$ and take the limit, yielding

$$rU(t) = b(t) + U_t$$

with $U_t := \lim_{\Delta \rightarrow 0} \frac{U(t+\Delta) - U(t)}{\Delta}$

A.1.2 Surplus representation

We aim at representing the joint value function in form of the surplus equation. To do this, we restart with the discrete time representation of the joint value equation, equation 9. Note that $\Omega(P, N, t) := S(P, N, t) + NU(t)$. We define the substitutions $S_N := S(P, N, t + \Delta) - S(P, N - 1, t + \Delta)$, $S_{t+\Delta} := S(P, N, t + \Delta) - S(P, N, t)$, $S_{P', P, N} := S(P', N, t + \Delta) - S(P, N, t + \Delta)$, $U_{t+\Delta} = U(t + \Delta) - U(t)$ and rewrite the following expressions

$$\begin{aligned} \Omega(P', N + 1, t + \Delta) - \Omega(P, N, t) &= S(P', N + 1, t + \Delta) - S(P, N + 1, t + \Delta) \\ &\quad + S(P, N + 1, t + \Delta) - S(P, N, t + \Delta) \\ &\quad + S(P, N, t + \Delta) + (N + 1)U(t + \Delta) \\ &\quad - S(P, N, t) - NU(t) \\ &= S_{P', P, N+1} + S_{N+1} + S_{t+\Delta} + NU_{t+\Delta} + U(t + \Delta) \\ \Omega(P', N, t + \Delta) - \Omega(P, N, t) &= S(P', N, t + \Delta) - S(P, N, t + \Delta) \\ &\quad + S(P, N, t + \Delta) + NU(t + \Delta) - S(P, N, t) - NU(t) \\ &= S_{P', P, N} + S_{t+\Delta} + NU_{t+\Delta} \\ \Omega(P, N + 1, t + \Delta) - \Omega(P, N, t) &= S(P, N + 1, t + \Delta) - S(P, N, t + \Delta) + S(P, N, t + \Delta) \\ &\quad + (N + 1)U(t + \Delta) - S(P, N, t) - NU(t) \\ &= S_{N+1} + S_{t+\Delta} + NU_{t+\Delta} + U(t + \Delta) \\ \Omega(\tilde{P}, N - 1, t + \Delta) - \Omega(P, N, t) &= S(\tilde{P}, N - 1, t + \Delta) - S(P, N - 1, t + \Delta) \\ &\quad + S(P, N - 1, t + \Delta) - S(P, N, t + \Delta) \\ &\quad + S(P, N, t + \Delta) + (N - 1)U(t + \Delta) - S(P, N, t) - NU(t) \\ &= S_{\tilde{P}, P, N-1} + S_{N-1} + S_{t+\Delta} + NU_{t+\Delta} - U(t + \Delta) \end{aligned}$$

We subtract $(1 - \Delta r)\Omega(P, N, t)$ from both sides of equation 9 and use the substitutions, yielding

$$\begin{aligned} \Delta r(S(P, N, t) + NU(t)) &= \Delta Y(P, N, t) + (1 - \Delta r)[\\ &\quad (EU \text{ Mobility}) + \Delta\delta (S_{\bar{P}, P, N-1} + S_{N-1} + S_{t+\Delta} + NU_{t+\Delta}) \\ &\quad (UE \text{ Mobility}) + (1 - \Delta\delta)\Delta\lambda \left(S_{N+1} + S_{t+\Delta} + NU_{t+\Delta} + \int_P^\infty S_{P', P, N+1} dF(P', t) \right) \\ &\quad (\text{Innovation}) + (1 - \Delta\delta)(1 - \Delta\lambda)\Delta\beta \left(S_{t+\Delta} + NU_{t+\Delta} + \int_P^\infty S_{P', P, N} dV(P', t) \right) \\ &\quad (\text{No change}) + (1 - \Delta\delta)(1 - \Delta\lambda)(1 - \Delta\beta) (S_{t+\Delta} + NU_{t+\Delta}) \end{aligned}$$

We divide by Δ and take the limit when Δ goes to zero. We also use the equation for the value of unemployment and denote $R(P, N, t) = (P - b(t))N$

$$\begin{aligned} rS(P, N, t) &= R(P, N, t) + S_t \\ &\quad (EU \text{ Mobility}) + \delta (S_{\bar{P}, P, N-1} + S_{N-1}) \\ &\quad (UE \text{ Mobility}) + \lambda \left(S_{N+1} + \int_P^\infty S_{P', P, N+1} dF(P', t) \right) \\ &\quad (\text{Innovation}) + \beta \int_P^\infty S_{P', P, N} dV(P', t) \end{aligned}$$

with $S_t := \lim_{\Delta \rightarrow 0} \frac{S(P, N, t+\Delta) - S(P, N, t)}{\Delta}$

A.1.3 Affine surplus representation

We will proceed by guess and verify. We guess the affine surplus representation $S(P, N, t) = N\hat{S}(P, t) + S^0(P, t)$ for the surplus equation

$$\begin{aligned} rS(P, N, t) &= R(P, N, t) + S_t + (\lambda - \delta) S_N + \delta S_{\bar{P}, P, N-1} \\ &\quad + \lambda \int_P^\infty S_{P', P, N+1} dF(P', t) + \beta \int_P^\infty S_{P', P, N} dV(P', t) \end{aligned} \quad (10)$$

Using the guess, define and express the following short-hands

$$\begin{aligned}
S_N &:= S(P, N, t) - S(P, N - 1, t) = \hat{S}(P, t) = S_{N+1} = -S_{N-1} \\
S_t &:= \lim_{\Delta \rightarrow 0} \frac{S(P, N, t + \Delta) - S(P, N, t)}{\Delta} = N\hat{S}_t(P, t) + S_t^0(P, t) \\
S_{P', P, N} &:= S(P', N, t + \Delta) - S(P, N, t + \Delta) = N\hat{S}_{P', P}(P, t) + S_{P', P}^0(P, t)
\end{aligned}$$

with the corresponding substitutions $\hat{S}_t := \lim_{\Delta \rightarrow 0} \frac{\hat{S}(P, t + \Delta) - \hat{S}(P, t)}{\Delta}$, $\hat{S}_{P', P} := \hat{S}(P', t) - \hat{S}(P, t)$, $S_t^0 := \lim_{\Delta \rightarrow 0} \frac{S^0(P, t + \Delta) - S^0(P, t)}{\Delta}$, $S_{P', P}^0 := S^0(P', t) - S^0(P, t)$. Note in particular that $S_{N+1} = -S_{N-1}$. We verify the initial guess by using the differenced surplus equation ($rS(P, N, t) - rS(P, N - 1, t)$) to obtain the implicit equations that define $\hat{S}(P, t)$ and $S^0(P, t)$. From

$$rS(P, N, t) - rS(P, N - 1, t) = rS_N = r\hat{S}(P, t)$$

we obtain

$$r\hat{S}(P, t) = (P - b(t)) + \hat{S}_t(P, t) + \delta\hat{S}_{\bar{P}, P} + \lambda \int_P^\infty \hat{S}_{P', P} dF(P', t) + \beta \int_P^\infty \hat{S}_{P', P} dV(P', t)$$

Using the surplus equation 10, we now back out the equation defining $S^0(P, t)$

$$\begin{aligned}
rN\hat{S}(P, t) + rS^0(P, t) &= N \left((P - b(t)) + \hat{S}_t(P, t) \right) \\
&+ N \left(\delta\hat{S}_{\bar{P}, P} + \lambda \int_P^\infty \hat{S}_{P', P} dF(P', t) + \beta \int_P^\infty \hat{S}_{P', P} dV(P', t) \right) + rS^0(P, t) \\
&= R(P, N, t) + S_t + (\lambda - \delta) S_N + \delta S_{\bar{P}, P, N-1} \\
&+ \lambda \int_P^\infty S_{P', P, N+1} dF(P', t) + \beta \int_P^\infty S_{P', P, N} dV(P', t)
\end{aligned}$$

Hence,

$$\begin{aligned}
rS^0(P, t) &= S_t^0(P, t) + (\lambda - \delta) \hat{S}(P, t) + \delta \left(S_{\bar{P}, P}^0 - \hat{S}_{\bar{P}, P} \right) \\
&+ \lambda \int_P^\infty \left(\hat{S}_{P', P} + S_{P', P}^0 \right) dF(P', t) + \beta \int_P^\infty S_{P', P}^0 dV(P', t)
\end{aligned}$$

A.1.4 Derivations Distributions Balanced Growth Path

To show that we can represent the surplus function on the balanced growth path, we rewrite the equation

$$\begin{aligned} rS(P, N, t) &= R(P, N, t) + S_t + (\lambda - \delta) S_N + \delta S_{\tilde{P}, P, N-1} \\ &\quad + \lambda \int_P^\infty S_{P', P, N+1} dF(P', t) + \beta \int_P^\infty S_{P', P, N} dV(P', t) \end{aligned}$$

On the BGP, where

$$\begin{aligned} F(P, t) &= \Phi(Pe^{-\gamma t}) \\ G(P, t) &= \Theta(Pe^{-\gamma t}) \\ V(P, t) &= \Upsilon(Pe^{-\gamma t}) \\ S(P, N, t) &= e^{\gamma t} \sigma(Pe^{-\gamma t}, N) \\ &= e^{\gamma t} (N \hat{\sigma}(Pe^{-\gamma t}) + \sigma^0(Pe^{-\gamma t})) \\ f(P, t) &= e^{-\gamma t} \Phi'(Pe^{-\gamma t}) \\ v(P, t) &= e^{-\gamma t} \Upsilon'(Pe^{-\gamma t}) \\ b(t) &= e^{\gamma t} b \end{aligned}$$

such that

$$\begin{aligned} S_N &:= S(P, N, t) - S(P, N-1, t) = e^{\gamma t} (\sigma(Pe^{-\gamma t}, N) - \sigma(Pe^{-\gamma t}, N-1)) := e^{\gamma t} \sigma_N \\ S_t &:= \lim_{\Delta} \frac{S(P, N, t+\Delta) - S(P, N, t)}{\Delta} = e^{\gamma t} \left(\lim_{\Delta} \frac{\sigma(Pe^{-\gamma t+\Delta}, N) - \sigma(Pe^{-\gamma t}, N)}{\Delta} \right) \\ &:= e^{\gamma t} \sigma_t \\ S_{\tilde{P}, P, N-1} &:= S(\tilde{P}, N-1, t) - S(P, N-1) = e^{\gamma t} (\sigma(\tilde{P}e^{-\gamma t}, N-1) - \sigma(Pe^{-\gamma t}, N-1)) \\ &:= e^{\gamma t} \sigma_{\tilde{P}, P, N-1} \\ S_{P', P, N} &:= S(P', N, t) - S(P, N, t) = e^{\gamma t} (\sigma(P'e^{-\gamma t}, N) - \sigma(Pe^{-\gamma t}, N)) \end{aligned}$$

Plugging into the surplus equation and making the substitution $x = Pe^{-\gamma t}$

$$\begin{aligned}
rS(P, N, t) &= R(P, N, t) + S_t + (\lambda - \delta) S_N + \delta S_{\bar{P}, P, N-1} \\
&\quad + \lambda \int_P^\infty S_{P', P, N+1} dF(P', t) + \beta \int_P^\infty S_{P', P, N} dV(P', t)
\end{aligned}$$

such that

$$\begin{aligned}
re^{\gamma t} \sigma(Pe^{-\gamma t}, N) &= (x - b)e^{\gamma t} N + e^{\gamma t} \sigma_t + (\lambda - \delta) e^{\gamma t} \sigma_N + \delta e^{\gamma t} \sigma_{\bar{x}, x, N-1} \\
&\quad + \lambda \int_P^\infty e^{\gamma t} \sigma_{x', x, N+1} e^{-\gamma t} \Phi'(x) dx e^{\gamma t} + \beta \int_P^\infty e^{\gamma t} \sigma_{x', x, N} e^{-\gamma t} \Upsilon'(x) dx e^{\gamma t}
\end{aligned}$$

With simplification, yielding

$$\begin{aligned}
r\sigma(x, N) &= (x - b)N + \sigma_t + (\lambda - \delta) \sigma_N + \delta \sigma_{\bar{x}, x, N-1} \\
&\quad + \lambda \int_P^\infty \sigma_{x', x, N+1} \Phi'(x) dx + \beta \int_P^\infty \sigma_{x', x, N} \Upsilon'(x) dx
\end{aligned}$$

We hence find the surplus equation independent of time.

A.1.5 Derivations Distributions Balanced Growth Path

Using the balanced growth path distributions such that

$$\begin{aligned}
\frac{\partial f(P, t)}{\partial t} &= -\gamma e^{-\gamma t} \Phi'(ze^{-\gamma t}) - z\gamma(e^{-\gamma t})^2 \Phi''(ze^{-\gamma t}) \\
\frac{\partial g(P, t)}{\partial t} &= -\gamma e^{-\gamma t} \Theta'(ze^{-\gamma t}) - z\gamma(e^{-\gamma t})^2 \Theta''(ze^{-\gamma t})
\end{aligned}$$

we can derive the productivity distribution of the unemployed workers and the distribution of firms.

Distribution of the unemployed Starting from the equation for the change in the distribution of the unemployed

$$\delta g(P, t) \eta_p + \mu_w w(P, t) \frac{1}{u} - \lambda f(P, t) \eta_{IJ} = \frac{\partial f(P, t)}{\partial t}$$

where $\eta_{IJ} = \frac{N_t^J}{u_t N_t^I}$ we obtain by plugging in

$$e^{-\gamma t} \left(\delta \Theta'(ze^{-\gamma t}) \eta_p + \frac{\mu_w}{u} \Pi'(ze^{-\gamma t}) - \lambda \Phi'(ze^{-\gamma t}) \eta_p \right) = e^{-\gamma t} \left(-\gamma \Phi'(ze^{-\gamma t}) - z\gamma(e^{-\gamma t}) \Phi''(ze^{-\gamma t}) \right)$$

$$\lambda - \delta \frac{\Theta'(ze^{-\gamma t})}{\Phi'(ze^{-\gamma t})} + \frac{\mu_w}{N^J/N^I} \frac{\Pi'(ze^{-\gamma t})}{\Phi'(ze^{-\gamma t})} = \frac{1}{\eta_{IJ}} \gamma \left(1 + \frac{z(e^{-\gamma t}) \Phi''(ze^{-\gamma t})}{\Phi'(ze^{-\gamma t})} \right)$$

Using $x = ze^{-\gamma t}$

$$\frac{\lambda}{\delta} - \frac{\gamma/\eta_{IJ}}{\delta} \left(1 + \frac{x\Phi''(x)}{\Phi'(x)} \right) = \frac{\Theta'(x)}{\Phi'(x)} - \frac{\mu_w}{\delta} \frac{N^I}{N^J} \frac{\Pi'(x)}{\Phi'(x)}$$

Leveraging assumptions 1 and 2, we take the limit such that $\lim_{x \rightarrow \infty} \frac{x\Phi''(x)}{\Phi'(x)} = -\frac{(\theta+1)}{\theta}$. We also use that $\lim_{x \rightarrow \infty} \frac{\Theta'(x)}{\Phi'(x)} = \frac{k_\Theta}{k_\Phi}$ and $\lim_{x \rightarrow \infty} \frac{\Pi'(x)}{\Phi'(x)} = \alpha_\Pi$ We obtain

$$\frac{(\lambda + \frac{\gamma}{\eta_p \theta})}{\delta} = \frac{k_\Theta}{k_\Phi} - \frac{\mu_w}{\delta} \frac{N_0^I}{N_0^J} \alpha_\Pi$$

Distribution of firm productivity From

$$\lambda (f(P, t)G(P, t) - g(P, t)\bar{F}(P, t)) + \beta (v(P, t)G(P, t) - g(P, t)\bar{V}(P, t)) + \mu_f g(P, t) + \delta \left(g\left(\frac{P - (1 - \alpha)\underline{P}_t}{\alpha}, t\right) - g(P, t) \right) = \frac{\partial g(P, t)}{\partial t}$$

we obtain by plugging in

$$\begin{aligned} & e^{-\gamma t} \lambda (\Phi'(ze^{-\gamma t})\Theta(ze^{-\gamma t}) - \Theta'(ze^{-\gamma t})(1 - \Phi(ze^{-\gamma t}))) + \\ & e^{-\gamma t} \beta (\Upsilon'(ze^{-\gamma t})\Theta(ze^{-\gamma t}) - \Theta'(ze^{-\gamma t})(1 - V(ze^{-\gamma t}))) + \\ & + e^{-\gamma t} \left(\mu_f \Theta'(ze^{-\gamma t}) + \delta \left(\frac{1}{\alpha} \Theta' \left(\frac{z - (1 - \alpha)\underline{z}_t}{\alpha} e^{-\gamma t} \right) - \Theta'(ze^{-\gamma t}) \right) \right) \\ & = e^{-\gamma t} (-\gamma \Theta'(ze^{-\gamma t}) - z\gamma(e^{-\gamma t}) \Theta''(ze^{-\gamma t})) \end{aligned}$$

we express using $x = ze^{-\gamma t}$ and simplify

$$\begin{aligned} & \lambda \left(\frac{\Phi'(x)}{\Theta'(x)} \Theta(x) - (1 - \Phi(x)) \right) + \beta \left(\frac{\Upsilon'(x)}{\Theta'(x)} \Theta(x) - (1 - V(x)) \right) + \\ & + \left(\mu_f + \delta \left(\frac{\frac{1}{\alpha} \Theta' \left(\frac{x - (1-\alpha)\underline{X}_t}{\alpha} \right)}{\Theta'(x)} - 1 \right) \right) = -\gamma \left(1 + \frac{x\Theta''(x)}{\Theta'(x)} \right) \end{aligned}$$

We take limit, using $\lim_{x \rightarrow \infty} \frac{x\Phi''(x)}{\Phi'(x)} = -\frac{(\theta+1)}{\theta}$, $\lim_{x \rightarrow \infty} \frac{\frac{1}{\alpha} \Theta' \left(\frac{x - (1-\alpha)\underline{X}_t}{\alpha} \right)}{\Theta'(x)} = \alpha^{\frac{1-\theta}{\theta}} - 1$. We also use that $\lim_{x \rightarrow \infty} \frac{\Theta'(x)}{\Phi'(x)} = \frac{k_\Theta}{k_\Phi}$ and $\lim_{x \rightarrow \infty} \frac{\Upsilon'(x)}{\Theta'(x)} = \alpha \Upsilon \frac{k_\Phi}{k_\Theta}$

$$\lambda \frac{k_\Phi}{k_\Theta} + \beta \alpha \Upsilon \frac{k_\Phi}{k_\Theta} + \mu_f + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) = \gamma / \theta$$

A.1.6 Joint Value Function with Job-to-Job Mobility

In addition to the previous events discussed for the setting without job-to-job mobility, a firm experiences two more events, a EE Hire or an EE Exit.

- (*EE Hire*): The firm experiences the chance of meeting an employed worker at rate $s\lambda(1-u)$. If the worker is of higher productivity than the firm, the joint firm value increases to $\int_P^\infty \Omega(P', N+1, t+\Delta) dG(P', t)$, if the worker is not as productive, the value increases to $\int_{\underline{P}}^P \Omega(P, N+1, t+\Delta) dG(P', t)$. The worker firm coalition further sees drop in the value contribution at the sending firm of size $\int_{\underline{P}}^\infty \Omega(P', N'+1, t+\Delta) - \Omega(P', N', t+\Delta) dG(P', t)$, which is the value that the origin firm would be willing to pay to prevent the worker from leaving. Note that we are using the guess and verify approach such that $\Omega(P', N'+1, t+\Delta) - \Omega(P', N', t+\Delta)$ is independent of the sending firm size.
- (*EE Exit*): The firm has the chance that one of its workers is contacted by another firm at rate $\hat{\lambda}$. In that case, the firm does not experience a productivity disruption and keeps its value at $\Omega(P, N-1, t+\Delta)$, the worker keeps its productivity at P . At the new firm, the worker is offered the maximum marginal value that can be offered at the origin firm $\Omega(P, N, t+\Delta) - \Omega(P, N-1, t+\Delta) = \Omega_N(P, N, t)$. Hence, total value at the origin firm is changed to $\Omega(P, N, t+\Delta)$.

We can hence write the discrete time value function in an interval Δ as

$$\begin{aligned}
& \Omega(P, N, t) = \Delta Y(P, N) + (1 - \Delta r)[\\
& \text{(EU Mobility)} + \Delta \delta \left(U(P) + \Omega(\tilde{P}, N - 1, t + \Delta) \right) \\
& \text{(UE Mobility)} + (1 - \Delta \delta) \Delta \lambda u \left(\int_P^\infty \Omega(P', N + 1, t + \Delta) dF(P', t) \right) \\
& \quad + (1 - \Delta \delta) \Delta \lambda u \left(\int_{\underline{P}}^P \Omega(P, N + 1, t + \Delta) dF(P', t) - \int_{\underline{P}}^\infty U(P') dF(P', t) \right) \\
& \text{(EE Hire)} + (1 - \Delta \delta) \Delta \lambda (1 - u) \left(\int_P^\infty \Omega(P', N + 1, t + \Delta) dG(P', t) \right) \\
& \quad + (1 - \Delta \delta) \Delta \lambda (1 - u) \left(\int_{\underline{P}}^P \Omega(P, N + 1, t + \Delta) dG(P', t) \right) \\
& \quad + (1 - \Delta \delta) \Delta \lambda (1 - u) \left(- \int_{\underline{P}}^\infty (\Omega(P', N' + 1, t + \Delta) - \Omega(P', N', t + \Delta)) dG(P', t) \right) \\
& \text{(EE Exit)} + (1 - \Delta \delta) (1 - \Delta \lambda) \Delta \hat{\lambda} (\Omega(P, N, t + \Delta)) \\
& \text{(Innovation)} + (1 - \Delta \delta) (1 - \Delta \lambda) (1 - \Delta \hat{\lambda}) \Delta \beta \left(\int_P^\infty \Omega(P', N, t + \Delta) dV(P', t) \right) \\
& \quad + (1 - \Delta \delta) (1 - \Delta \lambda) (1 - \Delta \hat{\lambda}) \Delta \beta \left(\int_{\underline{P}}^P \Omega(P, N, t + \Delta) dV(P', t) \right) \\
& \text{(No change)} + (1 - \Delta \delta) (1 - \Delta \lambda) (1 - \Delta \hat{\lambda}) (1 - \Delta \beta) \Omega(P, N, t + \Delta)]
\end{aligned}$$

where $\tilde{P} = \alpha P + \underline{P}(1 - \alpha)$. Using the same steps as in appendix section [A.1.1](#) for the case without EE mobility, we obtain

$$\begin{aligned}
& r\Omega(P, N, t) = Y(P, N, t) + \Omega_t \\
& \text{(EU Mobility)} + \delta \left(U(t) + \Omega_{\tilde{P}, P, N-1} + \Omega_{N-1} \right) \\
& \text{(UE Mobility)} + \lambda u \left(\Omega_{N+1} - U(t) + \int_P^\infty \Omega_{P', P, N+1} dF(P', t) \right) \\
& \text{(EE Hire)} + \lambda (1 - u) \left(\Omega_{N+1} + \int_P^\infty \Omega_{P', P, N+1} dG(P', t) - \int_{\underline{P}}^\infty \Omega_{P', N'} dG(P', t) \right) \\
& \text{(Innovation)} + \beta \int_P^\infty \Omega_{P', P, N} dV(P', t)
\end{aligned}$$

where $\Omega_{P', N'} := \Omega(P', N' + 1, t + \Delta) - \Omega(P', N', t + \Delta)$. We can compare this to the situation without EE mobility, and we find that we are having two additional terms due to EE Hires. Note also that the value function is independent of $\hat{\lambda}$ as mobility leaves the joint surplus

unaffected.

A.1.7 Affine surplus representation with with Job-to-Job Mobility

We will proceed by guess and verify. We guess the affine surplus representation $S(P, N, t) = N\hat{S}(P, t) + S^0(P, t)$ for the surplus equation

$$\begin{aligned}
& rS(P, N, t) = N(P - b(t)) + S_t \\
& \text{(EU Mobility)} + \delta(-S_N + S_{\hat{P}, P, N-1}) \\
& \text{(Mobility)} + \lambda \left(u_t \int_P^\infty S_{P', P, N+1} dF(P', t) + s(1 - u_t) \int_P^\infty S_{P', P, N+1} dG(P', t) \right) \\
& \quad + \lambda \left(S_N - s(1 - u_t) \int_{\underline{P}}^\infty S_{N'}(P', t) dF(P', t) \right) \\
& \text{(Innovation)} + \beta \int_P^\infty S_{P', P, N} dV(P', t)
\end{aligned}$$

Using the guess, define and express the following short-hands

$$\begin{aligned}
S_N & := S(P, N, t) - S(P, N - 1, t) = \hat{S}(P, t) = S_{N+1} = -S_{N-1} \\
S_t & := \lim_{\Delta \rightarrow 0} \frac{S(P, N, t + \Delta) - S(P, N, t)}{\Delta} = N\hat{S}_t(P, t) + S_t^0(P, t) \\
S_{P', P, N} & := S(P', N, t + \Delta) - S(P, N, t + \Delta) = N\hat{S}_{P', P}(P, t) + S_{P', P}^0(P, t)
\end{aligned}$$

with the corresponding substitutions $\hat{S}_t := \lim_{\Delta \rightarrow 0} \frac{\hat{S}(P, t + \Delta) - \hat{S}(P, t)}{\Delta}$, $\hat{S}_{P', P} := \hat{S}(P', t) - \hat{S}(P, t)$, $S_t^0 := \lim_{\Delta \rightarrow 0} \frac{S^0(P, t + \Delta) - S^0(P, t)}{\Delta}$, $S_{P', P}^0 := S^0(P', t) - S^0(P, t)$. Note in particular that $S_{N+1} = -S_{N-1}$. We verify the initial guess by using the differenced surplus equation ($rS(P, N, t) - rS(P, N - 1, t)$) to obtain the implicit equations that define $\hat{S}(P, t)$ and $S^0(P, t)$. From

$$rS(P, N, t) - rS(P, N - 1, t) = rS_N = r\hat{S}(P, t)$$

we obtain

$$\begin{aligned}
r\hat{S}(P, t) & = (P - b(t)) + \hat{S}_t(P, t) + \delta\hat{S}_{\hat{P}, P} + \beta \int_P^\infty \hat{S}_{P', P} dV(P', t) \\
& \quad + \lambda \left(u_t \int_P^\infty \hat{S}_{P', P} dF(P', t) + s(1 - u_t) \int_P^\infty \hat{S}_{P', P} dG(P', t) \right)
\end{aligned}$$

Using the surplus equation 10, we now back out the equation defining $S^0(P, t)$

$$\begin{aligned}
rN\hat{S}(P, t) + rS^0(P, t) &= N \left((P - b(t)) + \hat{S}_t(P, t) \right) \\
&+ N \left(\delta \hat{S}_{\tilde{P}, P} + \beta \int_P^\infty \hat{S}_{P', P} dV(P', t) \right) + rS^0(P, t) \\
&+ N\lambda \left(u_t \int_P^\infty \hat{S}_{P', P} dF(P', t) + s(1 - u_t) \int_P^\infty \hat{S}_{P', P} dG(P', t) \right) \\
&= R(P, N, t) + S_t + (\lambda - \delta) S_N + \delta S_{\tilde{P}, P, N-1} \\
&+ \beta \int_P^\infty S_{P', P, N} dV(P', t) \\
&+ \lambda \left(u_t \int_P^\infty S_{P', P, N+1} dF(P', t) + s(1 - u_t) \int_P^\infty S_{P', P, N+1} dG(P', t) \right) \\
&+ \lambda \left(-s(1 - u_t) \int_{\underline{P}}^\infty S_{N'}(P', t) dF(P', t) \right)
\end{aligned}$$

Hence,

$$\begin{aligned}
rS^0(P, t) &= S_t^0(P, t) + (\lambda - \delta) \hat{S}(P, t) + \delta \left(S_{\tilde{P}, P}^0 - \hat{S}_{\tilde{P}, P} \right) + \beta \int_P^\infty S_{P', P}^0 dV(P', t) \\
&+ \lambda u_t \int_P^\infty \left(\hat{S}_{P', P} + S_{P', P}^0 \right) dF(P', t) \\
&+ \lambda s(1 - u_t) \left(\int_P^\infty \left(\hat{S}_{P', P} + S_{P', P}^0 \right) dG(P', t) - \int_{\underline{P}}^\infty \hat{S}(P', t) dG(P', t) \right)
\end{aligned}$$

A.1.8 Additional Equilibrium Relationships

In addition to the aforementioned equilibrium relationships, we note a set of additional restrictions. The first equates search intensity by workers and firms, such that

$$\tilde{\lambda} = \lambda \frac{N^J}{N^I}$$

The second restrictions derives from the equilibrium in the pool of unemployed workers. For a constant unemployment rate, the outflows from unemployment (as the mass of unemployed workers finding new employment, right hand side) and inflows (as the mass of new job market entrants and displaced workers, left hand side) have to balance, such that

$$\mu_I N^I + \delta N^J = u N^I \tilde{\lambda}$$

Hence, $\mu_I = (u\lambda - \delta)\frac{N^J}{N^I}$. Finally, for a constant average firm size $\frac{N^I u}{N^J}$, we require $\mu_f = \mu_I$.

A.1.9 Estimation Equations

Given the two equilibrium equations

$$\begin{aligned}\frac{\lambda + \frac{\gamma}{\eta_P \theta}}{\delta} &= \frac{k_\Theta}{k_\Phi} - \frac{\mu_w}{\delta} \frac{N^I}{N^J} \alpha_\Pi \\ \frac{\gamma}{\theta} &= \lambda \left(\frac{k_\Phi}{k_\Theta} u + (1-u)s \right) + \beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta} + \mu_f + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right)\end{aligned}$$

and the relations $\mu_f = (\lambda u - \delta)\frac{N^J}{N^I} = \mu_I$, $\eta_P = \frac{N^J}{u N^I}$, $\mu_w = \frac{\mu_f}{u}$, we rewrite the first equation as

$$\begin{aligned}\frac{\gamma}{\eta_P \theta} &= \delta \frac{k_\Theta}{k_\Phi} - \lambda - \frac{\mu_f}{u} \frac{N^I}{N^J} \alpha_\Pi \\ \frac{\gamma}{\theta} &= \frac{N^J}{u N^I} \left(\delta \frac{k_\Theta}{k_\Phi} - \lambda - \frac{(\lambda u - \delta)}{u} \alpha_\Pi \right)\end{aligned}$$

We rewrite the second equation as

$$\frac{\gamma}{\theta} = u\lambda \frac{k_\Phi}{k_\Theta} + (1-u)s\lambda + \beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta} + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) + (\lambda u - \delta) \frac{N^J}{N^I}$$

We observe the following mapping to estimated quantities

- probability of new hire from employment: $(1-u)s\lambda = EE$
- probability of new hire from unemployment $u\lambda = UE$
- average firm size $\frac{(1-u)N^I}{N^J} = f$
- estimates of $\frac{k_\Phi}{k_\Theta}$, $\beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta}$, $\delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right)$, δ

Using these short hands,

$$\begin{aligned}\frac{\gamma}{\theta} &= UE \frac{k_\Phi}{k_\Theta} + EE + \beta \alpha_\Upsilon \frac{k_\Phi}{k_\Theta} + \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1 \right) + (UE - \delta) \frac{(1-u)}{f} \\ \frac{\gamma}{\theta} &= \frac{(1-u)}{uf} \left(\delta \frac{k_\Theta}{k_\Phi} - \frac{((UE - \delta)\alpha_\Pi + UE)}{u} \right)\end{aligned}$$

From these equations, we find relative efficiencies $\alpha_\Upsilon, \alpha_\Pi$ as

$$\alpha_\Upsilon = \frac{\left(\frac{\gamma}{\theta} - UE \frac{k_\Phi}{k_\Theta} - EE - \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1\right) - (UE - \delta) \frac{(1-u)}{f}\right)}{\beta \frac{k_\Phi}{k_\Theta}}$$

$$\alpha_\Pi = \frac{\delta \frac{k_\Theta u}{k_\Phi} - \frac{\gamma u^2 f}{\theta(1-u)} - UE}{(UE - \delta)}$$

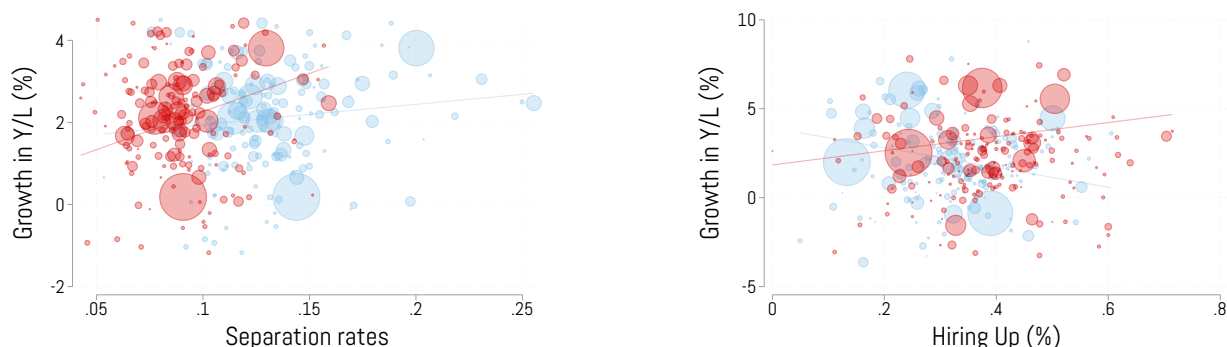
A.2 Data Overview

Data Set	Period	Variables
Worker data – Swedish Longitudinal Integrated Database for Health Insurance and Labour Market Studies (LISA, Longitudinell Integrationsdatabas för Sjukförsäkrings- och Arbetsmarknadsstudier)	1990-2019	worker id, firm id, age, year of graduation, gender, income, year, occupation, education
Firm data (Företagens Ekonomi)	1997-2019	firm id, firm size, value added, output, capital, year, industry
Customs data (Utrikeshandel med varor)	1997-2019	firm id, export/import flow, value, quantity, year, country
Product data (Industrins Varuproduktion)	1997-2019	firm id, year, product code, value of production, quantity
Death data (National Board of Health and Welfare)	1997-2016	worker id, year, cause of death
R&D data (Research and Development survey in private sector)	1997-2019	firm id, year, R&D expenditure

Table 5: Variables across datasets

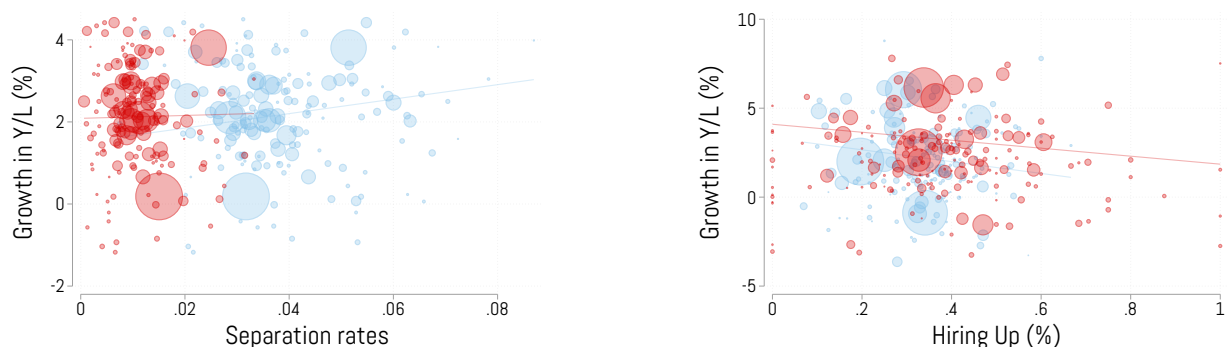
A.3 Regressions Motivation

Figure 11: Productivity growth and mobility (only EE mobility).



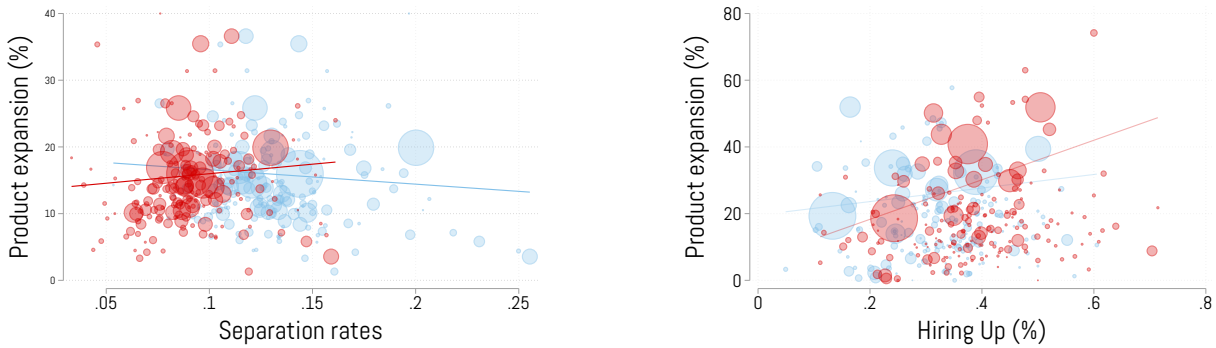
Notes: The left column shows binned scatter plots of the separation rate and the growth in labor productivity for occupations with below median wages (blue) and top decile occupations (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the growth in labor productivity for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry. Data for Sweden, 1997–2019.

Figure 12: Productivity growth and mobility (only EU or UE mobility).



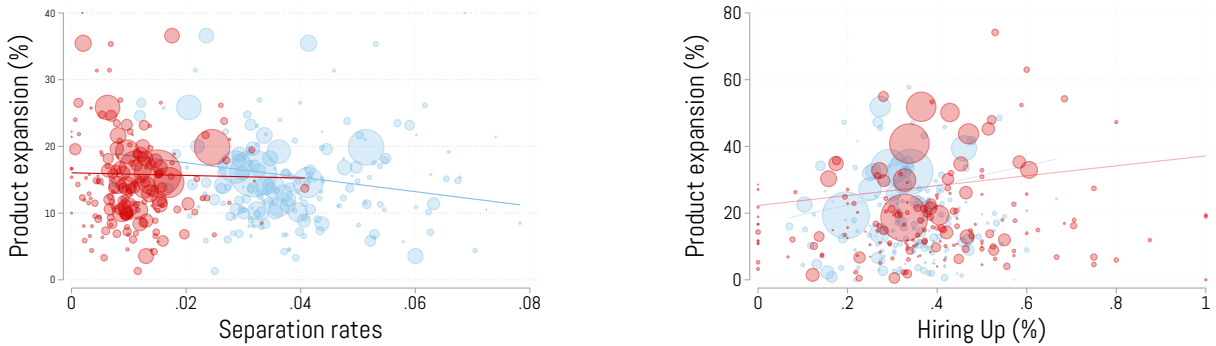
Notes: The left column shows binned scatter plots of the separation rate and the growth in labor productivity for occupations with below median wages (blue) and top decile occupations (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the growth in labor productivity for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry. Data for Sweden, 1997–2019.

Figure 13: Product expansion and mobility (only EE mobility).



Notes: The left panel shows binned scatter plots of the separation rate and the likelihood of product expansion for all workers (blue) and top decile occupations as categorized by average earnings (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the likelihood of product expansion for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry and products are denoted at 8-digit. Data for Sweden, 1997–2019.

Figure 14: Product expansion and mobility (only EU or UE mobility).



Notes: The left panel shows binned scatter plots of the separation rate and the likelihood of product expansion for all workers (blue) and top decile occupations as categorized by average earnings (red). The right hand side shows the share of workers who last worked at higher-productivity firms before entering the current firm and the likelihood of product expansion for these two types of workers. Ranking of firms is established in the year prior to mobility based on observed Y/L . A unit of observation is a 4-digit industry and products are denoted at 8-digit. Data for Sweden, 1997–2019.

Table 6: Regression Results - Labor Productivity

Dep. var.: Controls:	Growth in labor productivity					
	No controls		Y/L		Y/L + volatility	
	Bottom half	Top dec.	Bottom half	Top dec.	Bottom half	Top dec.
	(1)	(2)	(3)	(4)	(5)	(6)
Panel A						
Separation rate	0.04*	0.11***	0.10***	0.15***	0.05**	0.06
	(0.02)	(0.04)	(0.02)	(0.03)	(0.03)	(0.04)
Observations	171	171	171	171	170	170
Mean growth	0.02	0.02	0.02	0.02	0.02	0.02
Mean sep. rate	0.16	0.09	0.16	0.09	0.16	0.09
Panel B						
Hiring up	-0.06***	0.03**	-0.00	0.05***	0.03**	0.06***
	(0.02)	(0.02)	(0.01)	(0.01)	(0.01)	(0.01)
Observations	182	178	182	178	182	178
Mean growth	0.02	0.02	0.02	0.02	0.02	0.02
Mean hiring up	0.33	0.38	0.33	0.38	0.33	0.38
Controls						
Labor productivity			✓	✓	✓	✓
Sector sales volatility					✓	✓
Sector foreign demand volatility					✓	✓

Notes: The table shows regression estimates together with standard errors for the regression specification $\Delta P_{st} = \alpha_0 + Y_{st}\beta + X\Gamma_t + \epsilon_{st}$ where Y is either the separation rate or the share of hires from higher productivity firms. The unit of observation is a sector. The control vector X contains labor productivity, sales or foreign demand volatility, computed as sector average of firm-specific values.

Table 7: Regression Results - Product Expansion

Dep. var.: Controls:	Product expansion					
	No controls		Y/L		Y/L + volatility	
	Bottom half	Top dec.	Bottom half	Top dec.	Bottom half	Top dec.
	(1)	(2)	(3)	(4)	(5)	(6)
Panel A						
Separation rate	-0.23**	0.15	-0.09	0.30*	-0.46***	-0.12
	(0.10)	(0.17)	(0.11)	(0.16)	(0.12)	(0.20)
Observations	171	171	171	171	170	170
Mean product expansion	0.14	0.14	0.14	0.14	0.14	0.14
Mean sep. rate	0.16	0.09	0.16	0.09	0.16	0.094
Panel B						
Hiring up	0.22***	0.59***	0.25***	0.64***	0.243***	0.66***
	(0.08)	(0.10)	(0.08)	(0.10)	(0.09)	(0.101)
Observations	180	177	180	177	180	177
Mean product expansion	0.17	0.18	0.18	0.18	0.18	0.18
Mean hiring up	0.33	0.38	0.33	0.38	0.33	0.38
Controls						
Labor productivity			✓	✓	✓	✓
Sector sales volatility					✓	✓
Sector foreign demand volatility					✓	✓

Notes: The table shows regression estimates together with standard errors for the regression specification $\text{Product Exp.} = \alpha_0 + Y_{st}\beta + X\Gamma_t + \epsilon_{st}$ where Y is either the separation rate or the share of hires from higher productivity firms. The unit of observation is a sector. The control vector X contains labor productivity, sales or foreign demand volatility, computed as sector average of firm-specific values.

Table 8: Regression Results - Labor Productivity with Standardized Regressors and R&D

Dep. var.:	Growth in labor productivity					
	No controls		Y/L		Y/L + volatility	
	Bottom half	Top dec.	Bottom half	Top dec.	Bottom half	Top dec.
	(1)	(2)	(3)	(4)	(5)	(6)
Panel A						
Separation rate	0.002**	0.003***	0.004***	0.004***	0.001	0.002*
(standardized)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)
R&D activity	0.001	0.001	-0.002***	-0.003***	-0.002***	-0.003***
(standardized)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)	(0.001)
Observations	171	171	171	171	170	170
Mean growth	0.02	0.02	0.02	0.02	0.02	0.02
Mean sep. rate	0.162	0.09	0.16	0.09	0.16	0.09
Panel B						
Hiring up	-0.005***	0.006***	-0.001	0.006***	0.003*	0.008***
(standardized)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)	(0.002)
R&D activity	0.000	0.008***	-0.002	0.004***	0.001	0.005***
(standardized)	(0.002)	(0.002)	(0.002)	(0.001)	(0.002)	(0.001)
Observations	182	178	182	178	182	178
Mean growth	0.02	0.02	0.02	0.02	0.02	0.02
Mean hiring up	0.33	0.38	0.33	0.38	0.33	0.38
Controls						
Labor productivity			✓	✓	✓	✓
Sector sales volatility					✓	✓
Sector foreign demand volatility					✓	✓

Notes: The table shows regression estimates together with standard errors for the regression specification $\Delta P_{st} = \alpha_0 + Y_{st}\beta + X\Gamma_t + \epsilon_{st}$ where Y is either the standardized separation rate or the standardized share of hires from higher productivity firms. We also include the standardized R&D. The unit of observation is a sector. The control vector X contains labor productivity, sales or foreign demand volatility, computed as sector average of firm-specific values.

Table 9: Regression Results - Product Expansion with Standardized Regressors and R&D

Dep. var.:	Product expansion					
	No controls		Y/L		Y/L + volatility	
	Bottom half	Top dec.	Bottom half	Top dec.	Bottom half	Top dec.
Controls:	(1)	(2)	(3)	(4)	(5)	(6)
Panel A						
Separation rate	-0.000	0.007*	-0.000	0.007*	-0.014***	-0.004
(standardized)	(0.004)	(0.004)	(0.004)	(0.004)	(0.005)	(0.005)
R&D activity	0.016***	0.017***	0.017***	0.017***	0.015***	0.017***
(standardized)	(0.003)	(0.003)	(0.004)	(0.003)	(0.003)	(0.003)
Observations	171	171	171	171	170	170
Mean product expansion	0.14	0.14	0.14	0.14	0.14	0.14
Mean sep. rate	0.16	0.09	0.16	0.09	0.16	0.094
Panel B						
Hiring up	0.044***	0.083***	0.045***	0.083***	0.051***	0.088***
(standardized)	(0.008)	(0.010)	(0.008)	(0.010)	(0.009)	(0.010)
R&D activity	0.043***	0.070***	0.043***	0.065***	0.048***	0.066***
(standardized)	(0.009)	(0.009)	(0.009)	(0.009)	(0.009)	(0.009)
Observations	180	177	180	177	180	177
Mean product expansion	0.17	0.18	0.18	0.18	0.18	0.18
Mean hiring up	0.33	0.38	0.33	0.38	0.33	0.38
Controls						
Labor productivity			✓	✓	✓	✓
Sector sales volatility					✓	✓
Sector foreign demand volatility					✓	✓

Notes: The table shows regression estimates together with standard errors for the regression specification $\text{Product Exp.} = \alpha_0 + Y_{st}\beta + X\Gamma_t + \epsilon_{st}$ where Y is either the standardized separation rate or the standardized share of hires from higher productivity firms. We also include the standardized R&D. The unit of observation is a sector. The control vector X contains labor productivity, sales or foreign demand volatility, computed as sector average of firm-specific values.

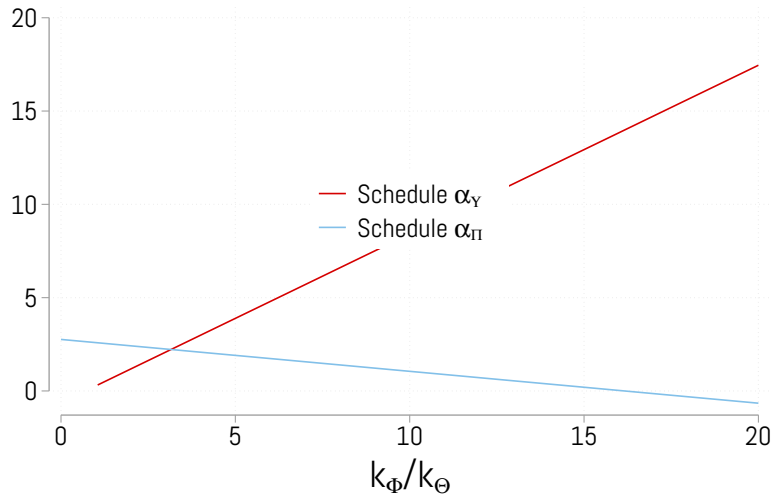
A.4 Estimation Result

Table 10: Estimated parameters

	Description	Value
Innovation Parameters		
θ	PL exponent	0.61
α	Y/L- Disruption	0.98
β	Y/L- Innovation	0.02
γ	Growth Rate	0.03
Labor Market Parameters		
$\bar{N}^I(1-u)/\bar{N}^J$	Average Firm Size	50.91
u	Unemployment Rate	0.07
UE	Job Arrival UE	0.01
EE	Job Arrival EE	0.03
δ	Job Displacement	0.02
Observations		242 380

Notes: The table shows parameter estimates.

Figure 15: Innovation Intensities



Notes: The figure shows a graphical representation of the two equations pinning down the estimated α_γ , α_π for a given $\frac{k_\Phi}{k_\Theta}$ and the set of the remaining parameter estimates. The two equations are

$$\alpha_\gamma = \frac{\left(\frac{\gamma}{\theta} - UE \frac{k_\Phi}{k_\Theta} - EE - \delta \left(\alpha^{\frac{1-\theta}{\theta}} - 1\right) - (UE - \delta) \frac{(1-u)}{f}\right)}{\beta \frac{k_\Phi}{k_\Theta}}$$

$$\alpha_\pi = \frac{\delta \frac{k_\Theta u}{k_\Phi} - \frac{\gamma u^2 f}{\theta(1-u)} - UE}{(UE - \delta)}$$

A.5 Mobility patterns over time

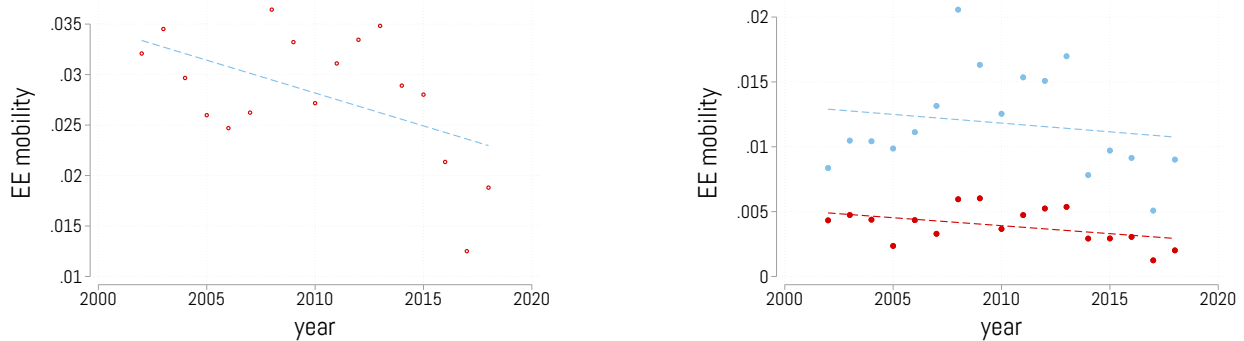


Figure 16: Hiring Rates Evolution

Notes: The left panel shows the average over time of the estimated rate of firm hires from other firms over all population groups. The right figure subdivides the sample into those in the top and bottom income groups.

Table 11: Sub-sample Analysis

	Description	All	Before	After
Innovation Parameters				
θ	PL exponent	0.61	0.51	0.89
α	Y/L- Disruption	0.98	0.98	0.99
β	Y/L- Innovation	0.020	0.019	0.023
γ	Growth Rate	0.028	0.025	0.038
Labor Market Parameters				
$N^I(1-u)/N^J$	Average Firm Size	50.91	52.55	48.69
u	Unemployment Rate	0.072	0.068	0.076
UE	Job Arrival UE	0.013	0.015	0.010
EE	Job Arrival EE	0.027	0.028	0.027
δ	Job Displacement	0.022	0.020	0.026
Observations		233 287	133 948	99 339

Notes: The table shows parameter estimates for the whole sample and two sub-sample analysis, once for the period before 2009 and once after 2009.

References

- Aghion, Philippe, Antonin Bergeaud, and John Van Reenen**, “The Impact of Regulation on Innovation,” *American Economic Review*, November 2023, *113* (11), 2894–2936.
- Akcigit, Ufuk, Murat Alp Celik, and Jeremy Greenwood**, “Buy, Keep, or Sell: Economic Growth and the Market for Ideas,” *Econometrica*, 2016, *84* (3), 943–984.
- Almeida, Paul and Bruce Kogut**, “Localization of Knowledge and the Mobility of Engineers in Regional Networks,” *Management Science*, 1999, *45* (7), 905–917.
- Andersen, Steffen and Kasper Meisner Nielsen**, “Participation Constraints in the Stock Market: Evidence from Unexpected Inheritance Due to Sudden Death,” *The Review of Financial Studies*, 2011, *24* (5), 1667–1697.
- Arora, Ashish, Sharon Belenzon, Andrea Pataconi, and Jungkyu Suh**, “The Changing Structure of American Innovation: Some Cautionary Remarks for Economic Growth,” *Innovation Policy and the Economy*, 2020, *20*, 39–93.
- Audoly, Richard**, “Firm Dynamics and Random Search over the Business Cycle,” Technical Report 2023.
- Baksy, Aniket, Daniele Caratelli, and Niklas Engbom**, “The Long-term Decline of the US.S. Job Ladder,” Technical Report 2024.
- Balke, Neele and Thibaut Lamadon**, “Productivity Shocks, Long-Term Contracts, and Earnings Dynamics,” *American Economic Review*, 2022, *112* (7), 2139–77.
- Bartelsman, Eric J., Pieter A. Gautier, and Joris De Wind**, “Employment Protection, Technology Choice, and worker allocation,” *International Economic Review*, 2016, *57* (3), 787–826.
- Becker, Sascha O and Hans K Hvide**, “Entrepreneur Death and Startup Performance*,” *Review of Finance*, 05 2021, *26* (1), 163–185.
- Benhabib, Jess, Jesse Perla, and Christopher Tonetti**, “Reconciling Models of Diffusion and Innovation: A Theory of the Productivity Distribution and Technology Frontier,” *Econometrica*, 2021, *89* (5), 2261–2301.

- Bennedsen, Morten, Francisco Pérez-González, and Daniel Wolfenzon**, “Do CEOs Matter? Evidence from Hospitalization Events,” *The Journal of Finance*, 2020, 75 (4), 1877–1911.
- Bertheau, Antoine, Pierre Cahuc, Simon Jaeger, and Rune Vejlin**, “Turnover Costs: Evidence from Unexpected Worker Separations,” *Working Paper*, 2022.
- Bilal, Adrien, Niklas Engbom, Simon Mongey, and Giovanni L. Violante**, “Labor Market Dynamics When Ideas are Harder to Find,” Working Paper 29479, National Bureau of Economic Research November 2021.
- , –, –, and –, “Firm and Worker Dynamics in a Frictional Labor Market,” *Econometrica*, 2022, 90 (4), 1425–1462.
- Bloesch, Justin, Birthe Larsen, and Bledi Taska**, “Which Workers Earn More at Productive Firms? Position Specific Skills and Individual Worker Hold-up Power,” Technical Report 2022.
- Braunerhjelm, Pontus, Ding Ding, and Per Thulin**, “Labour market mobility, knowledge diffusion and innovation,” *European Economic Review*, 2020, 123, 103386.
- Brooke, Hannah Louise, Mats Talbäck, Jesper Hörnblad, Lars Age Johansson, Jonas Filip Ludvigsson, Henrik Druid, Maria Feychting, and Rickard Ljung**, “The Swedish cause of death register,” *European Journal of Epidemiology*, 2017, 32 (9), 765–773.
- Buera, Francisco J. and Ezra Oberfield**, “The Global Diffusion of Ideas,” *Econometrica*, 2020, 88 (1), 83–114.
- Carlsson, Mikael and Oskar Nordstrom Skans**, “Evaluating Microfoundations for Aggregate Price Rigidities: Evidence from Matched Firm-Level Data on Product Prices and Unit Labor Cost,” *American Economic Review*, 2012, 102 (4), 1571–95.
- Da-Rocha, José-María, Diego Restuccia, and Marina Mendes Tavares**, “Firing costs, misallocation, and aggregate productivity,” *Journal of Economic Dynamics and Control*, 2019, 98, 60–81.
- Davis, Steven J. and John Haltiwanger**, “Gross Job Creation, Gross Job Destruction, and Employment Reallocation,” *The Quarterly Journal of Economics*, 1992, 107 (3), 819–863.

- **and** –, “Labor Market Fluidity and Economic Performance,” NBER Working Papers 20479, National Bureau of Economic Research, Inc September 2014.
- Decker, Ryan A., John Haltiwanger, Ron S. Jarmin, and Javier Miranda**, “Declining Business Dynamism: What We Know and the Way Forward,” *American Economic Review*, May 2016, *106* (5), 203–07.
- Engbom, Niklas**, “Misallocative Growth,” Technical Report 2023.
- Fujita, Shigeru, Giuseppe Moscarini, and Fabien Postel-Vinay**, “Measuring Employer-to-Employer Reallocation,” *American Economic Journal: Macroeconomics* Forthcoming.
- Harrigan, James, Ariell Reshef, and Farid Toubal**, “Techies and Firm Level Productivity,” Working Paper 31341, National Bureau of Economic Research June 2023.
- Hoey, Sam, Thomas Peeters, and Jan C. van Ours**, “The impact of absent co-workers on productivity in teams,” *Labour Economics*, 2023, *83*, 102400. European Association of Labour Economists (EALE) Conference 2022.
- Hopenhayn, Hugo, , and Liyan Shi**, “Knowledge Creation and Diffusion with Limited Appropriation,” Technical Report 2020.
- **and Richard Rogerson**, “Job Turnover and Policy Evaluation: A General Equilibrium Analysis,” *Journal of Political Economy*, 1993, *101* (5), 915–938.
- Hummels, David, Rasmus Jørgensen, Jakob Munch, and Chong Xiang**, “The Wage Effects of Offshoring: Evidence from Danish Matched Worker-Firm Data,” *American Economic Review*, June 2014, *104* (6), 1597–1629.
- Hyatt, Henry R. and James R. Spletzer**, “The shifting job tenure distribution,” *Labour Economics*, 2016, *41*, 363–377. SOLE/EALE conference issue 2015.
- Jaffe, Adam B., Manuel Trajtenberg, and Rebecca Henderson**, “Geographic Localization of Knowledge Spillovers as Evidenced by Patent Citations,” *The Quarterly Journal of Economics*, 1993, *108* (3), 577–598.
- Jäger, Simon and Jørg Heining**, “How substitutable are workers? Evidence from worker deaths.,” mimeo 2019.
- Jaravel, Xavier, Neviana Petkova, and Alex Bell**, “Team-Specific Capital and Innovation,” *American Economic Review*, April 2018, *108* (4-5), 1034–73.

- Jarosch, Gregor, Ezra Oberfield, and Esteban Rossi-Hansberg**, “Learning From Coworkers,” *Econometrica*, 2021, 89 (2), 647–676.
- Jones, Benjamin and Benjamin A. Olken**, “Do Leaders Matter? National Leadership and Growth Since World War II,” *The Quarterly Journal of Economics*, 2005, 120 (3), 835–864.
- Kaiser, Ulrich, Hans Christian Kongsted, and Thomas Rønde**, “Does the mobility of RD labor increase innovation?,” *Journal of Economic Behavior & Organization*, 2015, 110, 91–105.
- Klette, Tor Jakob and Samuel Kortum**, “Innovating Firms and Aggregate Innovation,” *Journal of Political Economy*, 2004, 112 (5), 986–1018.
- Koenig, Michael, Jan Lorenz, and Fabrizio Zilibotti**, “Innovation vs. imitation and the evolution of productivity distributions,” *Theoretical Economics*, September 2016, 11 (3).
- Kortum, Samuel S.**, “Research, Patenting, and Technological Change,” *Econometrica*, 1997, 65 (6), 1389–1419.
- Lentz, Rasmus and Dale Mortensen**, “Labor Market Friction, Firm Heterogeneity, and Aggregate Employment and Productivity,” 2022 Meeting Papers, BSE 2022.
- Leonard, Jonathan S.**, “In the Wrong Place at the Wrong Time: The Extent of Frictional and Structural Unemployment,” Working Paper 1979, National Bureau of Economic Research July 1986.
- Lim, Zaneta, Karen Gibbs, James E. Potts, and Shubhayan Sanatani**, “A review of sudden unexpected death in the young in British Columbia,” *Canadian Journal of Cardiology*, 2010, 26 (1), 22–26.
- Lise, Jeremy and Fabien Postel-Vinay**, “Multidimensional Skills, Sorting, and Human Capital Accumulation,” *American Economic Review*, August 2020, 110 (8), 2328–76.
- **and Jean-Marc Robin**, “The Macrodynamics of Sorting between Workers and Firms,” *American Economic Review*, April 2017, 107 (4), 1104–35.
- Liu, Jignan**, “Worker Mobility, Knowledge Diffusion, and Non-Compete Contracts,” Technical Report 2023.

- Lucas, Robert E. and Benjamin Moll**, “Knowledge Growth and the Allocation of Time,” *Journal of Political Economy*, 2014, 122 (1), 1–51.
- Luttmer, Erzo G. J.**, “Selection, Growth, and the Size Distribution of Firms*,” *The Quarterly Journal of Economics*, 08 2007, 122 (3), 1103–1144.
- Meinen, Philipp, Pierpaolo Parrotta, Davide Sala, and Erdal Yalcin**, “Managers as knowledge carriers – Explaining firms’ internationalization success with manager mobility,” *Journal of International Economics*, 2022, 138, 103633.
- Mion, Giordano and Luca David Opromolla**, “Managers’ mobility, trade performance, and wages,” *Journal of International Economics*, 2014, 94 (1), 85–101.
- Mukoyama, Toshihiko and Sophie Osotimehin**, “Barriers to Reallocation and Economic Growth: The Effects of Firing Costs,” *American Economic Journal: Macroeconomics*, October 2019, 11 (4), 235–70.
- Perla, Jesse and Christopher Tonetti**, “Equilibrium Imitation and Growth,” *Journal of Political Economy*, 2014, 122 (1), 52–76.
- Poschke, Markus**, “Employment protection, firm selection, and growth,” *Journal of Monetary Economics*, 2009, 56 (8), 1074–1085.
- Postel-Vinay, Fabien and Jean-Marc Robin**, “Equilibrium Wage Dispersion with Worker and Employer Heterogeneity,” *Econometrica*, 2002, 70 (6), 2295–2350.
- Saez, Emmanuel, Benjamin Schoefer, and David Seim**, “Payroll Taxes, Firm Behavior, and Rent Sharing: Evidence from a Young Workers’ Tax Cut in Sweden,” *American Economic Review*, 2019, 109 (5), 1717–63.
- Sauvagnat, Julien and Fabiano Schivardi**, “Are Executives in Short Supply? Evidence from Death Events,” *The Review of Economic Studies*, 02 2023, p. rdad027.
- Serafinelli, Michel**, ““Good” Firms, Worker Flows, and Local Productivity,” *Journal of Labor Economics*, 2019, 37 (3), 747–792.
- Singh, Jasjit and Ajay Agrawal**, “Recruiting for Ideas: How Firms Exploit the Prior Inventions of New Hires,” *Management Science*, 2011, 57 (1), 129–150.
- Sorkin, Isaac**, “Ranking firms using revealed preference,” *The quarterly journal of economics*, 2018, 133 (3), 1331–1393.

Stoyanov, Andrey and Nikolay Zubanov, “Productivity Spillovers across Firms through Worker Mobility,” *American Economic Journal: Applied Economics*, April 2012, 4 (2), 168–98.

Tambe, Prasanna and Lorin M. Hitt, “Job Hopping, Information Technology Spillovers, and Productivity Growth,” *Management Science*, 2014, 60 (2), 338–355.